ISOTOPE METHODS FOR DATING OLD GROUNDWATER



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INTERNATIONAL ATOMIC ENERGY AGENCY VIENNA, 2013

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FOREWORD

In many parts of the world, groundwater constitutes a major source of water for agricultural, energy, industrial and urban use, and it is expected to play an even greater role in the next decades on a global scale. The rising importance of groundwater is a result of increasing water demands deriving from population growth and concerns about the impact of predicted climate change on the hydrological cycle. Unfortunately, in many cases, water officials and managers lack the knowledge of the local groundwater resources required to ensure adequate and long term access to available water resources. In order to adopt adequate policies and to share resources with limited accessibility, sound and comprehensive information on the amount and condition of existing water resources is required.

New scientific, technical, social and legal questions and a growing number of conflicts and issues regarding water usage require a better understanding of the movement, origin and age of groundwater. Isotope hydrology methods have great potential to provide the hydrogeological information required to rapidly and effectively assess and map groundwater resources. For several decades, one of the major tools for obtaining information about groundwater origin, and its properties and movement has been the use of isotopes, which has often provided insights not available using other techniques. Information on groundwater age is required to address aspects such as recharge rates and mechanisms, resource renewability, flow rate estimation in aquifers and vulnerability to pollution, especially when dealing with shared water resources. Age information, mainly provided by radionuclides and modelling, is considered highly relevant for validating conceptual flow models of groundwater systems, calibrating numerical flow models and predicting the fate of pollutants in aquifers. Isotope tracers are now used to study groundwater age and movement, covering time spans from a few months up to a million years.

The understanding of groundwater occurrence and movement in large continental basins has been a matter of debate among experts. Despite the large number of studies which have been carried out in the past, many open questions remain, and ideas and concepts are often revised based on new conceptual models, isotope and tracer analyses or water flow models. The book's 14 chapters explain what is currently understood about the use and application of radionuclides and related geochemical tracers and tools to assess groundwater age and movement over time spans beyond a few thousand years.

The IAEA officers responsible for this publication were A. Suckow, P.K. Aggarwal and L. Araguas-Araguas of the Division of Physical and Chemical Sciences.

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Chapter 1

INTRODUCTION

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1.1. BACKGROUND

Groundwater is the largest component of fresh water accessible for human use. While two thirds of the surface area of planet Earth is covered with water, most of it is sea water or saline and only 2.5% is fresh water (Shiklomanov and Rodda (2004) [1]). A large portion of this fresh water — nearly 69% — is bound in ice and permanent snow cover in the Antarctic and Arctic, and in continental mountains. About 30% of fresh water, or 0.75% of all water on Earth, is present as fresh groundwater. Only 0.26% of the total amount of fresh water on Earth is in lakes, rivers and reservoirs that are most easily accessible for human use (the remaining 1% is estimated to occur as soil moisture, swamp water and permafrost). Groundwater, in both renewable and non-renewable aquifers, accounts for about 95% of accessible fresh water or 0.7% of all water on Earth, and provides more than half of all domestic and irrigation water used around the world (Fig. 1.1). In semi-arid and arid regions, and in domestic supplies for rural areas, 80–100% of all fresh water may be derived from groundwater.

In many parts of the world, groundwater levels are rapidly declining as groundwater withdrawal far exceeds natural recharge. Irrigated agriculture, particularly from groundwater, has been responsible for many of the strides made in self-sufficient food production in parts of Asia and has contributed to the 'green revolution' of the 1960s, resulting in greater food security. It is now estimated that more than half of the world's food production is derived from irrigated agriculture. Owing to the extent that fossil or non-renewable groundwater is being used to increase food production, both the water supply and food production may potentially become unsustainable in the future. The United Nations' Millennium Development Goals, adopted in 1999 by the governments of nearly 180 countries, and subsequent commitments, include the goal "to stop the unsustainable exploitation of water resources by developing water management strategies at the regional, national and local levels..."

Sustainable use and management of aquifers necessitates an understanding of aquifer hydrogeology and its dynamics. This understanding can be gained over a period of decades by observations and measurements of precipitation, river flows, groundwater levels, etc. Early developments in groundwater hydrology focused on means to estimate aquifer storativity and hydraulic conductivity, which led to the establishment of the theory of transient groundwater flow (Anderson (2008) [2]). Isotope techniques



FIG. 1.1. Occurrence of water on Earth (based on data from Shiklomanov and Rodda (2004) [1]).



FIG. 1.2. Distribution of ¹⁴C in groundwater in northern Africa.

— and particularly those that can be applied to estimate the age of groundwater — help to cost effectively build a conceptual framework of aquifer hydrogeology and flow system. The use of groundwater age for estimating aquifer storage, the rate of groundwater renewal and flow velocity was conceived as early as the natural radioactivity of tritium and ¹⁴C was discovered more than sixty years ago (Aggarwal et al. (2012) [3]). Groundwater age also provides unmatched advantages for improving numerical models of groundwater flow in large, regional aquifers where water level data are normally scarce.

The age of groundwater ranges from less than a month to a million years, or perhaps more. Old groundwater — defined in this book as groundwater with estimated ages greater than about one thousand years — occurs in many African, Asian and Latin American aquifers as indicated by measured ¹⁴C activities (IAEA (2007) [4]). The Nubian Aquifer in northern Africa, for example, is estimated to contain groundwater that was recharged at various times over the past million years (Sturchio et al. (2004) [5]). Figure 1.2 shows the distribution of groundwater ¹⁴C in northern and central Africa. This groundwater is presently used for drinking and irrigation. With an increasing population and potential changes in the current climate, it will become an even more important resource for meeting the fresh water demands of the region. It is crucial to understand the nature of recharge and groundwater flow in past climates in order to better characterize the changes that may be induced under new climate regimes.

1.2. OBJECTIVES

This book aims to provide the reader with a comprehensive understanding of why groundwater age is an important parameter for characterizing aquifer hydrogeology, how to estimate groundwater ages using different isotopes and how best to use age data for the analysis of groundwater flow.

1.3. SCOPE

A number of isotopes can be used to interpret groundwater ages over a wide range of timescales. (Fig. 1.3). A need was identified to create a synthesis of various isotope methods to date old groundwater and to critically evaluate their advantages and disadvantages for use in hydrology. This book is intended to provide hydrogeologists with a guideline describing existing sampling and measurment methods, and to provide tools to ensure reliability of the resulting interpretation of isotope data. A 'critical' evaluation is intended to assess sampling efforts required in the field and to select possible cooperation partners



FIG. 1.3. Isotope and chemical tracers use for estimating groundwater age.

and assess the problems inherent to each method, as well as model assumptions which lead to water age results of 20 000 to 1 million years.

It is hoped that sufficient detail and examples have been provided to convey to the reader that obtaining meaningful hydrological information from groundwater age data requires careful planning and sampling, skilled measurements and a significant number of cross checks to evaluate various assumptions. It is to be cautioned that an age estimate based on a single isotope or tracer at a single location may not be very informative. Multiple estimates, based on more than one tracer and at multiple locations, particularly when combined with a numerical model sufficient to represent the flow regime of the groundwater system of interest, are necessary to meaningfully use groundwater age data.

1.4. STRUCTURE

Chapter 2 describes fundamental concepts, data needs, and approaches that aid in developing a general understanding of groundwater systems. Chapter 3 discusses in detail the meaning of groundwater age in a physical hydrological system along with pitfalls to be avoided by misinterpreting or over-interpreting age data. The subsequent five chapters describe the basis for and use of various isotope methods for dating of old groundwater: ¹⁴C, ⁸¹Kr, ³⁶Cl, uranium isotopes and ⁴He.

The use of multiple isotope tracers and its potential advantages over single tracers are discussed in Chapter 9. Chapter 10 outlines the methods for combining results of groundwater age determination with quantitative numerical models of groundwater flow and transport processes within an aquifer. Finally, a series of case studies on the use of groundwater ages to characterize large, regional aquifer systems is presented. These include the Milk River aquifer in Canada (Fröhlich), the Santa Fe Group aquifer system of the Middle Rio Grande Basin in the United States of America (Plummer et al.), the Eastern Great Artesian Basin in Australia (Torgersen) and the Nubian aquifer system in northern Africa (Sturchio and Purtschert).

A wide variety of readers involved in groundwater research or in the exploration, management, planning and utilization of groundwater resources may find this book useful. Those interested in the use of multiple tracers to determine and use groundwater age data may gain a better understanding of the subject by reading all of the chapters in the order they are presented. A reader new to the concepts of groundwater dating who wants a general overview of the topic may wish to first read Chapter 2 (characterization and conceptualization), a definition of the concepts of groundwater age used in this book (Chapter 3) followed by case studies (Chapters 11–14). Readers who are familiar with isotope

techniques in general and are in need of information related to a specific isotope may wish to go directly to Chapters 4–8. Hydrologists and modellers who may not be interested in the details of the tracer techniques but in the application of groundwater tracers may wish to begin with Chapters 2 and 3, followed by Chapters 9 and 10 (system analysis using multitracer approaches and groundwater models, respectively).

Chapter 2

CHARACTERIZATION AND CONCEPTUALIZATION OF GROUNDWATER FLOW SYSTEMS

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2.1. INTRODUCTION

This chapter discusses some of the fundamental concepts, data needs and approaches that aid in developing a general understanding of a groundwater system. Principles of the hydrological cycle are reviewed; the processes of recharge and discharge in aquifer systems; types of geological, hydrological and hydraulic data needed to describe the hydrogeological framework of an aquifer system; factors affecting the distribution of recharge to aquifers; and uses of groundwater chemistry, geochemical modelling, environmental tracers and age interpretations in groundwater studies. Together, these concepts and observations aid in developing a conceptualization of groundwater flow systems and provide input to the development of numerical models of a flow system. Conceptualization of the geology, hydrology, geochemistry, and hydrogeological and hydrochemical framework can be quite useful in planning, study design, guiding sampling campaigns, acquisition of new data and, ultimately, developing numerical models capable of assessing a wide variety of societal issues — for example, sustainability of groundwater resources in response to real or planned withdrawals from the system, CO_2 sequestration or other waste isolation issues (such as nuclear waste disposal).

Tracer model ages can often help improve understanding of groundwater flow. Once developed, numerical models of groundwater flow can be used to test derived age information for consistency with geologic, hydrological and geochemical data, and to estimate the modern and palaeorecharge rates of an aquifer.

As the topic of conceptualization and characterization of groundwater systems is broad and complex, the reader is referred to some of the many useful references in the hydrological literature where additional information can be found (see, for example, texts by Bear (1979) [6]; de Marsily (1986) [7]; Domenico and Schwartz (1998) [8]; Driscoll (1986) [9]; Fetter (2000) [10]; Freeze and Cherry (1979) [11]; Mazor (2004) [12]; Todd and Mays (2005) [13]). Other examples can be found in some of the reports of hydrological investigations in the literature (see, for example, Back et al. (1988) [14]; Glynn and Plummer (2005) [15]; Glynn and Voss (1999) [16]; Heath (1984) [17]; Miller (2000) [18]; Reilly et al. (2008) [19]; Sanford et al. (2006) [20]; Thorn et al. (1993) [21]), or in training documents and other general references of the United States Geological Survey (USGS) (Franke et al. (1993) [22]; Franke et al. (1990) [23]; Heath (1983) [24]; Reilly et al. (1987) [25]).

2.2. THE GROUNDWATER FLOW SYSTEM

Groundwater is an important water resource that is critical for survival in many parts of the world. Environmental and isotopic tracers have become an important tool in the evaluation of that resource. Groundwater is, however, also part of the Earth's hydrological cycle. Thus, to understand a groundwater system and what tracers can reveal about it, it is important to first have an understanding of the entire hydrological cycle and how groundwater interacts with other parts of the cycle.

2.2.1. Hydrological cycle

Water on Earth is stored mainly as salt water in the oceans, but the fresh water that is required for life is present in atmospheric water vapour, as ice, mainly in the polar regions, and as liquid water in lakes, rivers, the soil, in unconsolidated geological materials, and in the cracks and pore spaces in rocks underground (Table 2.1).

Water cycles through these reservoirs by falling as precipitation on the land surface, partially running off into lakes and streams, partially evaporating and transpiring from the soil back into the atmosphere, and partially infiltrating through the soil and recharging groundwater reservoirs (Fig. 2.1). Water percolates downwards through the soil zone, where the pore spaces are still partially air-filled, and eventually reaches the water table (defined as where water pressure equals atmospheric pressure), where the pore spaces are completely saturated with water. The groundwater system consists of the entire thickness of water filled unconsolidated sediment and/or rock beneath the water table; however, the degree to which water is stored and transmitted in different geological materials varies dramatically. Groundwater will migrate from areas of high elevation to discharge into streams at lower elevations. These streams carry the water back to the oceans, where it can evaporate and fall again as precipitation. Groundwater near the coast can discharge directly into the oceans in submarine springs or seeps. Water levels observed in wells reflect the energy of the groundwater that feeds them.

The availability of groundwater for use as a resource depends not only on the quantity and quality of water in residence at any given time, but also on the rate that water replenishes a groundwater aquifer (Healy et al. (2007) [27]). Dating of groundwater using environmental or isotopic tracers helps in estimating groundwater age and can help evaluate the rate at which the groundwater is replenished. Physical measurements of water fluxes in the hydrological cycle also provide direct estimates of groundwater replenishment or recharge rates.

Evapotranspiration, the combination of direct evaporation and transpiration by plants, consumes much water of the total precipitation that falls upon the land surface. In cold regions, this can be less than half of the total precipitation, but in temperate climates, it is usually about two thirds of the precipitation, and in arid climates evapotranspiration can account for all but a small percentage of precipitation. Evapotranspiration can be measured at the land surface, usually by means of an energy budget, but in many temperate watersheds it can also be estimated as the difference between

Water source	Volume (10 ³ km ³⁾	Per cent of total fresh water
Salt water		
Oceans	1 350 000	
Fresh water		
Ice	27 800	69.3
Groundwater	8000	29.9
Lakes	220	0.55
Soil moisture	70	0.18
Atmosphere	15.5	0.038
Reservoirs	5	0.013
Rivers	2	0.005
Biomass	2	0.005

TABLE 2.1. GLOBAL WATER DISTRIBUTIONS ON EARTH (after Mook(2000) [26])



FIG. 2.1. The hydrological cycle. Numbers are annual water fluxes in 10³ km³ per year (Mook (2000) [26]; see also: http://ga.water.usgs.gov/edu/watercycle.html).

the average amount of precipitation falling on the watershed and the average discharge into streams from that watershed. The average discharge from a stream represents the water that has either run off during rain events or seeped into the stream as baseflow. This approach works best when inflow and outflow of groundwater as underflow directly from or to an adjoining watershed can be assumed to be small. Baseflow measurement within a stream and the exchange of groundwater and surface water are an important and frequently used method for estimating fluxes within a groundwater system.

The porosity, or storage capacity, of rocks and unconsolidated sediments can vary from less than 1% for fractured rocks to greater than 50% for fine grained sediments. The permeability, or hydraulic conductivity, of rocks or unconsolidated sediment is a measurement of how easily they can transmit water, and this can vary between geological materials by many orders of magnitude (Freeze and Cherry (1979) [11]; Heath (1983) [24]). Rock types and/or unconsolidated sediments within the groundwater system of interest, therefore, have an enormous impact on its storage capacity, replenishment rate and capability to yield water to wells in substantial quantities. Thus, it is essential that a hydrogeological study be performed as thoroughly as resources permit to determine the nature and distribution of the rocks and/or unconsolidated sediments, and to estimate their hydraulic properties.

2.2.2. Timescales for recharge and discharge

Even within a groundwater system of a uniform rock type, the length of a flow path and the time of travel for water along that path can vary greatly. Rolling topography will itself create flow path variability within a system (Tóth (1963) [28]). Water that recharges near streams will stay within local, shallow flow systems and discharge within a few years to tens of years after recharge. Water that recharges further from streams will follow intermediate flow systems of moderate depth, and discharge hundreds to thousands of years after recharge. Water that recharges near topographic divides furthest from streams can take deep flow paths in regional flow systems that discharge after tens of thousands of years or longer after recharge (Fig. 2.2). Such recharge may have occurred during different climatic



FIG. 2.2. Generalized block diagram showing conceptualization of groundwater recharge, discharge and groundwater age in a basin fill groundwater flow system (modified from Hely et al. (1971) [29]; Thiros (2000) [30]; not to scale).

conditions, such as during the most recent glacial cycle when precipitation and recharge rates were frequently higher than observed today in many locations.

2.3. CHARACTERIZATION OF GROUNDWATER FLOW SYSTEMS

In characterizing a groundwater flow system and developing a conceptualization of groundwater flow, three general classes of data are needed: geological, hydrological and geochemical.

2.3.1. Geological framework

One way of developing a geological framework of a groundwater flow system is to develop a three dimensional visualization describing its physical features. Basic features of a three dimensional geological description include characterization of thickness and lithology of rocks/sediment that compose the various geological units of the groundwater flow system and a description of geological structures. Some lithologic properties that need to be considered include effective porosity, permeability, mineralogy and their spatial and depth variations.

Mapping of faults, fracture systems, folds in rock and the orientation of these structures in relation to the direction of groundwater flow is critical in assessing the geological framework and controls on groundwater flow. Depending on their physical properties, geological structures, such as faults, can either enhance or retard groundwater flow. Regional variations in lithologic properties contribute to aquifer heterogeneity. From the standpoint of interpreting environmental tracer data, it is important to have a good understanding of aquifer heterogeneity, such as low permeability zones, confining layers or highly fractured domains, because they can act as sources or sinks for some of the environmental tracers used for age estimation.

The environmental tracers considered in this book can be affected variously by interactions with confining layers, diffusion into or from low permeability zones, convergence/divergence of flow paths, in situ production through nuclear reactions and, in some cases, geochemical interaction with the minerals of the aquifer matrix or those in low permeability zones. Therefore, information on aquifer heterogeneity is essential when interpreting environmental tracer data in 'old' (as used in this book, 'old' is defined as generally greater than 1000 a) groundwater.

There are a number of geophysical techniques that can be used to characterize aquifer heterogeneity (see, for example, http://water.usgs.gov/ogw/bgas/g2t.html). However, there is never enough geophysical information from boreholes, well logs, cores or cuttings to completely describe aquifer heterogeneity throughout a system. Surface geophysical techniques (such as seismic surveys) and even remote sensing techniques (such as InSAR: http://quake.usgs.gov/research/deformation/modelling/InSAR/index.html) are also very useful in constructing a conceptual description of the hydrogeological framework.

Geological mapping and construction of geological cross-sections of a groundwater flow system improve understanding of the spatial distribution of structural features, lithologic facies changes and, generally, the consequent spatial variations in hydraulic conductivity and mineralogy, as well as their heterogeneous distribution through the groundwater system being studied. Sedimentary basin modelling, stratigraphic modelling and structural modelling are some of the types of geological evolution simulation modelling now being used more frequently by hydrogeologists to describe the evolution of aquifer units after development by the oil and gas industry. Sedimentary basin modelling has also been used to understand the transport and fate of pore fluids and the palaeohydrology of sedimentary basins (Bethke (1985) [31]).

2.3.2. Hydrological framework

Essential information in construction of a hydrological framework includes land-surface elevation, locations of rivers and other drainage, areal distribution of precipitation, delineation of recharge and discharge areas, determination of a water balance for the groundwater flow system, mapping of the altitude of the potentiometric surfaces of the aquifers, and characterization of regional variability in the hydraulic properties of a groundwater flow system. The hydrological framework of a groundwater flow system can be visualized in maps of the potentiometric surface of aquifers, in cross-sections showing the relation of groundwater flow to the geological framework, and ultimately through a numerical model capable of simulating groundwater flow.

2.3.2.1. Water levels

Darcy's law states that groundwater flux is directly proportional to the gradient in the hydraulic head, or water level, and the hydraulic conductivity of the porous media (rock or sediment). Hydraulic gradients can be determined from contours drawn on maps defining lines of equal head depicting historical (pre-development, i.e. pre-pumping) water levels in unconfined aquifers or from water levels in piezometers in confined aquifers (see, for example, Bexfield (2002) [32]). Groundwater generally flows down the hydraulic gradient in directions normal to the lines of equal head. In confined aquifers, the hydraulic gradient is determined by mapping water levels in wells open to the aquifer of interest. Given the nature of aquifer heterogeneity and the fact that different wells can be open to different depths and different screened intervals within an aquifer, the mapped potentiometric surface is usually more

appropriately applied to regional flow characteristics than to local scale flow conditions. Information on well construction is critical in identifying wells that are only open to the aquifer of interest when mapping the potentiometric surface of a specific aquifer.

Thus, if the water levels are measured in a large number of wells in a groundwater system, it is possible to get an indication of the direction of water movement and the relative hydraulic conductivities of different parts of a geological framework. By combining water level measurements with estimated recharge rates, groundwater fluxes within a system can be calculated. As water takes the path of least resistance, it will preferentially follow more permeable layers or fracture zones. For this reason, it is often useful to have clusters, or nests, of wells at the same location that have screens open at different depths. In discharge areas, the water levels in deeper wells will be above the levels existing in shallower wells. Where layers or regions of low permeability exist, steep head gradients may also exist. In layered systems of alternating high and low permeability, flow in the former tends to be mostly horizontal, whereas flow in the latter tends to be mostly vertical. Water levels at and near points of groundwater extraction will decrease in proportion to the amount of water extracted.

A network of wells for the purpose of measuring water levels and collecting samples for analysis of environmental tracers is a basic and essential part of any groundwater investigation. Usually, such a network is assembled from existing wells open to the aquifer of interest. Essential data include well location and total depth, depth and length of the interval open to the aquifer, land surface elevation, and recognition of wells that may be open to multiple aquifers or to multiple depths within the aquifer of interest. Well construction information should be examined in relation to the geological framework to determine whether the water is derived from the aquifer of interest.

The drilling of additional wells can be very beneficial if the new wells are located where information is needed. A retrospective compilation of hydraulic data for existing wells and springs can help identify areas that should be targeted for further study. Attention should also be paid to the length of the well screen or open interval. Often, wells in fractured rock terrain or wells that are used for water extraction are open over relatively large aquifer thicknesses to maximize well yield. This reduces the usefulness of a well in interpreting water levels and environmental tracers as both types of observations are integrated vertically and, thus, cannot provide information on vertical segregation of water in the system.

A better choice for observation wells is to have a short screened interval, and to have multiple such wells at a single location; this applies to both water level and tracer measurements. In shallow water table aquifers, transient changes in water levels often occur seasonally for wells screened near the water table, with higher water levels occurring in the winter and spring when evapotranspiration is low and recharge high. It may be necessary to monitor such water levels for several seasons in order to obtain an average water level that is useful for conceptualizing a regional average flow system.

2.3.2.2. Hydraulic properties

As mentioned previously, the type and distribution of rocks and unconsolidated sediments within a groundwater system can be a major factor affecting the rate and movement direction of water. The hydraulic conductivity of rocks and sediment can vary by more than 12 orders of magnitude. This can lead to differences of several orders of magnitude in fluxes and hydraulic gradients that are established within natural flow systems. Rock types with the highest hydraulic conductivity include karstified limestones and some volcanic rocks. Rock types with the lowest hydraulic conductivity include crystalline rocks, some fractured rocks and well-lithified sedimentary rocks, especially shales and other argillaceous lithologies. However, local zones or fractures within such rocks can be relatively permeable. Unconsolidated sediments can vary widely in their permeability, which usually correlates with sediment grain size, grain sorting and depth of burial. Gravels are extremely permeable, whereas clays typically have low permeability. Well sorted sediments will be more permeable than their poorly sorted equivalents, and burial tends to compact the sediments, decreasing both their porosity and their permeability. The hydraulic properties of rocks or sediment can often be measured in situ. Measurements of hydraulic conductivity can also be made on core samples in the laboratory, but these small scale measurements usually have a low bias because they do not incorporate the larger scale features such as fractures or bedding. The hydraulic conductivity or transmissivity of an aquifer (its hydraulic conductivity multiplied by its thickness) is frequently measured using an aquifer test. The simplest form of these is a slug test, where a known volume of water is added or withdrawn quickly, and the water level is measured over time as it returns to its original level (Ferris et al. (1962) [33]; Kruseman and de Ridder (1990) [34]; Shuter and Teasdale (1989) [35]). Although slug tests are easy to perform, they often do not work well in highly permeable material (the water level equilibrates very quickly), and the measurement is only influenced by a limited volume of rock or sediment very near the well. A frequent alternative to simple slug tests is more complete aquifer tests, where water is extracted from a well at a constant rate over a period of time, usually at least 1–2 days. Water levels are observed throughout such a test, preferably at a well that is located some distance from an extraction well. This type of test is influenced by a much larger volume of the aquifer than a slug test, so may provide a value that is more reflective of a regional average.

Aquifer storage is also obtainable through an aquifer test, although with a little less accuracy than the transmissivity. In unconfined aquifers, a specific yield represents the volume of water released from storage from a unit area of the studied aquifer per unit decline in the water table. In bedrock aquifers, the storage term is related to compressibility of the rock matrix, which releases water as it undergoes a drop in fluid pressure. This causes a reduction in porosity as the matrix is compressed under the weight of the overburden.

2.3.2.3. Recharge amount and distribution

In spite of the wide range of hydraulic properties associated with various rock types, the recharge rate frequently controls how quickly groundwater is replenished. This is especially true in areas of either moderate to high topographic relief and/or areas that are semi-arid to arid. In arid regions, groundwater recharge is one of the most critical water balance components because of the difficulties in its measurement. Much research has been performed to develop various techniques for measuring recharge directly in the field (de Vries and Simmers (2002) [36]; Scanlon et al. (2002) [37]), but many of these techniques are limited by the fact that they make measurements only over small areas or small time periods, or both. Conventional techniques for estimating recharge rate are based on water balance equations that include hydrometeorological (precipitation-evapotranspiration) and geohydrological (groundwater level changes) parameters. In these equations, recharge is determined as the difference between other balance quantities that are directly measurable. The uncertainty in the measurement of these quantities determines the uncertainty of the recharge rate. If recharge is high, such as in humid regions (10 to more than 100 cm/a), its uncertainty is relatively low. However, in semi-arid and arid areas with recharge rates from virtually 0 to less than 100 mm/a, the uncertainties of measured balance parameters cause very high uncertainty in the estimated recharge rate. Thus, the very approximate nature of these groundwater balance estimations prompts chemical and isotopic studies to independently assess recharge rates. Especially for drier regions, geochemical and isotopic profiling in the unsaturated and shallow groundwater zone is more reliable and accurate than water balance methods and, thus, is practically indispensible for groundwater resource assessments. Geochemical and isotopic tools for recharge rate determination include Cl, chlorofluorocarbons (CFCs), ³H, ³H/³He and ¹⁴C. For groundwater systems with low or even negligible present day recharge, ¹⁴C is one of the most suitable tools.

It is usually not known to what extent modern recharge rates can be applied in estimating palaeorecharge rates. Still, it is important to determine modern recharge rates to provide a benchmark for comparison to palaeorecharge rates once they are derived from groundwater age information and the application of models to the flow system. For a regional groundwater assessment, long term and

spatially averaged recharge rates are usually needed. Local measurements must either be scaled up, or other methods used that integrate larger spatial and timescales. Measurement of baseflow in streams was mentioned earlier as one such approach that can work fairly well in temperate or humid climates, where recharge is often fairly evenly distributed with precipitation.

In semi-arid to arid regions, the distribution of recharge is usually quite heterogeneous, occurring mainly in the mountains or along mountain fronts or ephemeral streams during intermittent runoff events. Local measurement techniques can be useful in areas of focused recharge. In broad areas between mountain ranges or away from streams, recharge can be nearly zero or essentially zero, as can be determined by the accumulation of solute tracers within the unsaturated zone which occurs through continued conditions where evaporation removes the water but not the solutes. The chloride-mass balance technique (Wood and Sanford (1995) [38]) is one method that has proven useful under such conditions.

In humid regions, shallow flow systems usually contain young groundwater. If 'old' groundwater exists today in humid regions, it usually is at sufficient depth or beneath sufficient hydraulic confinement that it is isolated from the active flow system. If of meteoric origin, 'old' groundwater was initially recharged at the land surface, perhaps in outcrop areas along basin margins, or along outcrops at mountain fronts or in outcrops of coastal, wedge shaped aquifers. Subsequent flow has permitted a fraction of this water to reach depths where it is sufficiently isolated from the active flow system on timescales of thousands to more than millions of years. Most aquifers are 'leaky' to some extent and eventually flow to an area of discharge. 'Old' groundwater is found in deep sedimentary basins, usually beneath sequences of confining layers (see, for example, Phillips et al. (1989) [39]), in coastal aquifers beneath confining layers (Aeschbach-Hertig et al. (2002) [40]; Castro et al. (2007) [41]; Stute et al. (1992) [42]), or in arid regions where modern recharge is insufficient to replace the 'old' water or does so only very slowly (Patterson et al. (2005) [43]; Sturchio et al. (2004) [5]).

Aquifers in arid regions today may have been recharged predominantly during pluvial (wet) climatic periods in the past, and today, 'old' water persists due to low recharge rates that are insufficient to flush the groundwater flow system. In some cases, a temporal understanding of changes in areal recharge conditions may be gained from information on the past distribution of vegetation in an area or from other information on the relative pluviosity/aridity in an area. Palaeobotanical studies of pollen or relict vegetation distribution in soils and lake sediment might be useful in this context. Examples of other measures of pluviosity/aridity include tree ring reconstructions; determination of sedimentation rates in varve sequences; radiocarbon dating of palaeolake levels; records of chloride, nitrate and other atmospherically derived solutes in unsaturated zones (Walvoord et al. (2002) [44]) and archaeological evidence of past population migrations in water stressed regions.

In spite of the techniques that are available to directly measure recharge at the land surface, environmental tracers often prove to be the best tools for constraining estimates of long term and spatially averaged recharge rates.

2.3.3. Hydrochemical framework

Data on the concentrations of dissolved solutes, gases and isotopes can provide information about the local area from which they were recharged and can be used to trace groundwater flow on the timescale of the groundwater flow system. Geochemical data can be used to delineate zones of leakage through confining layers, interpret flow in relation to faults and other geological or hydraulic properties of an aquifer, and estimate travel times in groundwater systems. Dissolved gases and stable isotope data (²H and ¹⁸O of groundwater) can be used to recognize palaeowaters and interpret palaeoclimatic recharge conditions. Owing to their different timescales for introduction into aquifers, some environmental tracers can be used to help recognize recharge and discharge areas. Estimates of tracer model age can help to quantify recharge rates.

As part of the well and spring inventory process, all available chemical and isotopic data on water from the aquifer should be compiled, plotted on maps and contoured with respect to a known depth interval. Where available, chemical and environmental tracer data should be plotted as a function of depth in an aquifer. For example, areas of recharge or upward leakage can sometimes be recognized on maps of Cl⁻ concentration in groundwater or from plots of Cl⁻ as a function of depth. In unconfined aquifers, data are typically plotted at mid-depth below the water table of the open interval of a well (see Chapter 12). In some cases, gradients in environmental tracer concentration (and tracer model age) can be used to estimate recharge rate. This analysis will aid in recognition of recharge and discharge areas, defining directions of groundwater flow (see below), identifying areas that should be targeted for additional investigation, and may also provide an assessment of past climatic and environmental changes and palaeorecharge information.

2.3.3.1. Hydrochemical facies — relation of chemistry to groundwater flow

Although the shape of the pre-development potentiometric surface can define recent groundwater flow direction, maps of the potentiometric surface are not available on timescales of interest, such as during the last glacial maximum (LGM). Consequently, maps of the pre-development potentiometric surface may not exactly apply to interpreting palaeogroundwater flow conditions. Still, the shape of the pre-development potentiometric surface usually represents the predominant features of the palaeoflow system. An alternative approach to interpreting palaeoflow directions is to map spatial patterns in water chemistry and isotopic composition that can indicate past directions of groundwater flow.

Geochemical reactions along groundwater flow paths can lead to regional variations in water composition that evolve in the direction of flow. Iso-concentration contours of reacting dissolved constituents drawn on maps of water composition tend to align to the direction of groundwater flow. Glynn and Plummer (2005) [15], Back (1960) [45] and Back (1966) [46] defined the hydrochemical facies concept, placing geochemical observations in the context of groundwater flow in aquifers of relatively homogeneous hydrological and mineralogical properties.

In contrast, it is sometimes possible to distinguish different sources of water to the groundwater flow system on the basis of inert chemical or isotopic constituents (such as Cl⁻; Br⁻; dissolved noble gases and dissolved N₂; ¹⁸O and ²H in water; and sometimes Na⁺, Li⁺ and other chemical and isotopic constituents). In cases where inert tracer concentrations vary spatially along the groundwater recharge area, the path followed by a tracer delineates flow direction (Glynn and Plummer (2005) [15]). In this case, hydrochemical facies (sometimes referred to as 'hydrochemical zones') will align parallel to the flow direction. In more complex cases, the concentration of reactive constituents may vary spatially and temporally along a recharge area, and may also evolve along the direction of flow.

Non-reactive constituents, salinity and reactive constituents that reflect the minerals and geochemical conditions encountered at the time of recharge and in the later geochemical evolution of the groundwater can also provide information on the geological area of recharge and on the geological units traversed by groundwater to their point of sampling. Knowledge of the source and geochemical evolution of the groundwater will be essential in interpreting and adjusting tracer model ages obtained through various dating techniques discussed in this book (such as ¹⁴C and ⁴He). Together with improved/ adjusted estimates of groundwater ages, characterization of different groundwater geochemical facies in the groundwater system may also be used, as is done, for example, by Sanford et al. (2004) [47] and Sanford et al. (2004) [48] for the Middle Rio Grande Basin to calibrate groundwater flow models (and/or eventually fully coupled reactive transport models).

Extracting flow and hydrological information from geochemical observations requires understanding the aqueous reactivity of aquifer materials and the spatial and temporal distribution of recharge compositions. Many of the geochemical patterns observed in groundwater systems can also be related to heterogeneities in either reactive mineral abundances or in hydrological properties, and may be difficult to resolve, given the limited information typically available.

Flow patterns in regional aquifers, deduced from mapping hydrochemical facies and zones, can indicate flow directions that have occurred over timescales considerably greater than the timescale over which present day or even pre-development water levels were established. Differences between regional flow directions deduced from hydrochemical patterns and those indicated by a modern (pre-development) potentiometric surface can indicate changes in hydraulic conditions (such as recharge rate) on a shorter, more recent timescale than those responsible for hydrochemical observations (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]; Plummer et al. (2004) [51]; Sanford et al. (2004) [48]).

Especially in arid areas, groundwater within a regional groundwater flow system may have a number of possible source areas that include various nearby streams, mountain fronts or inflow from other basins. The solute or isotopic character of the water can give clues as to the source area. The study in the Middle Rio Grande Basin of New Mexico, USA (Chapter 12), is an example of how solutes can be used to determine the source of the water, and in turn help elucidate flow paths and the nature of a groundwater flow system.

2.3.3.2. Environmental tracers, hydrochemistry and timescales

Many different solutes and isotopes that recharge with water into a groundwater system provide information on the time since recharge, either because they decay at a known rate, accumulate in an aquifer from in situ processes, or because their concentration in precipitation has changed at a known rate over time (Clark and Fritz (1997) [52]; Cook and Herczeg (1999) [53]). The range in groundwater ages that is reflected in the tracers can vary from a few years to tens or hundreds of thousands of years, to millions of years (Chapter 1). The latter is the focus of this book, with examples given of the various tracers and various field examples. A tracer model age (see Chapter 3) of a sample of water from a well can be combined with the known hydraulic properties of the hydrogeological framework to back-calculate the recharge rate that would be required to yield the interpreted tracer model age. For 'old' groundwater, this may yield recharge rates that are not consistent with modern estimated rates, but that may be consistent with rates that would be expected during earlier and different climatic conditions. In this sense, some tracers can serve as a repository of information on past climatic conditions. The combined measurement of tracer model ages along presumed hydrological flow paths and in vertical profiles in aquifers can be even more useful in estimating travel times and palaeorecharge rates in aquifers.

There are a few chemical and isotopic indicators that can be used in recognizing 'old' groundwater — at least, it may be possible to recognize water from the LGM, about 22 ka calendar years before present (BP). Dissolved gases and the ¹⁸O and ²H isotopic composition of water may be used to estimate elevation and temperature at the time of recharge, and the intensity of recharge (by determining excess air entrapment) for given water samples. The relationship between ¹⁸O and ²H is also useful in determining recharge characteristics, including the extent to which infiltrating groundwater may have been exposed to evaporation. Examples of using noble gas recharge temperatures or recharge temperatures determined from measurements of dissolved nitrogen and argon in groundwater (1993) [54], Aeschbach-Hertig et al. (2000) [55] and Heaton et al. (1983) [56]. Consistently, an average cooling of about 5°C is observed at the LGM globally, though Aeschbach-Hertig et al. (2002) [40] found cooling of nearly 9°C in New Jersey, USA near the last glacial ice margin. Shifts in the stable isotopic composition of groundwater at the LGM to more depleted values are often observed and attributed to lower condensation temperatures (Dansgaard (1964) [57]; Rozanski et al. (1993) [58]; Straaten and Mook (1983) [59]) and changes in moisture source. However, in some coastal aquifers, the isotopic shift is towards enrichment at

the LGM, due in part to enrichment of the stable isotopic composition of ocean water (ice-volume effect) and changes in moisture source (Plummer (1993) [60]).

Groundwater recharged during the last glacial period is generally regarded as non-renewable on human civilization timescales. That is, once withdrawn from aquifers, natural recharge processes are not sufficient to replace the water on timescales of thousands of years. Recognizing non-renewable groundwater resources is critical to managing water supplies for future generations. Similarly, very 'old' groundwater, water recharged on the hundred thousand to million year timescale, is fossil water and equally non-renewable. Its identification is equally critical in guiding future management decisions and the need to locate other water resources, including those that may provide sustainable water supplies for the future (Alley et al. (1999) [61]) or act as waste containment barriers.

2.3.3.3. Obtaining representative samples from wells

One of the most difficult problems in groundwater hydrochemistry is obtaining samples that are representative of unaltered formation water. Part of the problem is that due to well construction or the physical properties of spring sources, almost all samples are mixtures, combining all of the flowlines reaching a well screen or discharge point. In some cases, water reaching the open interval of a well or discharging at a spring may be nearly uniform in age, but, in general, it is usually necessary to assume that discharge from wells and springs consists of different components with varying ages, i.e. consists of a frequency distribution of age (see Chapter 3). Such mixtures can occur naturally in an aquifer as a result of aquifer heterogeneity, but are also created through the sampling process. In the case of wells with large open intervals to an aquifer, the discharge is a mixture of all of the flowlines drawn into the open interval of a well. In the case of springs, the discharge also typically represents a frequency distribution of age in discharge from a well or spring (see Chapter 3).

Another problem in obtaining representative samples from wells is caused by the introduction of tracers of interest into a formation during the well construction process. All drilling operations potentially introduce atmospheric components into an aquifer. Well development procedures may not adequately remove these components and, without special precautions in the drilling process, there is normally not any way to determine whether formation water contains trace contamination from drilling processes. When sampling water from wells with the intent of estimating the tracer based model age of 'old' groundwater from measurements of environmental tracer concentrations, as discussed in this book, additional samples should be collected for analysis of components that can be indicators of the introduction of contamination from drilling processes. Some useful indicators of contamination from young sources include tritium, ⁸⁵Kr and CFCs. Owing to their extremely low detection limit, CFCs can be ideal tracers of drilling contamination (Plummer et al. (2004) [49]). In some cases, the driller may have imported treated water from municipal supplies for use in drilling and well development. Chlorinated water from municipal supplies may contain chloroform, which can be detected at extremely low concentrations using purge and trap gas chromatography with an electron capture detector (Plummer et al. (2008) [62]). If new wells are constructed, it is recommended that gas tracers be introduced into the drilling mud, such as halon-1211, sulphur hexafluoride or CFCs. Air rotary drilling procedures are not recommended because they introduce atmospheric gases into an aquifer. If jetting is used in well development, which consists of injecting high pressure air into the casing, the air injection should be far enough above the open interval of the well so as not to inject air into the formation.

Springs probably are the least desirable sources for sampling 'old' groundwater because their discharge can represent a mixture of many waters of generally unknown origin (and age). Though the discharge of some springs may contain predominantly 'old' water, it is common to find fractions of tritium or CFCs, indicating a mixture. Not knowing the frequency distribution of age in a mixture or water source limits the usefulness of springs for groundwater dating purposes. Flowing wells that are open to a narrow interval of confined aquifers at a known depth are probably the most useful for

sampling 'old' groundwater, particularly if a well has been in use for many years. An example of this is provided by the sampling of the Nubian sandstone aquifer in Egypt (Patterson et al. (2005) [43]) for ⁸¹Kr (see Chapter 14). Production wells with turbine pumps or pumps with impellors may promote cavitation and gas phase separation, leading to uncertainty in tracer model age interpretation based on gaseous environmental tracers. One technique that has been used successfully is to place a relatively low capacity piston sampling pump at depth within or just above the well opening and a second higher capacity pump at a relatively shallow depth to maintain a fresh supply of formation water entering the well bore in the vicinity of the sampling pump.

2.4. DEVELOPMENT OF A NUMERICAL GROUNDWATER FLOW MODEL

There are a number of approaches hydrologists have taken in developing numerical models of groundwater flow, including relatively simple analytical solutions (see, for example, Genuchten and Alves (1982) [63]); lumped parameter models (see, for example, Małoszewski et al. (1983) [64]; Małoszewski and Zuber (1996) [65]); and finite difference and finite element models that can solve the partial differential equations of groundwater flow and solute transport in three dimensions (see, for example, Huyakorn and Pinder (1983) [66]; Konikow and Glynn (2005) [67]; Wang and Anderson (1982) [68]).

In many studies of groundwater systems, a numerical model is constructed that represents the hydrogeological framework. Although many simplifying assumptions are ultimately made when constructing such a model, it is usually best to combine all of the information and data gathered on a system in a fashion that forces interpretation to follow the principles and observations of solute chemistry and the physics of groundwater flow. A model can often yield results that are not conceptually intuitive, or various versions of the framework can be tested to eliminate certain hypotheses. Once constructed and calibrated to the hydrologist's satisfaction, a model can also be used to predict system behaviour when there are changes in outside stresses (increased pumping or reduced recharge, for example).

Models are constructed using computer software which solves the groundwater flow equation and allows users to assign hydraulic parameters to a hydrogeological framework (see Chapter 10). The framework can be recreated numerically to follow the degree of accuracy with which a system can be described in the field. Boundary conditions must also be assigned; these usually represent impermeable boundaries at the base of a model and the amount and distribution of land surface recharge. Equations are solved to provide a three dimensional distribution of hydraulic head (water levels) within a groundwater system. From these head maps, three dimensional velocity distributions can be calculated. The hydraulic parameters assigned can be adjusted to better fit simulated water levels in a system with those which are observed. From the velocity fields, the equation for advection and dispersion of a solute can be solved. Tracer model age can be substituted as a solute in the transport equation to provide the flow model age throughout the system (Goode (1996) [69]). Flowlines can be tracked throughout a model to determine source areas for water within various parts of a system. The simulated flow model ages and water sources can then be compared with observed tracer model ages and the model can be adjusted or calibrated, to better agree with observed data. As water level and environmental tracer data are independent, the use of both types of information creates the opportunity to obtain a model that more closely reflects the real system under study.

The MODFLOW code (Harbaugh et al. (2000) [70]; McDonald and Harbaugh (1988) [71]; Reilly (2001) [72]) is one of the most widely used computer codes for development of groundwater models of groundwater flow systems. Particle tracking calculations derived from the pathline programme, MODPATH (Pollock (1989) [73]), provide a means of simulating travel times in groundwater systems and of estimating the frequency distribution of age in discharge from wells. Inverse modelling capabilities, such as those obtained from the application of UCODE (Poeter and Hill (1998) [74]) to MODFLOW–MODPATH calculations, permit refinement of the groundwater model utilizing

environmental tracer data. MODFLOW and an integrated family of compatible codes is freely available from the USGS (http://water.usgs.gov/nrp/gwsoftware/modflow.html). Sanford (Chapter 10) discusses construction of groundwater models and applications of groundwater models in interpreting environmental tracer data.

Development of a numerical simulation model of groundwater flow in an aquifer system is an evolving process that utilizes the hydrogeological framework established for a groundwater system and can be refined as new hydrological, geological and environmental-tracer concentration data become available.

2.5. SUMMARY GUIDELINES FOR THE CHARACTERIZATION OF GROUNDWATER SYSTEMS AND THEIR FREQUENCY DISTRIBUTIONS OF AGE

Dating old water in a groundwater system requires a contextual understanding of the system, its geological structure, past and present hydrological conditions, and the geochemistry and geochemical evolution of its waters. Funding limitations, temporal constraints, aquifer heterogeneity and limits on describing that heterogeneity will determine the extent of contextual understanding that can be reached. There will always be a threshold beyond which uncertainties in model age and frequency distribution in age cannot be reduced. A water resources manager or scientist trying to describe a groundwater system and understand its frequency distribution of age has the responsibility to incorporate as much information as possible, from a wide variety of sources, into a conceptual framework.

In a first step, a methodical approach might seek to obtain the following information needed to characterize a groundwater system:

- (a) Characterize the geological framework, the geological structure and geological properties of the groundwater system:
 - (i) Determine the spatial distribution of strata or other geological units;
 - (ii) Determine the distribution of faults, fractures, folds and their geophysical properties;
 - (iii) Determine the porosity and mineralogy of the various geological units, and their boundaries (faults, soil and bedrock);
 - (iv) Determine the spatial extent of aquifer heterogeneity, locating areas in which variations in lithologic properties would affect the hydraulic properties of porosity, permeability, transmissivity and storage in aquifers;
 - (v) Construct visualizations (geological maps, geological cross-sections, three dimensional descriptions of stratigraphy and lithology) of the geological framework.
- (b) Characterize the hydrological framework, and the distribution of past and present hydrological conditions:
 - (i) Determine the distribution of water levels in wells, including their distribution in space and changes over time that reflect seasonal fluctuations and drawdowns from nearby extraction wells;
 - (ii) Determine the position of perennial and intermittent streams across the system, and long term average flows or baseflows in those streams;
 - (iii) Determine the distribution of areal recharge into the system or, more specifically, the distribution of precipitation, and develop an understanding of the evapotranspiration processes, surficial geology and geomorphology limiting or focusing groundwater infiltration;
 - (iv) Assess the spatial distribution of hydraulic permeabilities and storativities associated with various geological units in the system;
 - (v) Assess the potential for groundwater leakage into aquifers of interest and assess lateral flows into, or out of, the groundwater system.
- (c) Characterize the hydrochemical framework, geochemical patterns, environmental tracers, and geochemical evolution of the waters in time and space:

- (i) Determine the spatial (vertical and horizontal) distribution of, usually, non-reactive constituents (or of constituents unlikely to leave the water phase through precipitation, sorption or degassing), to infer directions of groundwater flow;
- (ii) Determine the spatial (vertical and horizontal) distribution of selected environmental tracers to delineate hydraulic properties of the groundwater flow system: recharge areas, discharge areas, groundwater flow paths, leakage and/or cross-formational flow, groundwater/surface water interaction, mixing and frequency distribution of age in discharge from wells and springs, and extent of evaporation (evapotranspiration);
- (iii) Determine the spatial (vertical and horizontal) distribution of concentrations of environmental tracers, stable isotopes and dissolved gases to delineate temporal aspects of the groundwater flow system: tracer model ages, travel times, recharge rates, recharge temperatures, excess air entrapment, climatic variations in the stable isotope composition of groundwater; Determine the spatial (vertical and horizontal) distribution of both reactive and non-reactive constituents to determine through inverse and forward geochemical modelling: the extent of various water–rock reactions, the extent of mixing and other hydrochemical processes affecting solute composition and geochemical adjustments of ¹⁴C model ages.
- (d) Develop a conceptual description of the groundwater flow system utilizing all geological, hydrological and geochemical data. Where is the aquifer recharged? Where does the aquifer discharge? Is leakage to/from other aquifers important? How do aquitards affect groundwater storage, flow and solute transport? How does flow vary with depth? What is the spatial distribution of tracer model ages? What are the relevant timescales of the groundwater flow system?
- (e) Develop numerical models of the groundwater flow system utilizing all of the geological, hydrological and geochemical data to test the conceptual description of the groundwater flow system, eliminate hypotheses and identify additional data requirements.

Following characterization of the geology, hydrology and geochemistry of the groundwater flow system and development of a conceptual description for groundwater flow in the system, numerical



FIG. 2.3. Building a conceptual understanding: the iteration between information gathering and modelling steps needed to characterize groundwater systems and their frequency distribution of age.

modelling is a logical follow-up that can augment understanding of the groundwater system, its frequency distribution of age and identify knowledge gaps. Numerical modelling may also be a source of the estimations and assessments needed to best characterize the groundwater system. Various types of numerical modelling may be used for this purpose: deterministic hydrological and geochemical modelling to simulate given processes; statistical modelling, data modelling or geospatial modelling to simulate spatial and/or temporal distributions of information; and stochastic modelling, stratigraphic basin modelling or other types of modelling that can combine deterministic process information with statistical distributions and statistical inferences, and help create reasonable realizations to characterize and describe a groundwater system.

Inverse geochemical modelling, or inverse hydrological modelling, will be an integral part in creating a conceptual framework for a groundwater system. Inverse modelling uses the available information and measurements and seeks to determine from that information the values and spatial distribution of geological, hydrological and geochemical properties of a system. Inverse hydrological modelling, for example, is often used to determine the hydraulic conductivity of various geological units. In contrast, inverse geochemical modelling seeks to explain the observed geochemical evolution of groundwater by determining the possible sets of reactions that could be responsible for that evolution. More complex inverse modelling can be conducted to assess the possible spatial distribution of given properties. In addition to providing a better understanding of a groundwater system and its geochemical and hydrological processes, inverse modelling can help determine the most important data collection needs for a system, for example, the critical data gaps that if filled could provide a substantially better understanding and conceptual framework.

Finally, predictive modelling or forward numerical modelling can be used to simulate the hydrological and geochemical processes operating in the context of the geological structure and boundary conditions of a groundwater system. Forward modelling uses the information and data gathered, and statistical modelling and inverse modelling can be conducted to further refine that information and determine key operative processes. Through sensitivity analyses, forward modelling will provide further information regarding possible critical data gaps that need to be addressed. Forward modelling can be used to explain and predict the frequency distribution of ages in a groundwater system, thereby contributing to a conceptual understanding of that system.

The cycle of: (i) information and data gathering, (ii) inverse modelling and (iii) predictive modelling can be repeated as time and financial resources allow, or until a water resources manager or scientist feels that a sufficient understanding of the groundwater system under review and its frequency distribution of ages has been reached (Fig. 2.3).

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Chapter 3

DEFINING GROUNDWATER AGE

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3.1. INTRODUCTION: WHY SHOULD GROUNDWATER BE DATED?

This book investigates applications of selected chemical and isotopic substances that can be used to recognize and interpret age information pertaining to 'old' groundwater (defined as water that was recharged on a timescale from approximately 1000 to more than 1 000 000 a). However, as discussed below, only estimates of the 'age' of water extracted from wells can be inferred. These groundwater age estimates are interpreted from measured concentrations of chemical and isotopic substances in the groundwater. Even then, there are many complicating factors, as discussed in this book. In spite of these limitations, much can be learned about the physics of groundwater flow and about the temporal aspects of groundwater systems from age interpretations of measured concentrations of environmental tracers in groundwater systems. This chapter puts the concept of 'age' into context, including its meaning and interpretation, and attempts to provide a unifying usage for the rest of the book.

3.2. WHAT DOES 'GROUNDWATER AGE' MEAN?

The concept of an 'idealized groundwater age' (Δt) implies the time elapsed between when water entered the saturated zone (in other words, when it entered the groundwater) and when the water was sampled at a specific location (x, y, z), presumably at a specific distance (Δs) downstream in
the groundwater system (Fig. 3.1(a)). The idea of radiometric 'dating' of groundwater was proposed as an extension of radiocarbon dating as applied to solid materials that contain carbon (such as wood, shells, charcoal, travertine) (Münnich (1957) [75]). Radiocarbon dating of solids usually applies to materials with a (presumably) well defined initiation time (e.g. the year a tree ring was laid down or a band of travertine precipitated). The difference between this initiation time and current time is the age of the sample. The atoms of carbon within the object are presumed to have remained fixed in place, with no new carbon added or old carbon lost, until the sample is analysed for its radiocarbon content. The object is then 'dated' by applying the radioactive decay equation using the current measured radiocarbon content and assumed initial radiocarbon content. The interval of time calculated in this fashion is called the '¹⁴C model age'. Provided that the basic assumptions (the initial radiocarbon content amount and the presumption that atoms of carbon have been neither gained nor lost) are correct, the '¹⁴C model age should equal the actual age. However, in many cases, the basic assumptions are not valid and the ¹⁴C model age of the solid may significantly differ from its 'true' age.

Groundwater literature has not always adequately distinguished the fundamental conceptual differences between the age of solid material and the age of groundwater that result from the mobile and mixable nature of water. As a result, much groundwater dating literature refers to an idealized concept of groundwater age (see above) which has a conceptual origin in what has been referred to as a 'hydraulic age' (Davis and Bentley (1982) [76]). From Darcy's law, it is known that given the permeability of a porous medium and the hydraulic gradient across it, one can calculate the specific discharge, and if the effective porosity is also known, the average interstitial velocity of the water can be calculated. By extrapolation, if the exact permeability distribution within an entire groundwater system and its distribution of hydraulic gradients are known, one can calculate velocity distributions and travel time from the water table to any given point within the system. The physics of groundwater movement, thus, dictates that any groundwater has travelled to its current location under a given set of physical conditions within a time frame determined by those conditions. This simple concept of groundwater movement has often been referred to as 'piston' flow. The difficulty of adequately characterizing the permeability distribution of subsurface materials has led to the measurement of environmental tracers as a means to estimate this 'idealized groundwater age'. However, because solutes and tracers disperse (mix) in groundwater and because piston flow neglects many aspects of this dispersion and mixing, the information hypothetically contained within an estimate of such an 'idealized groundwater age' would still need to be interpreted within a process context. Consider, for example, the flow system depicted in Fig. 3.1, where the direction s is along the flow path and $s \perp 1$ and $s \perp 2$ represent orthogonal directions to s. In Fig. 3.1, (a) equals an 'idealized groundwater age'; (Δt) would imply an elapsed time between the time water entered the saturated zone (when it entered the groundwater) and the time at which it was sampled at a specific position (x, y, z, t) at a specific distance (Δs) downstream in the groundwater basin. Figure 3.1(b) shows, however, that even for 1-D systems, groundwater (even at the most minute sampling scale) represents a collection of water molecules that have individually undergone transport and mixing reactions along multiple transport paths as a result of, for example, longitudinal dispersive processes, creating water samples that alter any 'idealized groundwater age' to a frequency distribution. Figure 3.1(c) shows that for more realistic 2-D and 3-D systems, additional transverse dispersion and finite sampling volumes may mix pathways of different lengths (possibly different recharge entryways) with the same velocity; or pathways with identical path lengths but different velocities. The net impact of 2-D and 3-D transverse dispersion is to create mixtures that affect the standard deviation about the mean of the frequency distribution of groundwater ages. Figure 3.1(d) indicates that transverse dispersion will also ultimately mix (very, very old) aquitard groundwater with (old) aquifer groundwater. As aquitard groundwater is characterized by a distinctly older groundwater age, it will induce a long asymmetric tail on the old side of the sample frequency distribution of groundwater ages. Figure 3.1(e) shows that the process of convergent mixing of different groundwater flows creates a mixture of component waters that is characterized by a bimodal probability distribution.



FIG. 3.1. The concept of groundwater dating represents levels of complexity. This is explained in the text below.

The following questions can be posed:

- What if the groundwater arrived at position (x, y, z) mostly by flow in the *s* direction, but was additionally under the influence of specific dispersive mixing parallel to the flow direction (D_s) as well as perpendicular to the flow direction $(D_{s\perp_1}, D_{s\perp_2})$? How does simple flow and simple mixing influence the interpretation of an 'idealized groundwater age'?
- What if the groundwater arrived at position (x, y, z) via flow from two (or more) similar but not identical entryway sources (Figs 3.1(b) and 3.2)?
- How does multicomponent mixing from distinctly different source regions under convergent flow impact the meaning and interpretation of an 'idealized groundwater age' (Fig. 3.1(e))?
- What if the groundwater system has not operated at a steady state, e.g. $v_s = f(t)$? How does (would) the observed 'idealized groundwater age' at position x, y, z vary as a function of time ($\Delta t = f(x, y, z, t)$? When hydraulic heads may have varied significantly over the timescale of groundwater age, what if the groundwater arrived at position (x, y, z) via flow in a direction that is not equivalent to the currently defined flow direction? Within the concept of this 'idealized groundwater age', a calculation of groundwater velocity in the *s* direction (v_s) is possible but not meaningful in this context.

These examples illustrate that even within the simple definition of an 'idealized groundwater age', its interpretation in terms of the processes that control 'idealized groundwater age' remains complex. Additionally, this illustrates an important concept:

— It is the net impact of all processes by which groundwater reaches the position (x, y, z, t) that determines groundwater age.

The corollary is:

— The understanding of groundwater age at a specific location (x, y, z, t) requires knowledge of all processes by which groundwater flows to that specific location.

These considerations demonstrate that a more physically based definition of groundwater age is needed.

3.3. GROUNDWATER AGE DISTRIBUTION

'Idealized groundwater age' has been defined above as the elapsed time since water entered the saturated zone. However, samples of groundwater are finite in volume and contain very large numbers of molecules. In a bulk fashion, groundwater moves in response to spatial gradients in fluid potential. In addition to this, inasmuch as water is a fluid and the relative positions of molecules are not fixed, those molecules move in random paths as well as through bulk flow (Fig. 3.2). These potential driven and entropy driven transport processes interact in a complex fashion to produce transport processes variously described as 'advection', 'diffusion', 'hydrodynamic dispersion' and so on (see Phillips and Castro (2003) [77] for a discussion of the influence of various transport processes on groundwater age tracers). One implication of groundwater transport is that the transport path of any individual molecule of water may (and almost certainly does) differ from the mean path obtained by averaging many molecules (Fig. 3.1). (It is acknowledged that water molecules have a specific identity of the order of picoseconds; for this discussion, this concept is ignored.) The result is that any finite sized sample of groundwater contains water molecules that have resided in the system for differing periods of time. This being the case, a groundwater sample at a specific location cannot be adequately characterized by any single value of 'age'; rather, it is characterized by a frequency distribution of ages (Fig. 3.1(b), etc.).

The concept of fluid age defined by a frequency distribution of ages was introduced by Danckwerts (1953) [78]. Since then, it has been widely applied in fluid dynamics, chemical engineering, atmospheric science, oceanography and hydrology (Hooper (2003) [79]; Loaiciga (2004) [80]; McGuire and McDonnell (2006) [81]). In the chemical engineering literature, the concept is generally referred to as



FIG. 3.2. A depiction of the role of dispersion in creating multipath routes from recharge to discharge in a 3-D groundwater system. Flow down the hydraulic head gradient produces decision points upon each encounter with the host grains of an aquifer. This probabilistic process creates dispersion in groundwater age arriving at position (Δx) downstream (Fig. 3.1(b)).

the 'residence time distribution function'. The residence time distribution is a mathematically rigorous and practically useful function (see references above for examples).

In this book, 'frequency distribution of age' will generally be used rather than 'residence-time distribution'. This is simply to avoid confusion since 'residence-time distribution' has been traditionally used in the chemical engineering literature to refer to distribution in the discharge of a system, whereas distribution in a finite sample from within the system is generally being referred to. The mathematics of these two cases differs. Małoszewski and Zuber (1982) [82] have provided mathematical formulations applicable to frequency distribution of age in groundwater systems and Małoszewski et al. (1983) [64] show examples of their application. McGuire and McDonnell (2006) [81] reviewed analogous mathematical approaches for the outputs of drainage basins. Goode (1996) [69] pioneered a flexible numerical approach to simulating age distributions in complex groundwater systems and Varni and Carrera (1998) [83] estimated the frequency distribution of age at a single point.

An extreme example of frequency distribution for groundwater age would arise from an extensive, hydraulically uniform aquifer with a high recharge rate that is spatially localized (e.g. at a small outcrop area of the formation). This system will be advection dominated because the spatially uniform aquifer minimizes the effects of dispersive mixing relative to advective transport and the high recharge rate produces small gradients of groundwater age with flow distance. In the absence of convergent flowlines, the distribution of groundwater ages within a small sample of groundwater in this case will have a prominent mode with a relatively narrow distribution around that mode. As the ratio of dispersion to advection increases, the frequency distribution of ages (spread around the mode) increases.

Although it is tempting to characterize the 'age' of a water sample by calculating some central tendency, unless the system is strongly advection dominated, this can yield quite misleading results. For example, imagine a small, rapidly recharged aquifer that is bounded by thick shale of extremely low permeability. The shale is still diffusing connate water (which was present when it was deposited in the Cretaceous) into the aquifer. If 99.9% of the water discharged from the aquifer was recharged 5 years before the samplig date, and 0.1% is water from the shale (with an age of, for example, 65 million years), the average age of the discharge is 65 ka. This number conveys no useful information about the system and is, in fact, quite misleading if taken at face value. However, when a system is

strongly advection dominated, an estimate of the mode of the frequency distribution of groundwater age can still provide useful information.

To summarize, the 'age' of a groundwater sample is a function of the frequency distribution of the elapsed time since each of the individual water molecules crossed the water table (Figs 3.1(b)–(d)). Unfortunately, this frequency distribution is difficult (to impossible) to determine for groundwater systems, even in a coarse sense. For estimating groundwater ages, one must rely on either inferences from the concentration of chemical or isotopic tracers measured in a water sample, or on calculations based on the physics of fluid mass transport. If the age estimate is obtained from a chemical tracer measurement, then a conceptual/mathematical model must be employed to convert tracer concentrations into an age; the single age value that results is called the 'tracer based model age'. For example, a groundwater age obtained using ¹⁴C-tracer data and the radioactive decay equation would be called a 'tracer based model age' or more specifically a '¹⁴C based model age'. This terminology reinforces the principle that calculated age is inseparable from the conceptual/mathematical model employed and the assumptions that model includes. It is, therefore, a useful measure of age only to the extent that the model corresponds to the characteristics of a system. Following a not uncommon practice, the expression will be simplified (in a specific case) to '¹⁴C model age' or (in a general case) 'tracer model age'.

In the majority of cases, the mathematical models and assumptions employed to interpret tracer data do not include mixing processes and yield single values of tracer model ages (errors cited are typically associated with tracer measurement error and do not contain information about the frequency distribution of age). These single values of tracer model ages may correspond to the mean ages of age distributions, but in most cases probably do not. Multiple tracers, combined with knowledge of the hydrogeology, can often aid in understanding (at least in a qualitative fashion) the relation between a single value of a tracer model age at a location and the frequency distribution of groundwater ages at that location.

3.3.1. Examples of groundwater age distribution

The examples given above illustrate possible forms of the frequency distribution of groundwater age in some simple hypothetical groundwater systems. Several examples of frequency distributions in more realistic systems have been provided by numerical modelling.

As mentioned above, if an age estimate is obtained from application of the physics of fluid mass transport, it is called the 'hydraulic age', which represents one type of 'flow model age'. In many cases, such calculations include only advective transport. In more complete models, additional processes may be included and in both cases a spatial distribution of 'hydraulic ages' may be calculated. An excellent example of this approach is provided by Goode (1996) [69], who illustrated the role of dispersion with a simple numerical groundwater flow model for a layered system (0–30 m, hydraulic conductivity is 10^{-5} m/s; 30-70 m, hydraulic conductivity is 10^{-6} m/s). Figure 3.3(a) shows the hydraulic head contours (0.2 m contours) of a simple flow system, which determine the streamlines shown in Fig. 3.3(b). For a case involving only advection and no dispersion (Fig. 3.3(c)), the groundwater age structure (10 a intervals) is noticeably different from a case of advection with dispersion (Fig. 3.3(d); $D_m = 1.16 \times 10^{-8}$ m²/s; $\alpha_L = 6$ m, $\alpha_T = 0.6$ m), especially at the boundary of the slow flow region in the zone of upflowing streamlines. The younger ages in the upflowing streamline region under the advection with dispersion case (Fig. 3.3(d)) are the result of dispersive mixing between slow moving streamlines and fast moving streamlines. The no-dispersion case (Fig. 3.3(c)) results in a more isolated pocket of flow and older groundwater ages.

Goode (1996) [69] and Bethke and Johnson (2008) [84] generalized these dispersion mixing and convergent mixing issues that impact the transport and mixing processes in groundwater flow systems and that influence groundwater age distribution. For 1-D groundwater flow without dispersion (piston flow, Fig. 3.1(a)), groundwater at a specific location should result in a single idealized groundwater



FIG. 3.3. The results of Goode (1996) [69] showing a direct simulation of groundwater ages within a very simple aquifer where the upper 30 m of the aquifer has a hydraulic conductivity of 10^{-5} m/s and the lower 70 m has 10^{-6} m/s. (a) shows the hydraulic head contours (0.2 m contours) and the velocity vectors; (b) shows the streamlines from recharge to discharge; (c) shows simulated age contours for the advection only condition (no dispersion) with a 10 a contour interval; (d) shows simulated age contours with dispersion (see Goode (1996) [69] for a complete description of the simulation; from Goode 1996 [69], reproduced with permission of the American Geophysical Union).

age. However, for groundwater flow with even 1-D longitudinal dispersion (in the same direction as the flow velocity), multiple microscale pathways produce a frequency distribution of groundwater ages. When 2-D and 3-D flow are included (Fig. 3.2), transverse dispersion may mix: (i) pathways of different lengths (and possibly different recharge entryways) with the same velocity; or (ii) pathways with identical path lengths but different velocities. The net impact of 2-D and 3-D transverse dispersion is to create mixtures and increase the width of groundwater age distribution (Fig. 3.1(c)).

For the longest timescale of flow, molecular diffusion may ultimately mix aquitard groundwater with the aquifer groundwater (Fig. 3.1(d)). As aquitard groundwater is usually characterized by distinctly older ages, the mixing of aquitard water with aquifer water (noting the Cretaceous shale example above) will induce a long asymmetric tail on the old side of age frequency distribution (Fig. 3.1(d)). The frequency distribution of groundwater age is, thus, dependent upon how much aquitard water was incorporated and the frequency distribution of ages within the aquitard groundwater.

In addition to simple dispersion induced mixing, groundwater flow paths may also converge to cause mixing; or an aquifer structure may induce mixing of groundwaters from layered aquifer systems. As illustrated in Fig. 3.1(e), the process of convergent mixing of different groundwater flows creates a mixture of component waters that is characterized by a bimodal age distribution. Samples collected from pumping wells or springs are susceptible to even further turbulent mixing in the discharge conduit where the sample is collected.

3.4. CHARACTERISTICS OF IDEAL TRACERS

An ideal groundwater age tracer should exactly replicate the transport and mixing of the groundwater with which it flows. As such, an ideal tracer: (i) should not be subject to chemical retardation with respect to the water flow; (ii) should undergo mechanical dispersion identical to that of the water molecules (and, thus, duplicate the frequency distribution of groundwater age); and (iii) should undergo molecular diffusion identical to that of the water molecules. An ideal groundwater tracer suitable for dating must then also change its concentration as a known and defined function of time from a defined initial condition to the location at which it can be sampled. The initial conditions for a tracer model age should be obtainable and should be established in the same location where the idealized groundwater age is zero. All of these attributes should result in the tracer, at the sampling location, having an age distribution that follows from the groundwater age distribution (e.g. for a radioactive tracer, this would correspond to the groundwater age distribution multiplied by the appropriate amount of decay for each age). In this context, the available choices of geochemical tracers suitable to dating needs are narrowed considerably; they are characterized by simple solubility controls, limited reactivity and known radioactive reaction rates for either ingrowth or decay (or in the case of stable tracers such as CFCs (IAEA (2006) [85]), known variability in the initial condition, simple geochemistry and 'no' loss terms). With a known initial condition and a known reaction (such as radioactive decay or known production), the measured concentration of a tracer in a groundwater sample at location x, y, z, t can be converted into a tracer model age through a defined mathematical formula with specific assumptions.

However, the tracer model age is subject to interpretation (and potential complication) as a result of both dispersion controlled mixing and convergence controlled mixing. The interpretation of tracer



FIG. 3.4. The groundwater age of a water sample can be represented by some central measure of frequency distribution of ages (Figs 3.1(b) and (c)).

model age is functionally dependent upon whether the reaction term is linear, concave or convex versus distance/time and the timescale of the tracer.

For the case of a linearly changing (under ideal conditions, possibly ⁴He) tracer concentration with time (see Fig. 3.4(a)), a mixture of young and old waters will create a mixture whose combined frequency distribution of groundwater ages accurately reflects the mixing and relative weighting of the old and the young water. However, for a tracer with exponential decay (such as ¹⁴C or ³⁶Cl), the mixing of old and a young groundwater will create a tracer mixture that is interpreted as younger than the weighted mean of the separate tracer ages of young and old water would imply (see Fig. 3.4(b)). In an ideal world, the tracer model age (determined by some geochemical method) would be a true reflection of the frequency distribution of groundwater age. Figure 3.4(a) shows that when a tracer increases (or decreases) linearly with time (e.g. possibly ⁴He or a tracer the input of which is linearly changing as a function of time), a mixture of groundwaters with different ages would produce a mixed water whose tracer model age would be in agreement with the weighted mix of groundwater ages. However, Fig. 3.4(b) shows that for a tracer whose variability with time is non-linear (typically exponential with time: ¹⁴C, ³⁶Cl, etc.), the effect of mixing (in this specific case) groundwaters with different ages would produce a tracer model age that does not agree with the weighted mix of groundwater ages. Without independent knowledge of what was mixed and in what proportions, it is not possible to interpret a tracer model age unequivocally as a measure of the central tendency of the frequency distribution of groundwater age.

Dispersion controlled mixing for tracers with concave functions such as radioactive decay will, therefore, always create conditions under which the tracer model age is an underestimate of the mean groundwater age; the degree of underestimation being a function of the degree of mixing and the decay constant. For convergence controlled mixing, the component end members are likely more widely disparate in their groundwater age distributions and the impact of convergent mixing on the tracer will result in a greater difference between the mean (or mode) of groundwater age distribution and the tracer model age, again with the tracer model age being younger than the correctly interpreted mixture of component end member ages. Tracer reaction rates and mixing end members must, therefore, be considered in the interpretation of tracer model ages. For cases in which the mean of the age distribution is not equal to the mode for the age distribution (e.g. Fig. 3.1(d)), or where the age distribution is bimodal (Fig. 3.1(e)), the interpretation of tracer model age and its relation to the mean or mode of age distribution becomes more complex.

3.5. ADDITIONAL LIMITATIONS ON TRACER MODEL AGES

Under favourable circumstances, groundwater age can be characterized by some central measure (mean, median, mode) of the frequency distribution of groundwater ages within a groundwater sample (e.g. Fig. 3.1(b)–(e)). However, because a groundwater sample has been aggregated (naturally or by some bias in the sampling protocol) via distinct and separate processes, interpreting some central tendency of distribution requires information on the nature of the distribution function. Such information is difficult to obtain for real world (as opposed to simulated, mathematically modelled) groundwater systems, and this greatly limits the ability to interpret single values of tracer model ages. To some extent, one can obtain information on the nature of age distribution via methods such as classical input–output analysis (Kirchner et al. (2000) [86]; McGuire and McDonnell [81] (2006); McGuire et al. (2005) [87]), interpretation of multiple tracers, especially radionuclides with a wide range of half-lives (Castro et al. (2000) [88]), or numerical simulation of the system (Castro and Goblet (2003) [89]; Park et al. (2002) [90]; Weissmann et al. (2002) [91]) and use these to help interpret individual tracer model ages, but even so the interpretations will have significant uncertainty associated with them.

It must be appreciated in groundwater dating that a single tracer model age is in fact a calculation that has a specific location/time associated with it (x, y, z, t), a specific initial condition and a specific Δs and Δt that delimit interpretation constraints. This means that only bulk properties between two flow

connected sampling points can be quantified unless additional information is available from well tests, additional sampling, other tracers, other dating methods, etc. This implies that multiple measures along a flow path will provide more and better information if interpreted together rather than individually. It has been noted (Bethke and Johnson (2008) [84]) that plots of tracer model age versus distance yield slopes in units of inverse velocity. Such plots can be used to support the existence of a continuous flowline as well as discontinuities in flow velocity.

Even when the conditions for appropriate application of a geochemical tracer for the calculation of a tracer model age can be confirmed and appropriate samples can be obtained, the calculation of a tracer model age must still be interpreted with caution. A tracer model age is an interpretation and an approximation that acknowledges all of the assumptions, idealizations and limitations of a tracer, as well as comparability of a tracer to the processes that determine groundwater age. Due to aquifer heterogeneity, dispersive mixing, and other physical and chemical processes, macroscale groundwater age distribution cannot be defined by tracer model age. Still, tracer model ages provide information that helps constrain age distribution and the generalities of flow in groundwater systems.

3.6. TRACERS IN THIS BOOK

The tracers available for application and interpretation in terms of tracer model ages are limited for timescales greater than 1000 a. Tracer model analysis of ⁴He, ¹⁴C, ³⁶Cl, ⁸¹Kr and ²³⁴U/²³⁸U provides valuable information and is discussed in the chapters that follow. However, the value of a tracer model age increases when two or more methodologies can be compared and contrasted in order to understand the relation between generally simplified assumptions inherent in tracer models and a more complex real system (see Chapter 9).

The geochemical groundwater tracers discussed in this book (⁴He, ³⁶Cl, ¹⁴C, ⁸¹Kr, ²³⁴U/²³⁸U) have been used to calculate tracer model ages in multiple groundwater systems with sufficient cross checks to ensure at least a minimal level of confidence in the results. In the following chapters, tracer specific processes will be defined and discussed which contribute to the calculation of tracer model ages, as well as how various processes affect the interpretation of these tracer model ages. The 'tracer model age' will be referred to as a generality and in specific cases will refer to, for example, the '¹⁴C model age' or the '⁴He model age' to differentiate which specific tracer has been used and what specific model has been used to calculate the tracer model age.

The case studies discussed in the following chapters reinforce the principle that multiple sampling points with multiple tracers including temperature, water chemistry, hydraulic head, stable isotopes and well borehole tests will provide information that is generally necessary for adequately characterizing groundwater basins. These can then be interpreted with the aid of detailed mathematical reaction and transport models ('flow model ages'). Additional constraints can often be imposed on the interpretation by optimizing hydraulic models to best simulate tracer transport data (Berger (2008) [92]). Yet, even for the best tracers and the simplest groundwater systems, the system of equations describing reaction and transport in a groundwater system will be under-constrained. In order to solve equations that describe flow in a groundwater basin, assumptions and simplifications must be made with regard to basin structure, the heterogeneity of basin properties and the evolution of a basin as a steady state or unsteady state flow system subject to temporally controlled uplift and erosion. Given this complexity, simple physics based flow models (see Castro et al. (2000) [88]; Torgersen and Ivey (1985) [93]) that include transport and mixing of groundwater as well as the source and sink functions that control tracer distribution (Bethke and Johnson (2008) [84]; Bethke et al. (2000) [94]; Bethke et al. (1999) [95]; Castro and Goblet (2003) [89]; Castro et al. (1998) [96]; Castro et al. (1998) [97]; Zhao et al. (1998) [98]) are useful in evaluating the controls on groundwater movement and flow times.

Flow in groundwater systems is typically dependent on a complex spatial distribution of hydraulic properties. Data to constrain this distribution are generally sparse. The spatial distribution of hydraulic head is relatively insensitive to the distribution of hydraulic properties unless materials of differing

properties are arrayed in continuous layers of strongly contrasting values (Gomez-Hernandez and Gorelick (1989) [99]). It is within this context that estimates of groundwater age via tracer model ages can provide significant constraints on the structure of a system. However, even with this additional information, groundwater systems are always under-constrained with regard to data requirements and the resulting models are always non-unique. To some extent, this limitation can be overcome by employing geostatistically based multiple conditional simulations, but even this computationally intensive approach provides only an indication of the possible range of behaviour of a system. It benefits the conclusions of a study when groundwater scientists maintain an appropriate sense of complexity that exists in the natural systems they study.

APPENDIX TO CHAPTER 3

AGE TERMINOLOGY

- old groundwater. Water that was recharged on a timescale of greater than 1000 to several million years; a practical timescale defined by the tracers discussed in this book.
- **idealized groundwater age.** The elapsed time between the time water entered the saturated zone (when it entered the groundwater) and the time the same water was sampled in a specific position downstream in the groundwater system.
- **frequency distribution of age.** The distribution of all idealized groundwater ages of all individual water molecules in a groundwater sample
- **tracer based model age or tracer model age.** The single age value that is obtained from the application of a conceptual/mathematical model to a measurement of the concentration of a chemical tracer in a groundwater sample; in the case of a specific tracer, for example, ¹⁴C model age
- flow model age. A hydraulic age calculated within a flow model
- **hydraulic age.** The single valued age estimate obtained from the application of physics of fluid mass transport in the groundwater system
- **mean age or average age.** The mean age is the average age of all individual water molecules in a system or sample. In terms of the mass age concept, mean age is the sum of the product of fraction of water and age of that fraction for all water fractions/ages recognized in a system

Chapter 4

RADIOCARBON DATING IN GROUNDWATER SYSTEMS

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"Radiocarbon dating of groundwater, which started with the original work of the Heidelberg Radiocarbon Laboratory back in the late 1950s, is certainly one of the most — if not the most — complicated and often questionable application of radiocarbon dating. The reason for this is to be found in the aqueous geochemistry of carbon in the unsaturated and saturated zones. Part of the carbon and radiocarbon content of dissolved carbon in groundwater is of inorganic and part is of organic origin." (Mook (1992) [100]).

4.1. INTRODUCTION

The radioactive isotope of carbon, radiocarbon (14 C), was first produced artificially in 1940 by Martin Kamen and Sam Ruben, who bombarded graphite in a cyclotron at the Radiation Laboratory at Berkeley, CA, in an attempt to produce a radioactive isotope of carbon that could be used as a tracer in biological systems (Kamen (1963) [101]; Ruben and Kamen (1941) [102]). Carbon-14 of cosmogenic origin was discovered in atmospheric CO₂ in 1946 by Willard F. Libby, who determined a half-life of 5568 a. Libby and his co-workers (Anderson et al. (1947) [103]; Libby et al. (1949) [104]) developed radiocarbon dating of organic carbon of biological origin, which revolutionized research in a number of fields, including archaeology and quaternary geology/climatology, by establishing ages and chronologies of events that have occurred over the past approximately 45 ka.

Cosmogenic ¹⁴C is produced in the upper atmosphere by the nuclear reaction (Mackay (1961) [105]; Mak et al. (1999) [106]):

$${}^{14}\mathrm{N} + \mathrm{n} \to {}^{14}\mathrm{C} + \mathrm{p} \tag{4.1}$$

where ¹⁴C oxidizes to ¹⁴CO and then ¹⁴CO₂, and mixes with the atmosphere. ¹⁴CO₂ is absorbed by plants during photosynthesis and becomes incorporated into the Earth's biological and hydrological cycles. The atmospheric mixing ratio of ¹⁴CO₂ is balanced by the rate of cosmogenic production, uptake by the various carbon reservoirs on Earth (atmosphere, oceans, marine organisms, plants) and radioactive decay. Carbon-14 decays according to:

$${}^{14}\mathrm{C} \to {}^{14}\mathrm{N} + \beta^- \tag{4.2}$$

with a generally accepted (consensus) half-life of 5730 ± 40 a (Godwin (1962) [107]). Chiu et al. (2007) [108] review the various measurements of ¹⁴C half-life and suggest that the modern half-life may be underestimated by approximately 300 a.

The conventional radiocarbon age, *t*, in years is, by definition:

$$t = \tau \ln \frac{A_o}{A} \tag{4.3}$$

where

 τ is the Libby mean-life (5568 a/ln 2, where 5568 is the Libby half-life);

 A_o is the initial ¹⁴C specific activity (in Bq/kg or mBq/g; 1 Bq = 1 disintegration per second);

A is the measured ¹⁴C specific activity.

By international convention, specific activities are compared to a standard activity, A_{ox} , where $A_{\rm ox} = 0.95$ times the specific activity of NBS oxalic acid (0.95 × 13.56 disintegrations per minute per gram of carbon (dpm/g C) in the year 1950 A.D.). The initial ¹⁴C specific activity, A_o, and the measured ¹⁴C specific activity of a sample, A, can be expressed as a percentage of this standard activity in per cent modern carbon (pmc) where pmc = $(A/A_{ox}) \times 100$ (Mook (1980) [109]). The modern, pre-nucleardetonation atmospheric ¹⁴C content is, by convention, 100 pmc, corresponding to 13.56 dpm/g C in the year 1950 A.D. (Stuiver and Polach (1977) [110]). Conventional radiocarbon ages continue to be reported based on the Libby half-life, so as not to conflict with earlier studies, and ¹⁴C model ages are then defined in 'radiocarbon years'. A further complication in radiocarbon dating was the discovery that the amount of ¹⁴CO₂ in the atmosphere has not been constant over time. Past variations in the solar wind and the geomagnetic fields of the sun and Earth have caused variations in the flux of cosmic rays reaching the Earth, resulting in variations in the atmospheric concentration of ¹⁴CO₂ (Kalin (1999) [111]). It is likely that the atmospheric ¹⁴C content has also changed in response to changes in the residence time of the major global reservoirs (terrestrial, biosphere and ocean). The discovery of past variations in the amount of atmospheric ¹⁴C has led to another major field of radiocarbon investigations in determining and refining radiocarbon calibration scales to convert radiocarbon years to calendar years. For example, the last glacial maximum (LGM) occurred about 18 ka radiocarbon years ago, which corresponds to about 21 ka calendar years (Bard et al. (1990) [112]). However, recent analysis of the Barbados sea level record places the LGM at about 26 ka calendar years (Peltier and Fairbanks (2006) [113]).

Münnich was the first to extend radiocarbon dating to dissolved inorganic carbon (DIC) in groundwater (Münnich (1957) [75]; Münnich (1968) [114]). Over the past 50 years, an extensive literature of investigations and applications of radiocarbon in hydrological systems has followed. Many advances in collection and analysis of ¹⁴C have also followed and now ¹⁴C content is almost routinely determined on carbon samples as small as 1 mg by using accelerator mass spectrometry (AMS). Many of the original studies were reported in proceedings of symposia sponsored by the Isotope Hydrology Section of the IAEA. A number of reviews summarize some of the advances, principles and problems in radiocarbon dating of DIC in groundwater (Fontes (1983) [115]; Fontes and Garnier (1979) [116]; Fontes (1992) [117]; Geyh (2005) [118]; Kalin (2000) [111]; Mook (1980) [109]; Mook (2005) [119]). Numerous studies have applied radiocarbon dating to establish chronologies of the (approximately) 0–40 ka timescale in hydrological systems, to estimate modern and palaeorecharge rates to aquifers, to recognize non-renewable palaeowaters, to extract palaeoclimatic information from the groundwater archive, to calibrate groundwater flow models, and to investigate the availability and sustainability of groundwater resources in areas of rapid population growth. It is beyond the scope of this chapter to review these many studies.

In spite of the many advances in collection, analysis and application of radiocarbon in the hydrological sciences, interpretation of the radiocarbon model age of dissolved carbon in groundwater is still limited by many uncertainties in determining the initial ¹⁴C content of dissolved carbon in recharge areas to aquifers and in accounting for the many chemical and physical processes that alter the ¹⁴C content along flow paths in aquifers. The purpose here is to summarize the current state of methods used to interpret ¹⁴C model age from measurements of ¹⁴C in DIC and dissolved organic carbon (DOC) in groundwater.

Historically, hydrologists and geochemists have resorted to simplifying assumptions regarding geochemical adjustments of radiocarbon in groundwater systems, often without sufficient data to know whether additional processes are needed to accurately date the DIC in groundwater systems. As many

geochemical interactions and hydrological processes in groundwater systems can affect radiocarbon content in aquifers, modern approaches to radiocarbon dating in groundwater systems are often treated within the context of geochemical modelling; that is, the study of geochemical evolution of water–rock systems. Relatively large uncertainties in the ¹⁴C model age of DIC in groundwater systems remain, however, and as a result, although radiocarbon calibration is commonly applied to dating of biological carbon, such calibration is rarely warranted in radiocarbon dating of DIC in groundwater due to the many unknown geochemical and physical processes affecting the ¹⁴C content of DIC.

Bethke and Johnson (2008) [84] recently distinguished between (i) sample age calculated according to a geochemical age-dating technique, as commonly applied in 'traditional' radiocarbon adjustment models; and (ii) piston flow age, the time required to traverse a flowline from the recharge point to a location in the subsurface. Furthermore, they recognized that because of hydrodynamic processes occurring in aquifers, a groundwater sample is a collection of water molecules, each of which has its own age. Similarly, Fontes (1983) [115] wrote:

"Owing to dispersion, the 'age' of a groundwater sample corresponds generally to a time distribution of many elementary flows. Thus, except in the theoretical case of a pure piston flow system, or of stationary waters entrapped in a geological formation, the concept of groundwater age has little significance."

These age concepts are discussed in Chapter 3 in the context of this book.

Although hydrodynamic processes can cause difficulties in the interpretation of tracer model age, many hydrogeological settings have been investigated where radiocarbon dating has provided useful information on flow and recharge rates, and ¹⁴C model ages have been partially corroborated by concordance with other isotopic and environmental tracers on the 0–40 ka timescale. The interpretion of the ¹⁴C model age is provided below, where the model age is the ¹⁴C piston flow age calculated by a 'traditional' geochemical adjustment method that is applied to DIC. Then, some of the more advanced geochemical modelling techniques that can help refine a ¹⁴C model age and quantify hydrodynamic mixing on the basis of solution chemistry and isotopic compositions will be discussed. A discussion of advances in radiocarbon dating of DOC follows. Finally, the complexities of assessing the effects of diffusive processes and leakage from or through confining units will be examined.

This chapter reviews some of the past radiocarbon adjustment models, the conditions under which they apply, and summarizes the geochemical modelling approach to radiocarbon dating as implemented in the inverse geochemical modelling code NETPATH (Plummer et al. (1994) [120]) which applies radiocarbon dating to the total dissolved carbon (TDC) system (DIC + DOC + CH₄). In an effort not to obscure the presentation with too many equations and details, these have been placed in the Appendix to Chapter 4, along with some example calculations. Units used in reporting radiocarbon measurements and conventional radiocarbon age are defined in the Appendix to Chapter 4. Equations describing isotopic fractionation in the carbonate system are summarized in the Appendix to Chapter 4 also provides some guidance on radiocarbon calibration to calendar years. Details pertaining to field sampling are provided as well as reference to available software used in radiocarbon dating of DIC in groundwater. Finally, the Appendix to Chapter 4 supplies a reference to selected AMS facilities providing radiocarbon determinations.

4.2. INTERPRETATION OF RADIOCARBON AGE OF DISSOLVED INORGANIC CARBON IN GROUNDWATER

Carbon-14 of cosmogenic origin is incorporated in groundwater during recharge by interaction of infiltrating water with soil CO₂ from plant root respiration and microbial degradation of soil organic matter (see, for example, Kalin (1999) [111]). Following recharge, DIC becomes isolated

from the modern ¹⁴C plant–soil gas–air reservoir and decays with time. Many physical and chemical processes can affect the ¹⁴C content of DIC in groundwater, beyond that of radioactive decay, and must be considered to interpret radiocarbon model ages and their uncertainties. The most important considerations in radiocarbon dating of DIC in groundwater can be grouped under four general topics:

- (a) Determination of the initial ¹⁴C content, A_0 , of DIC in groundwater recharge, at the point where infiltrating water is isolated from the unsaturated zone ¹⁴C reservoir;
- (b) Determination of the extent of geochemical reactions that occur within the aquifer following isolation from the unsaturated zone and the effect of geochemical reactions on ¹⁴C content;
- (c) Evaluation of the extent to which physical processes alter the ¹⁴C content (such as mixing of old and young water in samples pumped from wells; hydrodynamic dispersion along hydrological flow paths; matrix diffusion and/or diffusive exchange with confining layers, leakage from other aquifers or surficial waters, in situ production);
- (d) When warranted, correction for historical variations in atmospheric ¹⁴C content, through application of radiocarbon calibration scales.

These four topics are discussed below.

4.2.1. Determination of initial ¹⁴C in recharge water, A_0

In the unsaturated zone, CO_2 partial pressure is typically substantially higher than that in the atmosphere (about 10^{-3.5}) as a result of biological activity, soil moisture and, often, higher temperature (Brook et al. (1983) [121]). As infiltrating water moves through the unsaturated zone, the CO_2 in infiltrating water is augmented by soil zone CO_2 . The dissolved CO_2 reacts with carbonate and silicate minerals in the soil and sediment of the recharge area, resulting in increased concentrations of dissolved carbon (DIC and DOC) in the infiltrating water.

The term A_0 refers to the initial ¹⁴C content of DIC in groundwater that occurs following recharge and isolation of the water from the modern ¹⁴C reservoir of unsaturated zone CO₂. A_0 must be known or estimated to date the ¹⁴C of dissolved carbon in groundwater in hydrological systems. In the following, the term 'pmc' is used to express the ¹⁴C content as a per cent of the modern standard (see above).

4.2.1.1. Estimation of A_o from measurements in recharge areas

Ideally, measurements of the radiocarbon content of DIC and DOC in groundwater from the recharge areas of aquifers can be used to define A_0 , but this approach has two complications. First, many of the waters in recharge areas of aquifers today contain tritium and/or CFCs, which are indications of potential contamination of ¹⁴C from post-nuclear detonation (post-1950s) water. Water from the post-1950s bomb era has ¹⁴C amounts that are greater than the historic values that existed in pre-1950s recharge areas, and, if these observed values from recharge areas are used in dating, radiocarbon model ages will be biased old. Waters from recharge areas of aquifers can also be mixtures of pre- and post-bomb era waters, again leading to an old bias in the ¹⁴C model age. The issue here is not so much that of contamination, but rather of insufficient knowledge of the contamination to adequately calculate the effective A_0 value that would incorporate only natural, pre-bomb, ¹⁴C dilution processes, and would have applied at the time of recharge of the old groundwater under investigation.

Secondly, even if pre-bomb waters can be identified in the recharge area today, consideration needs to be given to the palaeoclimatic conditions corresponding to the time an old, geochemically evolved water sample was recharged. As shown below using some of the well known adjustment models, modelled values of A_0 can be sensitive to the δ^{13} C of soil gas CO₂. Further, the δ^{13} C of soil gas CO₂ can change significantly over time in recharge areas in response to climatic variations that cause changes in the relative proportions of plants utilizing the C₃ and C₄ photosynthetic pathways. In addition, the extent to which recharge waters evolve in isotopic equilibrium with soil gas (open system

evolution) or react with carbonates following recharge (closed system evolution) (Clark and Fritz (1997) [52]; Deines et al. (1974) [122]) can lead to uncertainties in ¹⁴C model age of old groundwater as much as a full ¹⁴C half-life. Isotopic fractionation in open and closed systems is discussed in the Appendix to Chapter 4. Even if it can be determined whether recharge waters presently evolve under open or closed system conditions, it is not known whether modern conditions prevailed when the old groundwater was recharged.

Another assumption that is commonly made, and which is applicable in most but perhaps not all cases, is that the 'recharge area' of old groundwater was the same as that observed today. In some cases, differences in regional climate may have caused differences in the relative amounts of recharge from different areas over time. Furthermore, modern water resource management activities can also affect the distribution of modern recharge. Changes in aridity and other climatic factors in a recharge area over the timescale of an aquifer can cause changes in the distribution of C₄ to C₃ in plants, which can result in changes in the value of δ^{13} C of soil gas CO₂. Some of the models used to estimate values of A_0 in recharge areas (see below) are quite sensitive to the value of δ^{13} C of soil gas CO₂. Finally, although geological and tectonic processes often have not had enough time to significantly alter the landscape of groundwater recharge over the ¹⁴C timescale, exceptions do occur.

Still, if a set of groundwater samples can be obtained from the modern recharge area, or along a flow path, examination of the ¹⁴C content of DIC in relation to tritium (Geyh (2005) [118]; Kalin (1999) [111]; Verhagen (1984) [123]; Verhagen et al. (1974) [124]) or other anthropogenic environmental tracers, such as tritium and CFCs (IAEA (2006) [85]; Plummer et al. (2004) [49]; Plummer et al. (2004) [50]; Plummer and Busenberg (2000) [125]), or in relation to distance of flow in aquifers (Geyh (2000) [126]; Vogel (1970) [127]) can be used to estimate the modern, pre-bomb content of ¹⁴C.

Figure 4.1 compares ¹⁴C specific activities of DIC, expressed as pmc, as a function of CFC-12 and ³H concentrations for waters from recharge areas of the Middle Rio Grande Basin aquifer system of New Mexico, USA (Plummer et al. (2004) [50]). The data suggest that the pre-nuclear detonation content of ¹⁴C of DIC in recharge areas to the groundwater system was near 100 pmc. Carbon-14 values >100 pmc have CFC-12 piston flow ages from the mid-1960s for groundwater that infiltrated



FIG. 4.1. Carbon-14 content, expressed as pmc (per cent of the modern standard) of DIC in groundwater from the Middle Rio Grande Basin, NM, USA, as a function of (a) CFC-12 concentration (see graph in (b) for explanation of symbols) and (b) tritium.



FIG. 4.2. Concentrations of ¹⁴C and CFC-12 measured in groundwater from the Middle Rio Grande Basin, NM, USA (red triangles), in relation to concentrations expected for water containing modern DIC, not diluted with old DIC. The blue line represents the atmospheric input of radiocarbon (Levin and Kromer (1997) [128]; Levin et al. (1994) [129]) and CFC-12 (http://water.usgs.gov/lab) (unmixed, piston flow). The light dashed lines represent hypothetical mixing of old water with water from 1969, 1974, 1985 and 1997 (modified from Plummer et al. (2004) [49]).

from the Rio Grande (central zone) and post-1995 ages for waters which infiltrated along the eastern mountain front; the latter comprised mixtures or samples containing a fraction of non-atmospheric CFC-12 (Fig. 4.1(a)). The highest ¹⁴C value in samples low in tritium and CFC-12 is near 100 pmc (Figs 4.1(a) and (b)), consistent with open system evolution from this semi-arid region of the southwest USA (modified from Plummer et al. (2004) [49]).

Waters in the northern mountain front, north-western and eastern mountain front hydrochemical zones were recharged along mountain fronts that border the basin to the north and east. Water from the west–central zone is thought to have recharged in high elevation areas north of the basin (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]). Water from the central zone originated as seepage from the Rio Grande, which flows north to south through the centre of the basin. Many of the groundwater samples have low ¹⁴C values and are likely tens of thousands of years old, especially those of the central zone (Fig. 4.1). A_0 can be inferred, however, as the maximum ¹⁴C value in samples with the lowest CFC-12 and/or lowest ³H content, as these samples were likely the youngest samples that recharged prior to the bomb era (pre-1950s). The maximum pmc value of ¹⁴C in groundwater low in CFC-12 (<20 pg/kg) and low in ³H (<0.5 TU) is near 100 pmc in the Middle Rio Grande Basin samples, and probably within the range of 95–102 pmc (Fig. 4.1), suggesting a predominantly open system evolution (Appendix to Chapter 4).

During the past approximately 20 years, the ¹⁴C content of atmospheric CO₂ has averaged 120 ± 10 pmc in the northern hemisphere (Fig. 4.2). Most of the observed ¹⁴C values in samples that contain ³H or CFCs are in the range of 95–120 pmc, which is again consistent with the assumption of open system evolution (Fig. 4.1). As no samples with ¹⁴C values higher than 123 pmc were observed, it is assumed that waters recharged during the mid-1960s and early 1970s (Fig. 4.2) were not sampled in recharge areas or, if present, were mixed and diluted with fractions of older, pre-bomb water. The distribution of ¹⁴C values (Fig. 4.1) in both mountain front areas and in recent seepage from the Rio Grande suggests that A_0 is likely in the range of 95–102 pmc. In the Middle Rio Grande Basin study

(Plummer et al. (2004) [49]; Plummer et al. (2004) [50]), a value of A_0 equal to 100 pmc was assumed for all waters. The unadjusted ¹⁴C model ages would decrease by 400 a if a value of A_0 of 95 pmc were used instead of 100 pmc, and increase by 150 a if a value of A_0 of 102 pmc were used instead of 100 pmc. These ¹⁴C model age differences are quite minor in comparison to uncertainties in age due to geochemical reactions.

4.2.1.2. Estimation of A_o using 'traditional' geochemical adjustment models

If geochemical reactions occur that affect the DIC, these reactions usually result in a lowering of the ¹⁴C content of DIC, independent of the radioactive decay of ¹⁴C. Applied to the initial ¹⁴C value, the carbonate reactions will lower the adjusted value of A_0 (termed A_{nd} , where the subscript refers to 'no decay'), resulting in adjusted ¹⁴C model ages that are younger than the unadjusted (or conventional) ¹⁴C model age. It is, therefore, important to recognize and quantify the effects of any geochemical reactions occurring that can affect the ¹⁴C content of DIC.

Traditionally, hydrologists have applied models that account for some of the more important carbonate reactions that occur in groundwater systems (Eichinger (1983) [130]; Evans et al. (1979) [131]; Fontes (1983) [115]; Fontes and Garnier (1979) [116]; Fontes (1992) [117]; Ingerson and Pearson Jr. (1964) [132]; Kalin (1999) [111]; Mook (1972) [133]; Tamers (1975) [134]) to the DIC of water from a single well to estimate adjusted ¹⁴C model ages (Fig. 4.3). Each traditional adjustment model is based on a set of assumptions regarding chemical and isotopic fractionation reactions that may affect the DIC ¹⁴C content of a water sample, without radioactive decay of the ¹⁴C. The models produce an initial ¹⁴C value, A_0 , that has been adjusted for geochemical reactions without accounting for radioactive decay (also denoted A_{nd}). An effort is made in this publication to retain original notation; therefore, there is some redundancy in terminology. In the traditional approach to radiocarbon dating, values A_0 or A_{nd} , are compared to the measured ¹⁴C value in the decay equation to estimate ¹⁴C model age (Fig. 4.3).

This approach is best suited for geochemical systems undergoing relatively simple water–rock reactions, such as usually occurs in shallow recharge areas, but, depending on the choice of model, can be applied to radiocarbon dating of DIC in groundwater systems undergoing carbonate mineral dissolution, gypsum dissolution, Ca/Na ion exchange, CO_2 gas dissolution and isotope exchange



FIG. 4.3. Conceptualization of the application of 'traditional' adjustment models in radiocarbon dating of DIC in groundwater. The models, such as those of Tamers, Fontes and Garnier, Mook, Ingerson and Pearson, Eichinger and others, are applied to a single water analysis in the system (Plummer and Sprinkle (2001) [135]).

between soil CO₂, calcite and DIC during recharge. Some of the well known traditional adjustment models are described below.

The geochemical aspects of radiocarbon dating can be divided into two parts: (i) definition of the ¹⁴C content at an initial point in the system (A_o), such as in the recharge zone where water becomes isolated from the modern ¹⁴C reservoir and (ii) adjustment of this initial ¹⁴C value for chemical reactions occurring along the flow path to the final well where ¹⁴C content (A) has been measured (Wigley et al. (1978) [136]). Traditionally, radiocarbon dating of groundwater has combined these two problems to develop an adjustment model that can be applied to a single water analysis at some point in the flow system. In this case, water chemistry, δ^{13} C, and the ¹⁴C value of DIC are measured for a single water sample. An adjustment model accounting for inorganic reactions affecting the inorganic carbon reservoir is applied to the single water analysis to define the ¹⁴C pmc value expected in the observed water if there were no radioactive decay of ¹⁴C. The adjusted ¹⁴C pmc value is compared to the measured ¹⁴C value through the radioactive decay equation to estimate the ¹⁴C model age of DIC in the water sample. Time elapsed since recharge, *t*, is:

$$t = \frac{5730}{\ln 2} \ln \left(\frac{A_{\rm nd}}{A}\right) \tag{4.4}$$

where

5730 is the modern half-life of ${}^{14}C$;

 A_{nd} is the initial ¹⁴C content (pmc value) after adjustment for geochemical reactions without radioactive decay, often referred to as A_0 in traditional adjustment models;

A is the measured ${}^{14}C$ content (pmc value) in the sample.

The above decay equation differs from the conventional radiocarbon age in that A_o (and A_{nd}) is no longer defined to be 100 pmc and the modern ¹⁴C half-life is used. To apply radiocarbon calibration scales, the Libby half-life (5568 a) is used or age is converted to the Libby half-life (Appendix to Chapter 4). A series of adjustment models that have been used to estimate values of the adjusted initial ¹⁴C value in groundwater are summarized below. Most of these models were discussed by Fontes (1983) [115], Fontes and Garnier (1979) [116], Fontes (1992) [117] and Kalin (1999) [111].

Vogel model

Vogel (1967) [137] and Vogel (1970) [138] assigned an estimate of 85 ± 5 pmc for A_0 based on approximately one hundred ¹⁴C measurements of dissolved carbon in groundwater from north-western Europe (Fontes and Garnier (1979) [116]), and isotope mass balance calculations that included isotope dilution and isotope exchange processes during recharge (Vogel and Ehhalt (1963) [139]).

Tamers model

Tamers (1967) [140] assumed that the initial quantity of soil zone CO_2 containing ¹⁴CO₂ was diluted by dissolution of radiocarbon-'dead' calcite in recharge areas. If the reactions take place at approximately neutral to somewhat alkaline pH, where HCO_3^- (and $CO_{2(aq)}$) are the predominant species, the reaction is:

$$CaCO_3 + CO_{2(aq)} + H_2O \rightarrow Ca^{2+} + 2HCO_3^{-}$$

$$(4.5)$$

To a first approximation, half of the HCO₃ is derived from soil gas CO₂ ('g') and half from calcite ('c'). Tamers assumed that CO_{2(aq)} ('a') was derived from soil gas CO₂. A carbon and ¹⁴C mass balance assuming $C_T = a + b$ (where 'b' is HCO₃) is, following the notation of Kalin (1999) [111]:

$$A_{o\text{Tamers}}C_{T} = (a + 0.5b)A_{g} + 0.5bA_{c}$$
(4.6)

or

$$A_{\text{oTamers}} = [(a + 0.5b)A_{\text{g}} + 0.5bA_{\text{c}}]/(a + b)$$
(4.7)

where A denotes the ${}^{14}C$ pmc value.

Owing to chemical equilibria in the carbonate solution, it is not exactly correct to assume that the quantity 'a' $(CO_{2(aq)})$ is all from soil CO₂. A more general approach is to perform a carbon mass balance, assuming DIC was derived from soil CO₂, and carbonate minerals. This avoids the need to make assumptions about predominant species in the carbonate system.

The Tamers model can be derived by using simple chemical and carbon isotope mass balance relations. The chemical evolution of precipitation (rain) in the calcite– CO_2 water system is as follows:

$$rain + CO_2 + calcite \rightarrow groundwater composition$$
 (4.8)

and the chemical mass balance relations are:

$$\Delta C_{\text{DIC}} = \Delta CO_2 + \Delta \text{calcite}$$
(4.9)

and

$$\Delta Ca = \Delta calcite \tag{4.10}$$

where Δ represents the change in moles, final (groundwater) minus initial (rain).

The ¹⁴C isotope mass balance is then:

$$A_{\rm o}\Delta C_{\rm T} = A_{\rm calcite}\Delta_{\rm calcite} + A_{\rm CO_2}\Delta \rm CO_2$$
(4.11)

and

$$A_{\rm o} = (A_{\rm calcite} \Delta_{\rm calcite} + A_{\rm CO_2} \Delta \rm CO_2) / \Delta \rm C_T \equiv A_{\rm oTamers}$$

$$\tag{4.12}$$

The Tamers model is extended in NETPATH (Plummer et al. (1994) [120]) to the CO_2 -calcite–dolomite water system and to the CO_2 -calcite–dolomite–gypsum water system. These are described below.

Tamers model in the CO₂-calcite-dolomite-water system

Here, the carbonate minerals are assumed to be calcite and dolomite, and are referred to as the 'Tamers model', as implemented in NETPATH (denoted 'Tamers, NP'). The geochemical reaction is:

$$rain + CO_2 + calcite + dolomite \rightarrow groundwater composition$$
 (4.13)

and the chemical mass balance relations are:

$$\Delta C_{\rm T} = \Delta CO_2 + \Delta_{\rm calcite} + 2\Delta_{\rm dolomite} \tag{4.14}$$

 $\Delta Ca = \Delta_{\text{calcite}} + \Delta_{\text{dolomite}}$ (4.15)

$$\Delta Mg = \Delta_{dolomite} \tag{4.16}$$

$$A_{\rm o}\Delta C_{\rm T} = A_{\rm calcite}\Delta_{\rm calcite} + A_{\rm CO_2}\Delta CO_2 + 2A_{\rm dolomite}\Delta_{\rm dolomite}$$
(4.17)

The solutions to these equations are as follows:

$$\Delta_{\text{dolomite}} = \Delta Mg \tag{4.18}$$

$$\Delta_{\text{calcite}} = \Delta Ca - \Delta_{\text{dolomite}} = \Delta Ca - \Delta Mg \tag{4.19}$$

$$\Delta CO_2 = \Delta C_T - \Delta_{calcite} - 2\Delta_{dolomite} = \Delta C_T - \Delta Ca - \Delta Mg$$
(4.20)

$$A_{\text{oTamers, NP}} = [A_{\text{calcite}}(\Delta Ca - \Delta Mg) + A_{\text{CO2}}(\Delta C_{\text{T}} - \Delta Ca - \Delta Mg) + 2A_{\text{dolomite}} \Delta Mg]/\Delta C_{\text{T}}$$
(4.21)

The term ' Δ ' represents the change in mass (moles) taken as final minus initial.

Tamers model in the CO₂-calcite-dolomite-gypsum water system

This model is another mass balance model implemented in NETPATH that is similar to the previous modified Tamers model, but with the addition of a mass balance on SO₄, assumed from gypsum dissolution in the recharge area or soil, referred to as the 'mass balance' model in NETPATH (Plummer et al. (1994) [120]) (denoted 'Tamers, MB').

$$A_{\text{oTamers, MB}} = [A_{\text{calcite}}(\Delta Ca - \Delta Mg - \Delta SO_4) + A_{\text{CO2}}(\Delta C_{\text{T}} - \Delta Ca - \Delta Mg + \Delta SO_4) + 2A_{\text{dolomite}} \Delta Mg]/\Delta C_{\text{T}}$$
(4.22)

Both modified forms of the Tamers model default to the Tamers model if there is no dissolution of dolomite or gypsum.

Pearson model

Ingerson and Pearson Jr. (1964) [132] solved the Tamers model for the dilution of soil zone CO_2 by dissolution of carbonate minerals by using isotope mass balance relations for ¹³C and ¹⁴C (denoted 'Pearson'):

$$\delta_{\rm T}\Delta_{\rm DIC} = \delta_{\rm g}\Delta_{\rm g} + \delta_{\rm c}\Delta_{\rm c}$$
 (13C isotope mass balance) (4.23)

$$A_{\rm T}\Delta_{\rm DIC} = A_{\rm g}\Delta_{\rm g} + A_{\rm c}\Delta_{\rm c}$$
 (¹⁴C isotope mass balance) (4.24)

$$\Delta_{\text{DIC}} = \Delta_{\text{g}} + \Delta_{\text{c}} \qquad (\text{inorganic carbon mass balance}) \qquad (4.25)$$

$$A_{oPearson} = \frac{A_{g}(\delta_{c} - \delta_{T}) + A_{c}(\delta_{T} - \delta_{g})}{(\delta_{c} - \delta_{s})}$$
(4.26)

or

$$A_{\rm oPearson} = \frac{(A_{\rm g} - A_{\rm c})(\delta_{\rm T} - \delta_{\rm c})}{(\delta_{\rm g} - \delta_{\rm c})} + A_{\rm c}$$
(4.27)

where

A is ¹⁴C pmc value; δ is δ^{13} C;

and the subscripts T, g and c refer to total DIC, soil gas CO_2 and carbonate mineral(s), respectively, following the notation of Fontes (1992) [117].

Therefore, the Tamers model and the Pearson model account for the same processes; the Tamers model finds a solution on the basis of chemical and ¹⁴C mass balance relations, and the Pearson model uses only isotopic mass balance relations for ¹³C and ¹⁴C.

The Tamers, mass balance and Pearson models assume a simple mixing between CO_2 dissolved in soil water and carbon derived from the dissolution of carbonate minerals, with no other sources or sinks of carbon in the system. These assumptions imply that the groundwater evolves chemically and isotopically through dissolution of carbonate minerals under closed (to CO_2 gas exchange) conditions; that is, CO_2 enters the water in the unsaturated zone (open to CO_2 gas exchange) and carbonate minerals react in the saturated zone (closed to CO_2 gas exchange). Although none of the mass balance models specifically incorporate isotope exchange, it would be appropriate to use values of $\delta^{13}C$ and the ¹⁴C content of soil gas CO_2 as those in water in isotopic equilibrium with the soil gas, thus accounting for isotopic fractionation in dissolution of soil gas CO_2 . Examples of chemical and isotopic evolution of recharge waters in open conditions are provided in the Appendix to Chapter 4. The remaining models (below) consider isotopic exchange.

Eichinger model

Eichinger (1983) [130] modified the Pearson model (Eq. (4.26)) to include cases of partial isotopic exchange. The model is as follows, again following the notation of Kalin (1999) [111]¹:

$$A_{\text{oEichinger}} = A_{\text{oPearson}} \times B \tag{4.28}$$

where

$$B = (\delta_{\rm T} - \delta_{\rm e})/(\delta_{\rm i} - \delta_{\rm e}) \tag{4.29}$$

and

$$\delta_{i} = [a\delta_{a} + 0.5b(\delta_{a} + \delta_{c})]/(a + b)$$
(4.30)

and

$$\delta_{\rm e} = [a(\delta_{\rm c} - \varepsilon_{\rm cb} + \varepsilon_{\rm gb} + \varepsilon_{\rm ag}) + b(\delta_{\rm c} - \varepsilon_{\rm cb})]/(a+b)$$
(4.31)

In Eichinger's model, the term $A_{oPearson}$ is the Pearson model (Eq. (4.26)), which accounts for the same geochemical processes as the Tamers model, but is solved using ¹³C isotope mass balance relations, and δ_T is the measured value of δ^{13} C of total DIC in the groundwater. The term δ_i estimates the value of δ^{13} C of the total DIC after dissolution of the carbonate phase, but without any isotope exchange with carbonates. The term δ_e estimates the value of δ^{13} C of the DIC if the groundwater is in isotopic equilibrium with the solid phase, where δ_e is δ^{13} C of calcite, ε_{cb} is the additive fractionation factor between calcite and HCO₃, ε_{gb} is the additive fractionation factor between CO_{2gas} and HCO₃, and ε_{ag} is the additive fractionation factor between CO_{2gas} and HCO₃, The Eichinger model only includes isotope exchange with the solid phase.

IAEA model

In an IAEA study, Salem et al. (1980) [141] proposed that the Pearson model could be considered as a two step process: (i) equilibrium of the HCO_3^- with the gas phase followed by (ii) dissolution of solid carbonate. The equation is (Fontes (1992) [117]):

$$A_{oIAEA} = \frac{(\delta_{T} - \delta_{c})(A_{g} - A_{c}) + (\delta_{g} - \varepsilon_{gb} - \delta_{c})A_{c}}{(\delta_{g} - \varepsilon_{gb} - \delta_{c})}$$
(4.32)

¹ There is a typographical error in Eq. (10) of Kalin (1999) [111] where the term δ_c should be replaced with δ_e , as above. Further confusion regarding Eichinger's equation was noted in Plummer et al. (1994) [120] and Fontes (1992) [117], correcting a typographical error in Eichinger (1983) [130]. Finally, although mathematically correct and programmed correctly in NETPATH, Plummer et al. (1994) [120] add to the confusion by erroneously defining the term δ_e .

As with Pearson's model, this model implies that all chemical reactions can be accounted for by the ¹³C isotopic composition of the end members (pure mixing), with one of them completely isotopically exchanged with the gas phase. The IAEA model can be solved in NETPATH by choosing the Pearson model and selecting the isotope mass balance model ('mass balance with fractionation') for definition of δ^{13} C of soil gas CO₂. As pointed out by Fontes (1992) [117], the IAEA model gives higher A_o values than the Pearson model. In one numerical example, A_o from Pearson's model was approximately 58.2 pmc, but the IAEA model gave 96.2 pmc (Fontes (1992) [117]).

Evans model

Evans et al. (1979) [131] developed a model to account for isotopic fractionation during recrystallization (dissolution-precipitation) of calcium carbonate in groundwater. It is assumed that calcite is in isotopic equilibrium with dissolved HCO_3 . Their equation, as modified by Fontes (1992) [117] reduces to:

$$A_{\text{oEvans}} \approx (A_{\text{g}} - A_{\text{c}}) \left(\frac{(\delta_{\text{T}} + \varepsilon_{\text{cb}} - \delta_{\text{c}})}{(\delta_{\text{g}} + \varepsilon_{\text{cb}} - \delta_{\text{c}})} \right) + A_{\text{c}}$$
(4.33)

As pointed out by Fontes (1992) [117], the modified model (Evans et al. (1979) [131]) is similar to Pearson's model and produces A_0 values similar to Pearson's model despite the fact that the two models have quite different conceptualizations and derivations.

The Mook model

The Mook model (Mook (1972) [133]; Mook (1976) [142]; Mook (1980) [109]) estimates A_0 in a step by step approach, considering partial or complete isotopic equilibration in the soil zone between CO₂ gas and all aqueous carbon bearing species, including part of the dissolving carbonate mineral (Fontes (1992) [117]). The Mook model is more appropriate in systems in which reactions with carbonate minerals are not dominant (Fontes (1992) [117]; Mook (1976) [142]). The Mook model can be expressed as the Tamers model plus a correction term (Fontes (1992) [117]). Here, the Mook model is provided using the notation of Plummer et al. (1994) [120], which is mathematically equivalent to the form given by Fontes and Garnier (1979) [116]).

$$\begin{aligned} A_{oMook} &= N_{CO_2 aq} A_{CO_2 aq(o)} + 0.5(1 - N_{CO_2 aq}) (A_{CO_2 aq(o)} + A_{ls(o)}) \\ &+ (A_{CO_2 g(o)} (1 - 2 \times 10^{-3} \varepsilon_{gb}) - 0.5(A_{CO_2 aq(o)} + A_{ls(o)})) \\ &\times \frac{\delta^{13} C - N_{CO_2 aq} \delta^{13} C_{CO_2 aq(o)} - 0.5(1 - N_{CO_2 aq}) (\delta^{13} C_{CO_2 aq(o)} + \delta^{13} C_{ls(o)})}{\delta^{13} C_{CO_2 g(o)} - \varepsilon_{gb} (1 + 10^{-3} \delta^{13} C_{CO_2 g(o)}) - 0.5(\delta^{13} C_{CO_2 aq(o)} + \delta^{13} C_{ls(o)})} \end{aligned}$$
(4.34)

where

Nrefers to the fraction of DIC represented by the subscripted species;the subscript orefers to the initial condition before isotope exchange;the subscript lsrefers to limestone;and the subscript grefers to CO₂ gas.

Values of the additive fractionation factors (isotopic enrichment factor), ε_{ij} are provided in the Appendix to Chapter 4.

The Fontes and Garnier model

Fontes and Garnier (1979) [116] (see also Fontes (1983) [115]; Fontes (1992) [117]) present the 'global exchange–mixing model in closed system' for estimation of A_0 . This model considers the mixing of two end members, soil gas CO₂ and solid carbonate mineral, which is accompanied by a partial

isotopic exchange in a closed system during the mixing. The isotopic exchange is assumed to occur between a part of the CO₂ gas and calcite solid in the system (Fig. 4.4), where q and q' are the moles of calcite and CO_{2gas} that undergo complete isotopic exchange (with an isotopic enrichment factor, ε , between CO₂ gas and calcite). The partial isotope exchange in ¹³C (Fontes and Garnier (1979) [116]) is described by the following carbon isotope mass balance relations:

$$\delta_{\rm T} C_{\rm T} = (C_{\rm M} - q)\delta_{\rm M} + (C_{\rm T} - C_{\rm M})\delta_{\rm g} + q(\delta_{\rm g} - \varepsilon)$$
(4.35)

and

$$\delta_{\rm T} C_{\rm T} = C_{\rm M} \,\delta_{\rm M} + (C_{\rm T} - C_{\rm M} - q')\delta_{\rm g} + q'(\delta_{\rm M} + \varepsilon) \tag{4.36}$$

where (retaining the notation of Fontes and Garnier (1979) [116])

- δ is ¹³C content in ‰;
- C refers to carbon;

T, M, g refer to total, solid carbonate and gas, respectively;

- *q* is the moles of solid carbonate in isotopic equilibrium with a part of the soil gas CO₂;
- q' is the moles of soil gas CO₂ in isotopic equilibrium with the solid carbonate;
- ε is the isotopic enrichment factor (additive fractionation factor) between CO₂ gas and solid carbonate ($\varepsilon_{gc} = \delta_g \delta_c$).

As q = -q', the isotope exchange is shown by:

$$q = -q = \frac{\delta_{\rm T} C_{\rm T} - C_{\rm M} \delta_{\rm M} - \delta_{\rm g} (C_{\rm T} - C_{\rm M})}{\delta_{\rm g} - \varepsilon - \delta_{\rm M}}$$
(4.37)

where the sign of q indicates the direction of the exchange.

If q is positive, the isotopic exchange is dominated by gaseous CO₂, as might apply to infiltration water in contact with sediment that is low in carbonate mineral content in the soil zone, unsaturated zone or near the water table. Calculated values of q that are less than zero imply that the isotopic exchange is dominated by solid carbonate mineral, as might be more common in the saturated zone. Both processes occur and the sign of q indicates which process predominates during the isotopic evolution.



FIG. 4.4. The global exchange-mixing model in a closed system (Fontes (1983) [115]; Fontes and Garnier (1979) [116]).

In Fig. 4.4, cases 1 and 2 refer to exchange controlled by gaseous CO_2 of isotopic composition δ_g , and solid carbonate (calcite) of isotopic composition δ_M , respectively. The variables q and q' are the molalities of calcite and CO_{2gas} that undergo complete isotopic exchange (with an enrichment factor ε between CO_2 and calcite). C_T and C_M are the molalities of DIC and DIC of mineral origin, respectively; this is taken from Fontes and Garnier (1979) [116].

The carbon isotope mass balance relations of Fig. 4.4 can be written for ¹⁴C, prior to radioactive decay, so that A_0 is:

$$A_{o}C_{T} = C_{M}A_{M} + (C_{T} - C_{M})A_{g} + q(A_{g} - 0.2\varepsilon - A_{M})$$
(4.38)

where

A is the ¹⁴C pmc value; $\varepsilon^{14}C(\%) \cong 0.2 \ \varepsilon^{13}C(\%)$ (see Craig (1954) [143] and the Appendix to Chapter 4).

In developing their model, Fontes and Garnier (1979) [116] apply a chemical mass balance similar to that of the Tamers model, with provision for base exchange (Ca/Na cation exchange) and gypsum dissolution to estimate the mass of carbon dissolved from inorganic sources, C_M . Fontes (1992) [117] shows that the Fontes and Garnier (1979) [116] model reduces to the Tamers model if there is no isotopic exchange (k = 0):

$$A_{\rm oF-G} = A_{\rm oTamers} + k \tag{4.39}$$

or

$$A_{\text{oF-G}} = \left(1 - \frac{C_{\text{M}}}{C_{\text{DIC}}}\right) A_{\text{CO}_2 g} + \frac{C_{\text{M}}}{C_{\text{DIC}}} A_{\text{M}} + k$$
(4.40)

where

 $C_{\rm M}$ is the moles of carbon from carbonate mineral dissolution; $C_{\rm DIC}$ is the moles of total DIC in the groundwater sample; $A_{\rm CO_{2g}}$ is the ¹⁴C value of CO₂ gas; $A_{\rm M}$ is the average ¹⁴C pmc value of the carbonate minerals dissolving; and

$$k = \left(A_{\rm CO_{2}g} - 0.2\varepsilon_{\rm i-j} - A_{\rm M}\right) \left(\frac{\delta^{13}C_{\rm DIC} - \frac{C_{\rm M}}{C_{\rm DIC}}\delta^{13}C_{\rm M} - \left(1 - \frac{C_{\rm M}}{C_{\rm DIC}}\right)\delta^{13}C_{\rm CO_{2g}}}{\delta^{13}C_{\rm CO_{2g}} - \varepsilon_{\rm i-j} - \delta^{13}C_{\rm M}}\right)$$
(4.41)

where ε_{i-j} refers to the additive fractionation factor (also referred to as the isotopic enrichment factor; see Appendix to Chapter 4) between species i and j.

In using the model of Fontes and Garnier (1979) [116], k is first solved by using the additive fractionation factor, $\varepsilon_{CO_{2g}-HCO_{3}}$ ($\cong \delta^{13}C_{CO_{2g}} - \delta^{13}C_{HCO_{3}}$ at isotopic equilibrium). If k is positive, then the exchange is primarily between CO_{2gas} and HCO_{3} , and A_{0} is calculated by using the value of k based on $\varepsilon_{CO_{2g}-HCO_{3}}$. If k is negative, the reaction is dominated by isotopic exchange between calcite and bicarbonate, and the additive fractionation factor is replaced with the value of $\varepsilon_{calcite-HCO_{3}}$ (Appendix to Chapter 4), ($\cong \delta^{13}C_{calcite} - \delta^{13}C_{HCO_{3}}$ at isotopic equilibrium).

In application to recharge waters, the model of (Fontes and Garnier (1979) [116]) often yields quite reasonable estimates of A_0 , but it is sensitive to values of δ^{13} C of soil gas CO₂, which are often not

available. Therefore, several models are available in NETPATH to estimate the δ^{13} C of soil gas CO₂, as described below.

4.2.1.3. Models to estimate the $\delta^{13}C$ of soil gas CO_2

The models of Ingerson and Pearson, Evans, IAEA, Mook, Fontes and Garnier, and Eichinger all require a definition of δ^{13} C of soil gas CO₂. In the absence of measurement, several models were implemented in NETPATH (Plummer et al. (1994) [120]) to estimate values of δ^{13} C of soil gas CO₂. These are: (i) user defined; (ii) closed system mass balance without fractionation; (iii) a two-step process in which the mass balance is solved by assuming that CO₂ gas dissolved into the initial water maintaining isotopic equilibrium with the dissolved CO₂ (aq) (open system), followed by carbonate dissolution in a closed system; and (iv) a complete open system in which the δ^{13} C of soil gas CO₂ is calculated corresponding to isotopic equilibrium with the chemical and isotopic composition of the initial solution.

Model 1

Model 1, 'user defined', is used if δ^{13} C measurements of soil gas CO₂ are available or if there is climatic evidence that the palaeo- δ^{13} C of soil gas CO₂, at the time the water sample was recharged, differed from today.

Model 2

Model 2 solves a carbon isotope mass balance without isotopic fractionation for the case of dissolution of CO_2 gas, calcite, dolomite and gypsum:

$$\delta^{13} C_{CO_2 aq(o)} = \frac{\delta^{13} C_{DIC} C_{DIC} - \Delta_{calcite} \delta^{13} C_{calcite} - 2\Delta_{dolomite} \delta^{13} C_{dolomite}}{\Delta_{CO_{2g}}}$$
(4.42)

and

$$\delta^{13} C_{CO_2 g(o)} \equiv \delta^{13} C_{CO_2 aq(o)}$$
(4.43)

Model 3

Model 3 solves the same carbon isotope mass balance as in model 2, but assumes that the dissolved CO_2 is in isotopic equilibrium with the soil gas:

$$\delta^{13}C_{CO_2g(o)} \equiv \delta^{13}C_{CO_2aq(o)} + \mathcal{E}_{CO_2g-CO_2aq}$$
(4.44)

Model 3 applies to recharge through an unsaturated zone devoid of carbonate minerals, followed by subsequent carbonate mineral dissolution in the saturated zone (closed system dissolution).

Model 4

Model 4 assumes that the recharge water evolved under open system conditions:

$$\delta^{13} \mathbf{C}_{\mathrm{CO}_2 \mathsf{g}(\mathsf{o})} \equiv \delta^{13} \mathbf{C}_{\mathrm{DIC}} + \varepsilon_{CO_{2g-s}} \tag{4.45}$$

where $\varepsilon_{CO_{2g-s}}$ is the pH dependent isotopic enrichment factor between CO₂ gas and the DIC of the aqueous solution (see Wigley et al. (1978) [136] and the Appendix to Chapter 4). Models 3 and 4 tend to be the most realistic. Model 4 can apply, among other scenarios, to semi-arid regions with low recharge rates through carbonate bearing unsaturated zones.

4.2.1.4. Summary of traditional adjustment models

Table 4.1 lists geochemical processes included in the better known traditional adjustment models. Several studies have carefully documented differences between the various traditional adjustment models by using examples (Fontes (1992) [117]; Plummer and Sprinkle (2001) [135]). Fontes (1992) [117] compared calculated and measured ¹⁴C content in DIC for a series of unsaturated zone waters that recharge a chalk aquifer. Model calculations of A_0 from Tamers (1975) [134], Evans et al. (1979) [131], Fontes and Garnier (1979) [116], the IAEA (Salem et al. (1980) [141]), Ingerson and Pearson Jr. (1964) [132], Eichinger (1983) [130] and Mook (1972) [133] were compared to the measured ¹⁴C profile. The measured ¹⁴C content of DIC decreased from 117.5 pmc at a 2 m depth through the unsaturated zone to 67.1 pmc at a 20 m depth. The models most successful at estimating the initial ¹⁴C value at a 20 m depth and, thus, most representative of recharge waters, were those of Eichinger (71.5 pmc), Evans (75.5 pmc), Fontes and Garnier (77.1 pmc), and Ingerson and Pearson (77.2 pmc).

Plummer and Sprinkle (2001) [135] compared adjusted ¹⁴C model ages of DIC in 25 water samples from the Floridan aquifer, FL, USA, based on the models of Tamers (1975) [134], Ingerson and Pearson Jr. (1964) [132], Mook (1972) [133], Eichinger (1983) [130], and Fontes and Garnier (1979) [116], with the unadjusted ¹⁴C model age (Eq. (4.3), where $A_{nd} \equiv 100$ pmc). As expected, the adjusted ¹⁴C model ages were always younger than the unadjusted ¹⁴C model age. Relatively small differences (typically less than 10%) in adjusted ¹⁴C model age based on these traditional adjustment models were found when applied to the waters of the Floridan aquifer. However, Plummer and Sprinkle (2001) [135] demonstrated that the traditional adjustment models did not account for the observed enrichment in δ^{13} C of DIC in many of the more geochemically evolved groundwater samples. As a result, more complex adjustment models that included redox reactions, mixing with saline water, and carbonate mineral recrystallization were constructed by using NETPATH (see examples in Section 4.7.2).

					$A_{\rm o}$ mode	la				
Process	Conventional ¹⁴ C age:	Vogel	Tamers	Mass balance	Pearson	IAEA	Mook	Evans	Eich- inger	Fontes and Garnier
Carbonate dissolution			×	×	×	×	×	×	×	×
Soil gas CO_2 dissolution			×	×	×	×	×	×	×	×
CO ₂ gas– aqueous exchange						×	×			×
Calcite– HCO₃ exchange								×	×	×
Gypsum dissolution				×						×
Ca/Na cation exchange										×

TABLE 4.1. SUMMARY OF GEOCHEMICAL REACTIONS INCLUDED IN SELECTED TRADITIONAL A_0 ADJUSTMENT MODELS

^a See above text for references and discussion of each model.

Selection of the most appropriate adjustment model depends on which models most completely account for the geochemical processes affecting the chemical and isotopic composition of the waters. The model of Fontes and Garnier (1979) [116] is the most geochemically complete of the traditional adjustment models and often yields estimates of A_0 that are reasonable in aquifers undergoing relatively common inorganic geochemical reactions (Table 4.1). However, the model of Fontes and Garnier (1979) [116], as well as several other traditional adjustment models, depends on knowing the δ^{13} C value of unsaturated zone CO₂ in the recharge area. This can be estimated from the observed or postulated value of DIC δ^{13} C in the recharge area by using soil gas CO₂ models 3 or 4 (see Section 4.2.1.3), which usually bound the range of soil gas CO₂ δ^{13} C values. Alternatively, attention should be paid to palaeoclimatic conditions in the recharge area and possible changes in C₃ abundance relative to C₄ plants.

As a general rule, it is best to apply the traditional adjustment models only to waters in recharge areas to estimate the pre-bomb value of A_0 in a recharge zone. Waters in recharge areas tend to be the least geochemically evolved and most suitable for estimation of A_0 using the traditional adjustment models. More sophisticated geochemical corrections, such as those provided by NETPATH, discussed below, can clarify the evolution of recharge water into observed palaeowater. This process leads to the further geochemical adjustment of A_0 , accounting for more complex geochemical reactions occurring in the aquifer that are not accounted for in traditional adjustment models. It leads to the final adjusted value of A_0 , denoted A_{nd} (Eq. (4.3)), and often to improved estimates of the adjusted ¹⁴C model age.

4.3. SUMMARY OF PREDOMINANT GEOCHEMICAL REACTIONS IN GROUNDWATER SYSTEMS AFFECTING INTERPRETATION OF RADIOCARBON AGE

Many more geochemical and isotopic reactions occur in groundwater systems that are not considered by any of the traditional adjustment models. The most important of these pertain to the presence of organic carbon, either as ¹⁴C-bearing DOC in recharge waters and/or as a reactant in redox reactions that are driven by the oxidation of (usually ¹⁴C-'dead') organic carbon buried in aquifer sediment. In the first case, DOC in recharge waters is usually oxidized microbially to bicarbonate in the aquifer, adding to the initial ¹⁴C concentration; failure to include initial DOC (and its ¹⁴C content) leads to adjusted radiocarbon ages that are too young. In the second case, old organic carbon is oxidized in the aquifer, which dilutes the ¹⁴C reservoir, and if not accounted for, the adjusted age is too old. Commonly occurring redox reactions involving organic carbon in aquifers include oxygen reduction, nitrate reduction, manganese reduction, iron reduction, sulphate reduction and methanogenesis (see, for example, McMahon and Chapelle (2008) [144]). Each of these redox reactions adds carbon to the DIC concentration derived from organic sources.

Other common reactions, such as de-dolomitization (Plummer et al. (1990) [145]) or weathering of feldspars cause precipitation of calcium carbonate, which involves an isotopic fractionation affecting both ¹³C and ¹⁴C. Although the Fontes and Garnier model includes Ca/Na cation exchange, there are many other types of cation exchange that occur in groundwater. The most important of these involve the uptake of magnesium for sodium (Plummer et al. (1990) [145]) or the release of protons from organic matter in exchange for sodium (proton exchange) (Appelo (1994) [146]; Plummer et al. (1994) [120]). Uptake of magnesium and/or calcium on exchangers, such as clay minerals, permits additional dissolution of carbonate minerals (calcite and/or dolomite), which dilutes the ¹⁴C reservoir. If not corrected for cation exchange, the 'adjusted' ¹⁴C model age is too old. In the case of protons and sodium ions. The released protons react with old carbonates, if present, diluting the ¹⁴C reservoir and, again, if not accounted for, the 'adjusted' ¹⁴C model age is too old. A list of important geochemical reactions and processes that can affect interpretation of ¹⁴C model age, but are not entirely accounted for by the application of 'traditional' adjustment models, is provided in Table 4.2. An even deeper appreciation for the complexity of radiocarbon dating in groundwater systems is gained when one realizes that

RADIOCARBON AGE (in addition to those listed	ł in Table 4.1)			
Process/reaction	Resulting water type	Effect on $\delta^{13}C$	Effect on ¹⁴ C	Effect on unadjusted age
Dissolution of calcite and dolomite (marine carbonates)	Ca–Mg–HCO ₃	Increase in δ^{13} C; isotope dilution	Decrease in ¹⁴ C; isotope dilution	Old bias
CaSO ₄ dissolution (not a carbon source), calcite precipitation	Ca–SO ₄ –HCO ₃	Small decrease in δ^{13} C as 13 C is enriched in calcite cement; isotope fractionation	Small decrease in ¹⁴ C of DIC as ¹⁴ C is enriched in calcite cement; isotope fractionation	Old bias
CaSO ₄ dissolution (not a carbon source), dolomite dissolution and calcite precipitation; de-dolomitization	Ca–Mg–SO₄–HCO₃	Increase in δ^{13} C if dolomite enriched in 13 C, also slightly opposite trend from calcite cement formation; isotope fractionation	Decrease in ¹⁴ C; isotope dilution; isotope fractionation	Old bias
Ca/Na exchange, Mg/Na exchange, proton exchange (carbonate dissolution)	Na-HCO3	Increase in δ^{13} C; isotope dilution	Decrease in ¹⁴ C; isotope dilution	Old bias
Recrystallization of calcite (aragonite, Mg-calcites); isotopic exchange (calcite)	No change (increase in Sr, Mg from aragonite and Mg calcite)	Increase in 813C; isotope exchange	Decrease in ¹⁴ C; isotope exchange	Old bias
Oxidation of organic matter: Fe reduction (FeOOH)	Increase in Fe^{2+} and $HCO_{\overline{3}}$	Decrease in δ^{13} C; isotope dilution	Decrease in ¹⁴ C; isotope dilution	Old bias
Oxidation of organic matter; sulphate reduction (pyritization)	Decrease in SO ₄ , possible increase in H ₂ S, decrease in Fe ²⁺	Decrease in δ^{13} C; isotope dilution	Decrease in ¹⁴ C; isotope dilution	Old bias
Fermentation of organic matter; methanogenesis	Increase in CH ₄ and CO ₂	Increase in 8 ¹³ C of CO ₂ , depleted CH ₄ ; isotope dilution	Decrease in ¹⁴ C; isotope dilution	Old bias
Dissolution of plagioclase feldspar; dissolution of other primary silicates (calcite precipitation)	Na-Ca-HCO3	Small decrease in δ^{13} C as 13 C is enriched in calcite cement; isotope fractionation	Small decrease in ¹⁴ C as ¹⁴ C is enriched in calcite cement; isotope fractionation	Minor or none

TABLE 4.2. SUMMARY OF SELECTED CHEMICAL AND PHYSICAL PROCESSES IN GROUNDWATER SYSTEMS AFFECTING INTERPRETATION OF Y

Leakage of saline waters (may cause	Na-Cl	Small increase in δ^{13} C; isotone dilution	Small decrease in ¹⁴ C; isotone dilution	Old bias
Leakage or exchange with aquitards; diffusion,	Multiple	Variable	Decrease in ¹⁴ C; isotope dilution	Old bias
Addition of CO ₂ of magmatic origin (geogenic CO ₃)	Multiple	Generally enriched in δ^{13} C, range from -2 to $-6\%_0$	Decrease in ¹⁴ C; isotope dilution	Old bias
Warming along a geothermal gradient; calcite dissolution (closed system)	Small increase in Ca^{2+} and $HCO_{\overline{3}}$	Small increase in δ^{13} C; isotope dilution	Small decrease in ¹⁴ C; isotope dilution	Old bias
Increase in hydrostatic pressure with depth; calcite dissolution	Small increase in Ca ²⁺ and HCO ₃	Small increase in δ^{13} C; isotope dilution	Small decrease in ¹⁴ C; isotope dilution	Old bias
Evapotranspiration	Increase in all solutes in proportion to original water	None	None	None

multiple reactions and processes, such as those listed in Table 4.2, often occur together or in sequence along flow paths in aquifers.

4.4. GENERALIZED GEOCHEMICAL ADJUSTMENT MODELS

Wigley et al. (1978) [136] and Wigley et al. (1979) [147] describe the chemical and isotopic evolution of inorganic carbon in groundwater by the differential equations:

Carbon mass balance

$$d(m_{\rm DIC}) = \sum_{i=1}^{N} dI_i - \sum_{i=1}^{M} dO_i$$
(4.46)

Carbon isotope mass balance

$$d(Rm_{\rm DIC}) = \sum_{i=1}^{N} R^* dI_i - \sum_{i=1}^{M} R\alpha_{i-s} dO_i$$
(4.47)

where

R	is the isotope ratio;
$m_{\rm DIC}$	is the molality of DIC;
I and O	refer to incoming and outgoing moles of carbon, such as through dissolution and precipitation, respectively;
N and M	are the total number of incoming and outgoing phases;
i	refers to the <i>i</i> th carbon-bearing phase;
superscript *	refers to the incoming phases;
α_{i-s}	is the fractionation factor between the <i>i</i> th phase and the aqueous solution (adjusted
	for pH effects on the distribution of inorganic carbon species in solution; see
	Appendix to Chapter 4).

Analytical solutions to the two differential equations, in the form of Rayleigh distillation processes, were derived by Wigley et al. (1978) [136] and Wigley et al. (1979) [147] for the cases shown in Table 4.3.

The analytical solutions to the isotope evolution problem assume constant relative rates of reaction along the evolutionary flow path from the initial to the final condition. Thus, the ratio of incoming to outgoing moles of carbon is assumed to be constant along the flow path and, in its implementation

TABLE 4.3. SUMMARY OF ANALYTICAL SOLUTIONS TO RAYLEIGH DISTILLATION MODELS^a

		Number of fractionating outputs					
		0	1	2	М		
	0		×	×			
Number of inputs	1	×	×	×			
	2	×					
	N				NETPATH		

^aX: analytical solution in Wigley et al. (1978) [136] and Wigley et al. (1979) [147]. N and M refer to the total number of incoming and outgoing carbon-bearing phases, respectively.

in NETPATH, equal to that calculated from the net mass transfer for any particular model solved in the mass balance problem. Although the net mass transfer is determined by using inverse modelling techniques, as in NETPATH, the relative rates of reaction may vary along flow paths in groundwater systems. In application of the Wigley et al. equations to groundwater systems, it is also assumed that fractionation factors, α_{i-s} , are constant over the path of the reaction, and that a single value applies for each, even though pH can vary on the path. Although not exhaustive, Wigley et al. (1978) [136] and Plummer et al. (1983) [148] have shown that for some common geochemical reactions in groundwater systems, the modelled isotopic composition is not particularly sensitive to uncertainties in relative rates of reaction and variations in α_{i-s} along the reaction path.

NETPATH (Plummer et al. (1994) [120]) uses equations of chemical mass balance, electron balance and isotope mass balance to define all possible net geochemical reactions between the analysed initial and final water compositions along a flow path. As pairs of samples that occur along a specific flow path in an aquifer cannot always be identified, representative initial water compositions can be constructed through the simulation of geochemical reactions by using computer codes such as PHREEQC (Parkhurst and Appelo (1999) [149]); alternatively, waters in the recharge zone that apply to other flow paths can be selected if they can be assumed to be representative of initial conditions. The geochemical reactions are constrained to occur among reactant and product minerals and gases for the system, and to be consistent with the observed mineralogy, chemical and isotopic data of the aquifer and groundwater system.

Having found all of the possible geochemical reactions that can account for the chemical and isotopic constraints, NETPATH (Plummer et al. (1994) [120]) solves the chemical reaction as a forward isotope evolution model, using the general case of N non-fractionating inputs (dissolving carbonate phases) and M fractionating outputs (precipitation carbonate phases) (Wigley et al. (1978) [136]; Wigley et al. (1979) [147]). For each simulation, NETPATH calculates the ¹⁴C pmc value of TDC (TDC = DIC + DOC + CH₄), in the final water. NETPATH can be used to construct ¹⁴C adjustment models for a wide range of geochemical systems, including those considered in the 'traditional' adjustment models and many more systems that cannot be treated by previous DIC adjustment models. The approach is diagrammed in Fig. 4.5.



FIG. 4.5. Conceptualization of radiocarbon dating of dissolved inorganic carbon (or total dissolved carbon, TDC) in NETPATH (from Plummer and Sprinkle (2001) [135]).

By combining carbon mass balance equations with Rayleigh distillation equations for all incoming carbon sources and all isotopically fractionating outgoing carbon phases, the initial ¹⁴C (A_o) is adjusted for the modelled geochemical reactions (Fig. 4.5). Two evolutionary waters are selected in Fig. 4.5: the initial, A, and final, B. A and B are typically on a flow path but are only required to be representative of evolutionary pairs. A_o is modelled, measured or estimated in water from the initial well. NETPATH constructs geochemical adjustment models to estimate the ¹⁴C content of TDC in water from well B, without radioactive decay, A_{nd} . The piston flow travel time between A and B is calculated from the decay equation (Eq. (4.4)).

NETPATH includes most of the well known adjustment models described above, which can be applied to the initial water to obtain estimates of A_0 . In radiocarbon dating of DIC in groundwater using NETPATH, the 'traditional' adjustment models are usually applied to the initial water only; in the recharge portions of aquifers, the geochemical reactions may be less complex than those further down gradient. Application of models to the initial water is useful in defining A_0 in recharge areas where the ¹⁴C content of DIC has not been measured or is contaminated with fractions of post-nuclear detonation ¹⁴C.

Alternatively, NETPATH can be used to reconstruct the isotopic composition of the initial water by considering a reaction path beginning with precipitation that is in equilibrium with atmospheric CO_2 , which subsequently reacts in open (or closed) systems with soil gas CO_2 and reactive minerals in the recharge zone. In this case, the initial water chemical composition is solved by using forward simulation models such as PHREEQC.

In general use, the initial and final waters are defined separately in NETPATH. NETPATH is then used to describe the geochemical reactions that reproduce the chemical and δ^{13} C isotopic composition of DIC in the final water. This approach develops a separate adjustment model for each water analysis. The adjustment is applied to the initial ¹⁴C to compute the ¹⁴C expected in DIC (or TDC) at the final well in the absence of radioactive decay, A_{nd} (Fig. 4.5). The adjusted 'no decay' ¹⁴C pmc value is then used with the measured ¹⁴C pmc value to compute the apparent piston-flow travel time from the initial to the final point. Further details of radiocarbon dating applications in NETPATH are provided in Plummer et al. (1994) [120].

4.5. TOTAL DISSOLVED CARBON

Radiocarbon dating is usually only applied to the DIC of a system. None of the 'traditional' adjustment models described above allow for the presence of DOC. All carbon isotopic calculations in NETPATH are made in terms of TDC (TDC = DIC + DOC + CH₄). For consistency with this definition of TDC, it is necessary to change the values of A_0 calculated from the above inorganic models to the following:

$$A_{\rm oTDC} = \frac{A_{\rm oDIC} m_{\rm DIC} + {}^{14} C_{\rm DOC} m_{\rm DOC} + {}^{14} C_{\rm CH_4} m_{\rm CH_4}}{m_{\rm TDC}}$$
(4.48)

where

DOC is dissolved organic carbon; and *m* is molality.

If the concentrations of DOC and CH_4 are zero in the initial solution, then A_0 is defined identically to the above described inorganic carbon A_0 models. If DOC and/or CH_4 are present in the water to be ¹⁴C dated, their concentrations and ¹³C and ¹⁴C isotopic composition must be defined.

Special treatment is needed in NETPATH in defining the ¹³C and ¹⁴C composition of TDC. First, the carbon isotope fractionation factors, which are defined for inorganic carbon species, are calculated relative to TDC by using measured or defined values of the carbon isotopic composition of DOC and

 CH_4 (Plummer et al. (1994) [120]) (see the Appendix to Chapter 4). If DOC and/or CH_4 are present, NETPATH computes the average ¹⁴C model age of TDC. In NETPATH, DOC represents the sum of the moles of carbon (expressed in millimoles of carbon per kilogram of H_2O) of all of the dissolved organic species.

It is usually not possible to identify all of the individual DOC species that make up DOC. Similarly, it is difficult to determine the ¹³C and ¹⁴C content and oxidation state of carbon in individual organic species in solution. Considering these uncertainties, NETPATH accepts an average ¹³C and ¹⁴C content, and average oxidation state of carbon for the total DOC. If it is known, for example, from laboratory experiments that one or several of the dissolved organic species that make up the total DOC are reactive, more realistic models would be obtained by using data specific to the reactive species.

4.6. GEOCHEMICAL MASS TRANSFER MODELS

By using charge balance constraints and mass balance constraints on chemical, redox and isotopic constituents, inverse geochemical modelling helps eliminate reaction hypotheses that are inconsistent with chemical and isotopic observations, and can point to additional data needs that are critical to resolution of the problem. Typically, inverse geochemical modelling leads to multiple hypotheses, also known as reaction model solutions or sets of reactions, that may explain the observations and hopefully improve the conceptualization of groundwater flow and geochemical evolution in the system (Parkhurst and Plummer (1993) [150]; Plummer et al. (1983) [148]). When applied to radiocarbon dating of DIC in groundwater, the modelling, though non-unique, can place constraints on the calculated tracer model age of the waters. Several approaches have been taken to address geochemical model uncertainty.

Pearson (1992) [151] combined geochemical mass balance modelling with radiocarbon dating to generate a distribution of possible ¹⁴C model ages considering the non-unique nature of the modelling process. Parkhurst developed an inverse modelling capability in PHREEQC that considers the uncertainty in chemical data (Parkhurst (1995) [152]; Parkhurst (1997) [153]; Parkhurst and Appelo (1999) [149]). This uncertainty can be related to the analytical uncertainty of a particular sample or to the variability of analyses for a series of samples that should represent a particular water. Although PHREEQC does not treat radiocarbon dating in a general way, it can adjust an initial ¹⁴C content for all of the possible geochemical reactions in the system, and, in principle, lead to an estimation of the range of ¹⁴C model ages consistent with all of the chemical and isotopic data. As the generally available version of PHREEQC does not calculate fractionation factors as a function of solution composition, average isotopic compositions of precipitating or exsolving phases need to be calculated and entered manually. PHREEQC also produces what are called 'minimal models' within the inverse modelling mode. Minimal models are geochemical mass balance reaction models that include only reactants and products that, within the uncertainty in the chemical and isotopic data, must be included to account for the observed chemical and isotopic data.

Glynn and Brown (2012) [154] propose the combined use of inverse geochemical modelling using codes such as NETPATH or PHREEQC (in inverse modelling mode) and forward modelling (e.g. using PHREEQC or other codes) as an efficient way to conceptualize the geochemical evolution of groundwater systems. Inverse geochemical modelling helps identify the key geochemical reaction possibilities that can explain observed field data. The possibilities considered by inverse geochemical modelling include the possible 'mixing' or contributions of water and solutes converging (or diffusing) from various confining and transmissive zones (or surface water bodies) to form the 'final' groundwater sample collected for analysis. NETPATH and PHREEQC require that specific 'initial' water compositions be defined, as opposed to having a continuum of solution compositions, to represent this mixing process. Following inverse geochemical modelling and the determination of possible reaction and 'mixing' processes, forward 'predictive' modelling can be used: (i) to estimate the relative movements of reaction fronts, water and solutes; (ii) to assess the degree to which the groundwater system can be considered to be at a chemical steady state for the purpose of inverse modelling and radiocarbon dating with NETPATH; and (iii) to determine whether the mass transfers and ¹⁴C model ages calculated through inverse modelling are reasonable given the hydrogeochemist's knowledge of hydrological processes (flow rates as well as dispersive and diffusive mixing), reaction kinetics, mineral abundances, and the availability of surfaces and exchange capacities for sorption. Generally, the combined use of inverse and forward geochemical modelling will result in a better understanding of the essential data requirements; additional data and field observations are needed to improve the understanding of a groundwater system (Glynn and Plummer (2005) [15]). An iterative, progressively more informed process of data collection based on inverse and forward geochemical modelling, although not always practical, can provide an efficient framework for investigating groundwater systems.

NETPATH and PHREEQC (in inverse modelling mode) have many complementary capabilities, which may often argue for both codes being used together in trying to estimate a ¹⁴C model age. PHREEQC has the advantage of being able to consider uncertainties in 'initial' and 'final' solution compositions, as well as some additional mass and charge balance constraints (such as balances on individual valence states for various elements, water mole balance, individual solution charge balances, alkalinity balance) beyond those considered by NETPATH. NETPATH has the major advantage of solving the Wigley et al. (1978) [136] and Wigley et al. (1979) [147] isotope evolution equations, automatically (or manually if desired), calculating the relevant isotopic compositions of exsolving or precipitating phases, and allowing the straightforward calculation of ¹⁴C geochemical dilution adjustments (and A_o estimates following classical adjustment models). PHREEQC does not currently (2010) have these capabilities. Thorstenson and Parkhurst (2004) [155], however, calculated thermodynamically rigorous individual isotope equilibrium constants for common geochemical reactions and isotopes, and PHREEQC may eventually allow some automatic calculation of isotopic composition of exsolving phases in its forward modelling mode. PHREEQC forces mass balance constraints on all of the elements and redox states represented by given mineral reactions; in contrast, NETPATH allows one to use a subset of elemental and isotopic constraints. For a given set of aqueous solutions and chemical reactions postulated by the modeller and given uncertainty limits provided for various chemical and isotopic constituents (and pH) for each solution, PHREEQC will adjust 'initial' and 'final' solution compositions to satisfy individual solution charge imbalances, while minimizing the adjustments made. Similar to NETPATH, PHREEQC will also calculate all of the possible sets of reaction mass transfers and solution mixtures that can explain the evolution of the 'initial' waters into a 'final' water composition.

The modeller could combine the advantages of both codes through an iterative inverse modelling process: (i) using PHREEQC to calculate adjusted 'initial' and 'final' solution compositions; (ii) entering the adjusted solutions (and postulated reactions) in NETPATH; (iii) running NETPATH to calculate the isotopic compositions of exsolving or precipitating phases; (iv) entering those isotopic phase constraints back into PHREEQC; and (v) calculating new adjusted solutions in PHREEQC and iterating in this fashion until a suitable set of NETPATH reaction models is obtained with a reasonable ¹⁴C model age calculation. A new version of NETPATH, NetpathXL (Parkhurst and Charlton (2008) [156]) allows for the efficient combined use of a spreadsheet input data file for both codes, with minimal adjustment required to use either code. When developing inverse models in PHREEQC, there is an option to write all of the solution data as defined into a .lon file that can be read by NetpathXL. In addition, there is an option to write one .pat file and multiple .mod files (one for each model), which can be read by NetpathXL. The .pat file contains the solution compositions as adjusted by the inverse model, so it should be possible to run the exact PHREEQC model in NetpathXL to explore isotope compositions and ¹⁴C model ages. Recently, the IAEA developed a Windows based version of NETPATH (NETPATH-WIN and DB-WIN) that also permits spreadsheet input of data (El-Kadi et al. (2011) [157]).

Some of the modelling efforts and concepts described above were the focus of previous research efforts. Pearson (1992) [151] considered early on the possible effects of analytical uncertainties on the radiocarbon dating of groundwaters. In his approach to the issue, Pearson used a spreadsheet version of BALANCE (Parkhurst et al. (1982) [158]), a precursor code to NETPATH and a commercial

software code to automatically run a Monte Carlo distribution of a spectrum of inverse model simulations (with changing input solution compositions), and thereby obtain a range of ¹⁴C model ages. Cheng and Long (1984) [159] programmed a carbon isotope subroutine for the forward modelling code, PHREEQE (Parkhurst et al. (1980) [160]), that allowed for the simulation of chemical and carbon isotopic compositions along a postulated reaction path. Phillips et al. (1989) [39] used this capability in their investigation of radiocarbon dating for groundwater in the San Juan Basin of New Mexico. It is anticipated that many new numerical simulation tools will be developed in the future for the investigation of tracer model ages, following on these early starts and building on our current capabilities.

4.6.1. Some practical precautions and special cases in geochemical mass balance modelling

Inverse models (mass balance models) such as those produced in NETPATH and PHREEQC are combinations of masses of minerals and gases that must enter and/or leave (dissolve or precipitate) the initial water as it evolves chemically (and isotopically) to the final water. Each combination of phases and associated masses is a model, and exactly accounts for the change in moles of each element or isotope (selected as constraints) in the model between initial and final water. The model may include mixing with multiple waters in addition to calculated mass transfer and evaporation. As electrical neutrality is assumed, errors result if mass balance models are constructed between initial and final waters that do not balance in charge. This is particularly critical in radiocarbon dating in systems in which oxidation of organic carbon is considered. As phases are electrically neutral combinations of cations and anions, charge imbalance in the mass balance is (mathematically) left to the phases in the model that are not combinations of cations and anions, such as CO₂, CH₂O (a simplified formula for organic carbon of oxidation state zero) and CH₄. NETPATH has an option that, prior to solving the mass balance models, distributes the charge imbalance in proportion to the equivalents of cations and anions in initial and final waters. PHREEQC attains electrical neutrality through the adjustment of pH or the concentration of a selected ion. In general, it is best to construct geochemical models with complete chemical analyses.

Inverse geochemical models are not constrained by thermodynamics. Some models may be found that indicate dissolution of one or more phases for which thermodynamic analysis indicates the waters are oversaturated with the phase(s). Other models may require precipitation of a phase from undersaturated waters. Neither situation is possible and can be eliminated on the basis of thermodynamic infeasibility (Plummer (1985) [161]; Plummer et al. (1983) [148]). More common are mineral–water reactions in partial equilibrium systems (Helgeson (1968) [162]) in which one or more phases dissolve and one or more phases precipitate, some of which remain near thermodynamic equilibrium. Examples of partial-equilibrium chemical systems are provided in Plummer (1985) [161].

Individual inverse geochemical models may be found to be unreasonable for a wide variety of reasons, in addition to a lack of thermodynamic feasibility. Some models may indicate reaction mass transfers that are unrealistic given what is known regarding: (i) the kinetics of the reaction, (ii) the availability or concentration of a particular reactant, or (iii) the limited presence or absence of a particular reaction product. In addition, the ages calculated through inverse geochemical modelling may be unreasonable given the hydrological knowledge of a system, and could point to needed improvements in either the set of geochemical reactions considered to explain the observed evolution of the waters, or the possibility of additional hydrodynamic (and geochemical) processes. The calculation of a negative age for a groundwater sample is an obvious instance of such a discrepancy.

Any linear combination of 'end member' reaction models calculated by inverse modelling codes such as NETPATH or PHREEQC can potentially supply a mathematically consistent explanation of observed geochemical evolution in a groundwater system (Plummer et al. (1983) [148]). The possibility that a linear combination of unreasonable models, or of a mix of unreasonable and reasonable models, may be mathematically consistent with the observations is a troubling possibility that should
nevertheless be kept in mind when analysing reaction and inverse model possibilities for the purpose of radiocarbon dating in groundwater systems. The best way to avoid this conundrum is to obtain sufficient data regarding the chemical and isotopic composition of groundwater along a flow path, and to apply a sufficient number of constraints in inverse modelling to algebraically constrain the number of inverse models that can be calculated.

Recrystallization of carbonates is another important reaction that can greatly affect calculated ¹⁴C model age (Buddemeier et al. (1972) [163]; Garnier (1985) [164]; Mozeto et al. (1984) [165]). Recrystallization of calcite can be driven by small differences in Gibbs free energy between primary and secondary solids. The differences can result from trace impurities in the original calcite, such as Na and SO₄ in calcites of marine origin, that are released as the calcite recrystallizes into a more pure calcite in fresh water aquifers. Recrystallization can also be driven by differences in the surface free energy of physically damaged calcite in aquifers undergoing tectonic stress or in carbonate minerals crushed by the scouring of glaciers. In NETPATH, it is possible to specify the moles of a carbonate mineral that exchange isotopically with a kilogram of water. An indication that calcite recrystallization may be occurring in carbonate groundwater systems is the observation that $\delta^{13}C_{DIC}$ (measured) > $\delta^{13}C_{DIC}$ (modelled). Unfortunately, other uncertainties in the model can lead to the same observation, such as uncertainty in the isotopic composition of reactants or failure to consider all possible reactants.

4.7. EXAMPLES USING NETPATH

In many aquifers, reliable radiocarbon ages have been interpreted by using the traditional adjustment models described above. These tend to be aquifers where the processes of carbonate mineral dissolution and isotopic exchange processes of CO_2 and calcite dominate the recharge process and evolution in the system. Similar results can be obtained by using NETPATH in these systems. For



FIG. 4.6. Location of the regional confined Alliston aquifer, southern Ontario, Canada (from Aravena et al. (1995) [166]).

example, the initial water could be chosen as precipitation and the final water as a groundwater sample from the recharge zone.

Here, two examples are considered where geochemical modelling was essential in interpreting ¹⁴C model age. The first example involves the Alliston aquifer of Ontario, Canada, where palaeorecharge in glacial drift has undergone extensive interaction with buried organic matter in the methanogenic sediment (Aravena et al. (1995) [166]). In the second case, radiocarbon dating of water in the Floridan aquifer, FL, USA, undergoing de-dolomitization (dolomite and gypsum dissolution with calcite precipitation), oxidation of organic carbon (with iron reduction, sulphate reduction, pyrite formation), mixing with old saline water and recrystallization of marine calcite is considered (Plummer and Sprinkle (2001) [135]).

4.7.1. Alliston Aquifer System, Ontario, Canada

Aravena et al. (1995) [166] present chemical and isotopic data from groundwater in the Alliston aquifer (Fig. 4.6), a regional confined aquifer in southern Ontario, Canada, composed of sand and gravel lenses. The aquifer is confined above by a thick glacial till and below by Palaeozoic bedrock or by early Wisconsin glacial till. The water chemistry was predominantly $Ca-Mg-HCO_3^-$ type in the recharge



FIG. 4.7. Regional groundwater flow pattern (arrows), potentiometric contours (feet above sea level; 1 ft = 0.3048 m) and sampling sites in the Alliston Aquifer (from Aravena et al. (1995) [166]).

areas. Concentrations of HCO_3^- , Na, Cl, DOC and CH_4 increased along directions of groundwater flow, while concentrations of NO₃ and SO₄ decreased (to below detection in some cases).

Concentrations of dissolved carbon species in the Alliston aquifer were 169–428 mg/L HCO₃, 2.0–18 mg/L DOC and <10 to 3550 μ mol/L CH₄. The ¹⁴C content of DIC ranged from 0.7 to 63.8 pmc and $\delta^{13}C_{\text{DIC}}$ ranged from –12.7 to +2.0‰ in the Alliston aquifer. Aravena et al. (1995) [166] applied NETPATH to calculate ¹⁴C model ages in the Alliston aquifer. Several representative initial waters were selected and, because these waters contained bomb tritium, A_{oTDC} (TDC = DIC + DOC + CH₄) was computed based on the Tamers, Pearson, Fontes and Garnier, and Eichinger models, and A_{oTDC} was estimated from the available data. The data and model results are provided in Aravena et al. (1995) [166]. One example is the evolution of water from well OV29 in the recharge area to well OV49 further down gradient along flow path 2 (Fig. 4.7):

$$OV29 + 5.59 CH_2O + 0.12 NaCl + 0.22 dolomite + 0.99 goethite + 0.69 Na_2X \rightarrow 0.05 calcite + 0.79 siderite + 0.63 pyrite + 0.69 CaX + OV49$$
(4.49)

where CH_2O refers to sedimentary organic carbon of oxidation state 0, and masses of reactions are in millimoles per litre. The models were corroborated by close agreement in modelled and measured $\delta^{13}C$ of TDC. The unadjusted ¹⁴C model age was 15.1 ka. By using data on the $\delta^{13}C$ and ¹⁴C content of DIC, DOC and CH_4 measured in the groundwater samples, the adjusted ¹⁴C model age of TDC ranged from



FIG. 4.8. Location of wells sampled and flow paths I-V in relation to altitude of the pre-development potentiometric surface of the Upper Floridan aquifer. Contours in feet (1 ft = 0.3048 m; from Plummer and Sprinkle (2001) [135]).

5.5 to 5.8 ka at well OV49. Overall, two groups of waters were found in the Alliston aquifer — one group of waters has ¹⁴C model ages of less than 13 ka, and the other group has ¹⁴C model ages between 15 and 23 ka. The ¹⁴C model age range calculated by NETPATH was in agreement with the age range based on DOC age correction models (Aravena and Wassenaar (1993) [167]).

4.7.2. Floridan Aquifer System, FL, USA

Plummer and Sprinkle (2001) [135] applied geochemical modelling techniques to improve radiocarbon dating of DIC in the Floridan aquifer system, FL, USA. Water samples were obtained along five general directions of groundwater flow, based on the shape of the pre-development potentiometric surface (Fig. 4.8).

By using NETPATH, the predominant geochemical reactions that affect the ¹⁴C content of the DIC were: (i) dissolution of dolomite and anhydrite with accompanying calcite precipitation (de-dolomitization); (ii) sulphate reduction accompanying microbial degradation of sedimentary organic matter; (iii) recrystallization of calcite; and (iv) mixing of fresh water with as much as 7% saline water in some coastal areas. None of these processes/reactions are accounted for by any of



FIG. 4.9. Distribution of cumulative mass of calcite recrystallized (mmols/kg water; from Plummer and Sprinkle (2001) [135]).

the traditional inorganic adjustment models. As an example, a representative net geochemical reaction along flow path III was:

water I.1 + 0.57 dolomite + 1.71 anhydrite + 0.48 CH₂O + 0.12 goethite + 5.5 calcite_(primary) + 1.78 Na₂X + 0.53 sea water \rightarrow 0.95 calcite + 5.5 calcite_(secondary) + 1.78 CaX + 0.12 pyrite + 0.38CO₂ + water III.5 (4.50)

The part of the overall reaction pertaining to calcite recrystallization:

5.5 mmol/L calcite_(primary)
$$\rightarrow$$
 5.5 mmol/L calcite_(secondary) (4.51)

represents recrystallization of an estimated mass of 5.5 mmols of calcite (of marine origin, $\delta^{13}C_{\text{calcite}} \equiv 0\%$) per litre of aquifer, to form 5.5 mmols of secondary calcite (accounting for isotopic fractionation in calcite precipitation) in fresh water. One of the findings from the NETPATH modelling was that without calcite recrystallization, the modelled values of $\delta^{13}C_{\text{DIC}}$ were significantly depleted in ¹³C. The millimoles per kilogram of water of calcite recrystallization needed in the NETPATH models to match the observed $\delta^{13}C_{\text{DIC}}$ were estimated and plotted on a map (Fig. 4.9). The estimated masses of recrystallization increased near the ends of flow paths and were attributed to geochemical interactions caused by upward leakage from the Lower Floridan aquifer, through semi-confining layers, and discharge into the Upper Floridan aquifer. During recrystallization, a fractionation occurs (Appendix to Chapter 4) that enriches the secondary calcite with ¹⁴C from the DIC, lowering the ¹⁴C content of



FIG. 4.10. Comparison of ¹⁴C model ages calculated for dissolved inorganic carbon from 24 water samples from the Upper Floridan aquifer, Florida as (i) unadjusted age, (ii) adjusted age based on the model of Fontes and Garnier (1979) [116], and (iii) adjusted age calculated using NETPATH (from Plummer and Sprinkle (2001) [135]).



FIG. 4.11. Distribution of NETPATH adjusted ¹⁴C model ages of DIC in groundwater from the Upper Floridan aquifer, FL, USA (from Plummer and Sprinkle (2001) [135]).

DIC in dissolved HCO₃. Therefore, recrystallization of calcite lowers the value of A_{nd} and, thus, lowers the adjusted radiocarbon age.

Figure 4.10 compares the unadjusted ¹⁴C model age for waters along the five flow paths with the ¹⁴C model ages calculated from application of the Fontes and Garnier (1979) [116] model to the final water, and the NETPATH calculated ¹⁴C model ages, which include the geochemical mass balance models with calcite recrystallization.

Most of the waters outside of the recharge area had adjusted ¹⁴C model ages of 20-30 ka (Fig. 4.11).

The measured ¹⁴C values of DIC in the Floridan aquifer were low, and varied from about 33 pmc in the recharge area to as low as 0.23 pmc on flow path III. Along the same flow direction, $\delta^{13}C_{DIC}$ increased from -11.4 to -2.5%. Unadjusted ¹⁴C model ages ranged from about 9 to more than 50 ka. The calculated ¹⁴C model ages using NETPATH ranged from 1.4 to about 27 ka (Plummer and Sprinkle (2001) [135]).

4.8. RADIOCARBON DATING OF DISSOLVED ORGANIC CARBON

Owing to the many geochemical interactions that can lower the ¹⁴C content of DIC and, if not quantified, limit the usefulness of radiocarbon dating of DIC in groundwater, the feasibility of radiocarbon dating of DOC in groundwater was investigated in a series of studies (Drimmie et al. (1991) [168]; Hendry and Wassenaar (2005) [169]; Long et al. (1992) [170]; Murphy et al. (1989) [171]; Murphy et al. (1989) [172]; Purdy et al. (1992) [173]; Tullborg and Gustafsson (1999) [174]; Wassenaar et al. (1989) [175]; Wassenaar et al. (1991) [176]). A generally accepted definition of DOC is organic carbon that passes through a 0.45 μ m filter (Drever (1997) [177]). Groundwater typically contains less than 2 mg/L (as C) of DOC with a median concentration of about 0.7 mg/L (Leenheer et al.

(1974) [178]). With the development of ¹⁴C AMS analysis, radiocarbon dating of DOC in groundwater is possible, although relatively large volumes of water (100–200 L) are needed to extract and separate high molecular weight (HMW) and low molecular weight (LMW) fractions of DOC (Murphy et al. (1989) [171]; Murphy et al. (1989) [172]). Although radiocarbon dating with DOC can avoid many of the geochemical complications that affect the ¹⁴C content of DIC, research over the past two decades has shown that two of the problems that affect radiocarbon dating of DIC must also be evaluated in radiocarbon dating of DOC; namely, definition of the initial ¹⁴C value of DOC, $A_{o(FA)}$, where FA refers to the fulvic acid (HMW) fraction, and adjustment of $A_{o(FA)}$, to $A_{nd(FA)}$, for additional sources of (usually old) fulvic acid within the aquifer.

There are two main sources of DOC in groundwater: (i) particulate organic carbon (POC) in the soil zone and unsaturated zone that can have radiocarbon ages of zero to at least several thousand years; and (ii) sedimentary organic matter (SOM) such as lignite, peat or other forms of POC buried with the aquifer sediment that typically is radiocarbon-'dead'. Both sources of DOC can dilute the ¹⁴C content of DOC in an aquifer.

Biogeochemical processes also significantly lower DOC concentrations across unsaturated zones (Pabich et al. (2001) [179]). Loss of DOC during the recharge process does not, alone, complicate the definition of $A_{o(FA)}$. The problem is that within the soil zone and unsaturated zone, POC is not all modern and the assumption of 100 pmc for $A_{o(FA)}$ is usually not valid. Little is known about the rates of the complex series of biogeochemical processes that alters POC in soil zones, so that modelling of $A_{o(FA)}$ is currently not possible. The alternative is to measure $A_{o(FA)}$ in recharge waters of aquifers. One of the problems is that there is a spectrum of ¹⁴C values corresponding to the distribution of organic species and molecules recharging the groundwater system; generally, the 'younger' species will preferentially degrade (through fermentation or oxidation processes) relative to the 'older' species. Consequently, the distribution of ¹⁴C abundance, even in the absence of radioactive decay.

Methods of separating HMW and LMW fractions of DOC are provided in Thurman and Malcolm (1981) [180], Murphy (1987) [181], Murphy et al. (1989) [171] and Murphy et al. (1989) [172]. The HMW fraction is composed primarily of fulvic acids with a molecular weight range of 500–950 amu (Aiken and Malcolm (1987) [182]), whereas the LMW fraction consists primarily of short chain aliphatic hydrocarbons and substituted alcohols (molecular weight of <140 amu). Murphy et al. (1989) [172] found large and varying differences in the ¹⁴C content of the HMW and LMW fractions of DOC in individual samples from the Milk River aquifer, Canada, demonstrating the diverse origin of DOC in the aquifer and showing that radiocarbon dating of a composite DOC sample (HMW + LMW fractions) could be misleading. In the Milk River aquifer, LMW compounds generally had low ¹⁴C content, suggesting dilution with LMW DOC from ¹⁴C-'dead' kerogen within the aquifer. The ¹⁴C content of the HMW DOC generally followed that of the DIC, supporting a predominantly soil origin of the fulvic acid fraction (Murphy et al. (1989) [172]). Although the HMW (fulvic acids) DOC fractions are also mixtures of organic molecules of different age, they are thought to be predominantly of soil origin (Murphy et al. (1989) [172]) and probably better suited for radiocarbon dating than composite DOC or the LMW fraction of DOC (Clark and Fritz (1997) [52]).

Wassenaar et al. (1991) [176] found ¹⁴C values of the HMW fraction of DOC decreased in young, tritiated recharge waters of the Sturgeon Falls aquifer and Rodney aquifer in western Canada to 75 and 76 pmc, respectively at depths of 16–18 m. The ¹⁴C content of the HMW fraction of DOC ranged from 99 to 87 pmc in recharge waters from the Alliston aquifer (Canada), where the highest value was from a depth of 16–18 m and may have contained a higher fraction of DOC in recharge water from the Milk River aquifer was estimated to be as low as 30 pmc (Drimmie et al. (1991) [168]; Wassenaar et al. (1991) [176]). Measurements from a clay rich till aquitard system in Canada demonstrated that the ¹⁴C of the HMW fraction of DOC decreased from 97 pmc at depths of 1.2 m to 13–15 pmc at depths of 15–43 m (Hendry and Wassenaar (2005) [169]). The trend with depth was consistent with diffusive mixing

between two distinct end members: SOM formed since the Holocene (past 10 ka) and DOC in pore fluids of the aquitard (Hendry and Wassenaar (2005) [169]) suggesting, at least in this environment, that the HMW and LMW fractions of DOC were geochemically and biochemically conservative.

In studies where the ¹⁴C of DIC and DOC (or of the HMW fraction of DOC) are measured, the ¹⁴C content of DIC is usually significantly lower than that of the DOC (or of the HMW fraction of DOC) (Buckau et al. (2000) [183]; Burr et al. (2001) [184]; Drimmie et al. (1991) [168]; Murphy et al. (1989) [171]; Pettersson and Allard (1991) [185]; Purdy et al. (1992) [173]; Wassenaar et al. (1991) [176]). The differences can be attributed to the relatively large number of geochemical reactions (as well as other processes such as matrix diffusion and isotopic exchange) that can lower the ¹⁴C content of DIC in old groundwater. The two most significant geochemical processes are dilution of dissolved inorganic ¹⁴C (DI¹⁴C) from dissolution of carbonates and formation of DIC from microbial degradation of old organic carbon within the aquifer. Thomas et al. (2001) [186] found unadjusted ¹⁴C model ages of DIC in groundwater from Nevada as much as 20 ka, that, when corrected on the basis of δ^{13} C for carbonate rock recrystallization in this tectonically active aquifer, were in the range of 1–7 ka and similar to ¹⁴C model ages of DOC in the aquifer.

Although 'traditional' adjustment models adequately compensate for carbonate mineral dissolution, most studies comparing DO14C and DI14C ages have not evaluated the organic source of DIC. Geochemical models used to adjust the initial ¹⁴C value that included the degradation of organic matter in the aquifer (Aravena et al. (1995) [166]; Plummer (1993) [60]; Plummer et al. (1990) [145]; Plummer and Sprinkle (2001) [135]) yielded adjusted radiocarbon ages of DIC that were 'reasonable'; i.e. consistent with other palaeoclimate indicators (stable isotopes and palaeorecharge temperatures) or with results from numerical flow models. Buckau et al. (2000) [183] applied 'traditional' adjustment models to the DIC of the Gorleben aquifer, Germany, finding ¹⁴C model ages of 1-10 ka in tritiumcontaining recharge water, and DIC ¹⁴C model ages up to 31 ka in waters that had Holocene stable isotope signatures. By taking into account dilution of the DIC from microbial degradation of DOC in the aquifer, and determination that $A_{o(DIC)}$ in the aquifer was near 50 pmc, Buckau et al. (2000) [183] demonstrated that the waters that contained elevated concentrations of DOC were so young that significant ¹⁴C decay could not be detected, and that the ages were consistent with the age limits derived from ²H and ¹⁸O. Buckau et al. (2000) [187] demonstrate the release of large concentrations of LMW (1.7–171 mg C/L) and HMW (2.6–22 mg C/L) DOC fractions in waters of the Gorleben aquifer compared to the relatively low DOC concentrations in the recharge waters (0-2.2 mg C/L). The contribution of DOC from sedimentary organic matter in the Gorleben aquifer overwhelms the initial DOC fractions, demonstrating the difficulty of dating DOC in organic rich aquifers. The next important advance in the application of radiocarbon dating of DOC in groundwater will likely be in the field of compound specific radiocarbon dating (Ingalls and Pearson (2005) [188]; Kalin (1999) [111]).

Long et al. (1992) [170] suggested that the most important justification for the study of ¹⁴C of DOC in aquifers is for comparison with travel times inferred from ¹⁴C in DIC. Differences in ¹⁴C model ages between DIC and DOC can aid in refining geochemical adjustment models of the ¹⁴C content of DIC as well as help to interpret the ¹⁴C content of DOC in aquifers. A useful approach to establishing radiocarbon chronologies in aquifers where inorganic and organic carbon sources contribute to the ¹⁴C DIC pool is to date the DIC. This is done by constructing geochemical adjustment models accounting for all of the predominant inorganic and microbially mediated organic degradation reactions in the TDC system, such as implemented in NETPATH (Plummer et al. (1994) [120]), and demonstrated by Aravena et al. (1995) [166] and Plummer and Sprinkle (2001) [135].

4.9. HYDRODYNAMIC AND AQUIFER MATRIX EFFECTS ON RADIOCARBON AGES

4.9.1. Mixing processes

Groundwater pumping extracts water preferentially from the most hydraulically conductive zones adjacent to well screens. This means that the waters extracted and their solutes, including DIC and DOC, generally come preferentially from one or more transmissive aquifers, transmissive zones or from highly conductive fractures. It is important, however, to consider the spatial scale of the effects of groundwater pumping and movement. In a study investigating regional groundwater depletion, Konikow and Neuzil (2007) [189] showed that most of the regional groundwater depletion caused by pumping actually came from a change in storage in confining layers. Thus, a significant fraction of a water sample pumped from a well may represent water that has not only been residing in 'mobile' zones of the groundwater system. Some of the water may have leaked from/through confining layers. If the leakage occurs primarily from more recently recharged (usually shallower)² horizons, the water sample will contain a fraction of younger water and, possibly, younger solutes. If the leakage occurs primarily from less recently recharged (usually deeper) horizons, the water will contain a fraction of older water and older solutes. In general, water samples extracted from given horizons will have a frequency distribution of water and tracer model ages (cf. review by Bethke and Johnson (2008) [84]; Chapter 3 in the present volume discusses this issue at length and how it affects groundwater 'age' concepts). This natural range in age distributions can be coupled with the following facts: (i) different solutes undergo different types and extents of reaction and, therefore, undergo varying extents of retardation in groundwater systems (Atteia et al. (2005) [190]; Glynn and Brown (2012) [154]; Maloszewski and Zuber (1991) [191]); (ii) different solutes have different histories of recharge into the groundwater system (Plummer et al. (1993) [192]), as well as different production and removal histories in their passage through the system; and (iii) different solutes may even have undergone different extents of dispersal and/or exclusion through the system (LaBolle et al. (2006) [193]; Neuzil (1986) [194]; Neuzil and Provost (2009) [195]). Consequently, it is no surprise to find that different dating techniques provide different tracer model ages for a given sample (see DePaolo (2006) [196]; IAEA (2006) [85]; Maloszewski and Zuber (1991) [191]; Plummer et al. (1993) [192]).

4.9.2. Subsurface production

The possibility of subsurface production of ¹⁴C was investigated by Zito et al. (1980) [197] and with regard to the Stripa granite by Andrews et al. (1989) [198]. Although it is theoretically possible to produce ¹⁴C in groundwater from nuclear reactions induced by emissions from U and Th nuclei, the effect is normally not important in waters younger than 50 ka (Zito et al. (1980) [197]), which is approximately the limit for ¹⁴C dating. The minimum ¹⁴C content from in situ production in the Stripa fracture fluids corresponded to a decay time of 32 ka, for an initial ¹⁴C value of 50 pmc. However, the question of in situ production of ¹⁴C would need to be investigated on a site specific basis and depends on several factors, including the localization of U- and Th-bearing minerals with respect to pore spaces and various target materials (Al, Mg, O, Si, B) in the aquifer (Zito et al. (1980) [197]).

4.9.3. Diffusive exchange with confining layers

In addition to the possible advective leakage of waters from other conductive zones of a groundwater system (through confining zones), diffusive exchange of water and solutes is also an

 $^{^2}$ One exception may occur when shallow, relatively less transmissive zones overlie deeper relatively more transmissive zones. In this situation, waters in the deeper zones may have been more recently recharged than waters in the shallower zones.

important process to consider. Any groundwater system may have a range of 'stagnant'³ zones, typically containing old water and solutes which can possibly exchange diffusively with younger water and solutes in more mobile regions of the system. Large chemical and isotopic concentration gradients are often found between mobile and stagnant zones in groundwater systems, with stagnant zones usually containing more highly concentrated, sometimes more chemically reducing waters. A wide range of stagnant zones can occur: confining beds or aquitards, clay or silt lenses, unfractured rock matrices with some connected porosity between mineral grains, connected porosity inside individual mineral grains, and internal exchange layer porosity in clay minerals. Many of the diffusion processes will involve aqueous ion diffusion through a water phase, although this phase can have varying electrochemical properties because of interfacial effects with the contacting solid surfaces. Some of the diffusion can also occur through surface diffusion processes, including surface diffusion inside the double layer of clays (Helfferich (1995) [199]). Atteia et al. (2005) [190] offer a comprehensive review examining the contributions of diffusion and leakage from low permeability layers to the geochemical evolution of groundwater systems.

4.9.4. Transport models

Ideally, the complex interplay between advective, dispersive and diffusive processes, geochemical reactions and radioactive decay (or production) would be investigated using forward-modelling reactive transport codes such as PHAST (Parkhurst et al. (2004) [200]). Owing to the multiplicity of possible computer intensive simulations varying parameters, processes and configurations, inverse modelling is needed to constrain the range of possible simulations and optimize parameter values (for given configurations and processes chosen for a particular system). Inverse modelling could include inverse geochemical modelling with NETPATH/PHREEQC to determine sets of possible reactions and mixing processes that might control the geochemical evolution of the groundwater. Inverse modelling with codes such as UCODE (Poeter and Hill (1998) [74]) could also be used to estimate and constrain flow and transport models and model parameters. Having sufficient high quality data and an understanding of what is reasonable in the hydrological and geochemical behaviour of a system would be key to the useful application of the modelling process.

4.9.5. Analytical solutions

In the absence of full featured but time consuming inverse and forward simulations of groundwater systems, some analytical solutions are available that can quickly quantify the potential importance of diffusive processes on observed radiocarbon ages for given groundwater samples. The solutions were first derived for the study of radionuclide transport in fractured rocks, initially for the transport of a radionuclide through a single fracture with transverse diffusion into a rock matrix (Neretnieks (1980) [201]; Neretnieks (1981) [202]; Tang et al. (1981) [203]), then for transport through a parallel set of fractures with transverse diffusion into the intervening rock matrix (Sudicky and Frind (1982) [204]; Sudicky and Frind (1984) [205]). A more general 3-D analysis for fractured rock media was provided by Therrien and Sudicky (1996) [206]. Although Tang et al. (1981) [203] recognized early on the application of their analytical solution to radiocarbon dating of groundwater in a thin aquifer bounded by thick confining beds, Sanford (1997) [207] provided an elegant analytical derivation and solution for a parallel series of stagnant and flow zones, applicable either for porous or fractured rock media. The basic equations in Sanford (1997) [207] for the analytical solution under steady-state conditions

³ Historically, hydrologists have often considered low permeability zones as zones that were completely impervious to flow, such as aquicludes, for example. In reality, advective flow generally does occur through low permeability zones and, more often than not, can be quantitatively meaningful when integrated over large regional areas and/or over large timescales. In this chapter, 'stagnant' zones is simply used to indicate zones for which diffusive transport processes dominate over advective ones over the time periods and areas of interest.

(with respect to both flow and transport) of a parallel flow and stagnant zone system, with a constant tracer input concentration (e.g. a ¹⁴C content of 100 pmc), constant flow zone width, w_{flow} , and constant stagnant zone width, w_{stag} , are further discussed in recent papers by Cook et al. (2005) [208] and DePaolo (2006) [196]. Sanford's steady state solution can take the form of a diffusion loss constant that can be added to the radioactive decay constant for a given tracer such as ¹⁴C. Sanford relates the diffusion corrected, t_c , and diffusion uncorrected, t_u , ages for a sample through the following equation:

$$t_{\rm c}/t_{\rm u} = k/(k + k_{\rm diff}) \tag{4.52}$$

where k and k_{diff} are the radioactive decay and diffusive loss constants, respectively. For ¹⁴C, k is 1.21×10^{-4} per a or 3.83×10^{-12} per s (corresponding to a half-life of 5730 a). The diffusive loss constant, k_{diff} , can be calculated from the following equation:

$$k_{\rm diff} = \frac{2\sqrt{kD_{\rm eff}}}{\varphi w_{\rm flow}} \tanh\left(\frac{w_{\rm stag}}{2}\sqrt{\frac{k}{D_{\rm eff}}}\right)$$
(4.53)

where

 φ is the porosity in the flow zone; and the effective diffusion coefficient, D_{eff} , can be related to the aqueous diffusion coefficient, D_0 , through a variety of equations that generally include the effects of matrix (or stagnant zone) porosity, θ_{stag} , and tortuosity, τ .

These equations and the magnitude of D_{eff} vary significantly in different studies. Cook et al. (2005) [208] provide a fairly general formulation:



FIG. 4.12. Plot of the ratio of the diffusive rate constant, k', to the decay constant of 14 C, k, over the length scales at which vertical heterogeneties occur in porous media. Shaded regions indicate where diffusion is either negligible (white), significant (pale yellow) or dominant (pink). The ratios assume a porosity of the flow zone of 0.30, a coefficient of molecular diffusion of $1 \times 10^{-10} \text{ m}^2/\text{s}$, and a decay constant of $3.83 \times 10^{-1}/\text{s}$ (modified from Sanford (1997) [207]). Sanford's analytical solution and the adjacent plot will generally tend to an overestimation of the effects of ${}^{14}\text{C}$ diffusive loss on ${}^{14}\text{C}$ model ages as discussed in the text.

$$D_{\rm eff} = D_0 \theta_{\rm stag} \tau$$

The aqueous diffusion constant, D_0 , for carbonate and bicarbonate species is variously cited: 0.04 m²/a ($1.3 \times 10^{-9} \text{ m}^2/\text{s}$) by Cook et al. (2005) [208], and 0.03 m²/a ($9.5 \times 10^{-10} \text{ m}^2/\text{s}$) by DePaolo (2006) [196], who may be including a tortuosity effect in his lower number. In their example describing a fractured rock system, however, Cook et al. (2005) [208] assumed a tortuosity of 0.03 and a matrix porosity of 0.02. Porous media have higher stagnant-zone porosity and tortuosity compared to fractured rock matrices. This explains the two orders of magnitude difference in the effective ¹⁴C diffusivities (D_{eff}), $10^{-10} \text{ m}^2/\text{s}$ and $7.6 \times 10^{-13} \text{ m}^2/\text{s}$, used by Sanford (1997) [207] and Cook et al. (2005) [208], respectively.

Sanford used his steady state model calculations to estimate the effect of diffusive loss on radiocarbon dating of waters in the stratified basalts of the island of Oahu, where he calculated that the diffusive losses of ¹⁴C could result in a ¹⁴C model age that could be 100 times too old. He also applied his model to ¹⁴C dating of waters in the Bangkok Basin, an alluvial system of stratified clay, sand and gravel lenses, where he estimated the near equal removal of ¹⁴C through radioactive decay and diffusive loss. His calculations assumed that the clay lenses had an average thickness of about 6 m, and that the transmissive sand layers had a thickness of about 20 m. Figure 4.12 (from Sanford (1997) [207]) can be used to estimate the relative importance of diffusive ¹⁴C loss in radiocarbon dating.

It must be noted that Sanford's analytical solution did not consider the possibility of sorption and isotope exchange with the solid phase, a process that can be important in carbonate (limestone, dolomite) or chalk aquifers. Małoszewski and Zuber (1991) [191] added these processes in their own analysis of diffusive effects on radiocarbon dating. The additional retardation caused by the sorption and exchange of ¹⁴C leads to additional decay and loss of the isotope, even in a steady state system. In contrast to this loss, the concentrations of non-decaying constituents, such as ¹³C, are not affected by sorption and exchange processes under steady state conditions. However, groundwater systems are probably never in complete steady state with respect to all transport processes and geochemical reactions.

Sanford's analytical solution assumes steady state conditions and may either overestimate or underestimate diffusive losses of ¹⁴C in groundwater systems with changing flow and transport conditions. Sanford's analytical solution may provide a good estimate of ¹⁴C diffusive loss (and the needed groundwater age correction) in the case of parallel transmissive and stagnant zones, where the water in the stagnant zones is truly stagnant. Generally, however, Sanford's analytical solution may tend to overestimate the diffusive losses of ¹⁴C for the following reasons:

- (a) The solution assumes a binary layer flow system, with fast flow zones and stagnant zones. Advection is a non-fractionating transport process. By assuming that advection is insignificant in stagnant zones, the diffusive loss of ¹⁴C in those zones is maximized.
- (b) The solution assumes a 'layer-cake' alternating distribution of flow and stagnant zones, with one constant width for the flow zones and one constant width for the stagnant zones, and a diffusive gradient into the stagnant zones orthogonal to the flow direction in the flow zones. In contrast, stagnant zones in alluvial basins are likely to pinch out and be limited in areal extent. If the lenticular stagnant zones are small in their individual areal extents, diffusion into the lenses may be fast enough that no significant ¹⁴C decay will occur. Therefore, the 'layer-cake' configuration assumed by Sanford's analytical solution likely overestimates ¹⁴C diffusive losses in systems that have stagnant zones with very limited individual areal extents.
- (c) The solution assumes that transverse dispersion is great enough in the flow zones to ensure a constant ¹⁴C content across the width of each flow zone. In systems with large flow zones, such as thick aquifers, this may not be the case and this could limit the overall diffusive loss of ¹⁴C.
- (d) The solution assumes that Fick's law, as applied only to the ¹⁴C content in the water, controls the diffusion and the diffusive loss of ¹⁴C. It assumes that the chemical counter diffusion of ions from stagnant zones into flow zones does not affect ¹⁴C diffusion. In reality, major regional

aquitards often have significantly different chemistry from their neighbouring aquifers and are usually more saline. In such systems, coupled diffusion processes might have to be taken into account. Multicomponent diffusion is a complex process that can speed up the diffusion of certain ions and slow the diffusion of others, relative to the diffusive flux that might be calculated by assuming single ion diffusion. However, in the common case of stagnant zones that are significantly more saline than the flow zone of interest, intuition suggests that strong chemical counter diffusion fluxes of ions into the flow zone could potentially slow the diffusive flux and loss of ¹⁴C into the stagnant zones, relative to the ¹⁴C loss that might occur in a situation without a strong chemical counter diffusion.

In summary, Sanford's analytical solution is a useful tool for an initial estimation of potential ¹⁴C diffusive losses. However, it probably provides a maximum estimate of such losses, and is best applied to systems that have pervasive zones with no significant advective flow. It will probably not be applicable to alluvial basins with relatively coarse sediments and a paucity of truly stagnant zones, such as the Middle Rio Grande and San Juan Basins in New Mexico. After an examination of the geological information available for the Middle Rio Grande Basin, Sanford et al. (2004) [47] and Sanford et al. (2004) [48] did not correct ¹⁴C model ages for diffusive losses in that basin. In their study on the San Juan Basin, Phillips et al. (1989) [39] considered the potential effects of dispersive mixing and, more importantly, inter-aquifer leakage, on the sampled groundwater ¹⁴C model ages; they concluded that these effects did not significantly affect the estimated ¹⁴C model ages.

4.9.6. Matrix diffusion in unsaturated zones

Most of the studies that have investigated the effects of matrix diffusion on ¹⁴C dating of groundwater have considered only the effects that occur below the water table. There could be some situations in which the physical and chemical processes relating to diffusion, sorption, isotopic exchange and decay of ¹⁴C in matrices, lenses or grain pores in the unsaturated zone or near the water table might also need to be considered, even though the effects could be mitigated by gas phase exchange processes. Diffusive processes in the unsaturated zone or in perched groundwater could potentially lower the initial ¹⁴C content, A_0 , of recharging groundwater.

4.9.7. General conclusions regarding the effects of hydrodynamics and heterogeneity on ¹⁴C model ages in groundwater

Some general conclusions can be stated regarding the effects of matrix diffusion on ¹⁴C dating of groundwater. Most groundwater sampled for ¹⁴C analysis and radiocarbon dating is pumped from the more transmissive zones of a groundwater system. Owing to dispersive and diffusive effects (and usually their associated geochemical reactions), the groundwater flow rates obtained by using the ¹⁴C model ages estimated⁴ for these transmissive zones will underestimate the actual groundwater velocities in these zones. Further, the flow rates obtained will probably greatly overestimate the mean water velocity of the system as a whole (because the sampled water may not fully reflect the slower velocities and older ages of water in less transmissive zones). Consequently, if a system is at steady state, overall recharge to the system⁵ will be overestimated if the recharge rate is determined from ¹⁴C measurements insufficiently corrected for diffusive processes. From a water management perspective, the underestimation of water velocities in transmissive zones could cause a problem if water contamination is an issue; the overestimation of overall recharge to the system from a water supply perspective.

⁴ Without corrections for diffusion.

⁵ The system, as defined here, is the entire groundwater system. It includes all of its transmissive, less transmissive and stagnant zones.

The geometry and distribution of more transmissive and less transmissive, and/or stagnant zones will be important in determining the relative effects of diffusive processes (and of advective leakage). The relative sizes of stagnant and transmissive zones will matter as can be seen from the equations above. The orientation and aspect ratio of the zones relative to the recharge surface, and the distribution of these orientations and geometries will also be important. The use of multiple tracers with different effective diffusivities and decay or growth characteristics can potentially provide a better understanding of the distribution of model and actual groundwater velocities through the system.

Simple, easy to use, estimation techniques and numerical modelling tools are useful and needed to obtain a good understanding of the geochemical and hydrological processes occurring in aquifers and their potential impacts on the distribution of ¹⁴C content throughout a groundwater system. Ultimately, however, the heterogeneous nature and the structural and process complexity of groundwater systems may require more sophisticated full-featured numerical simulation tools. The full use of these tools, however, will be warranted only when there is sufficient information and data available to describe the groundwater system under investigation. In such a situation, ¹⁴C age dating may be used in conjunction with the chemical and isotopic characterization of various recharge and evolved waters, and the spatial delineation of their occurrence, to help calibrate full featured flow and transport simulations of a groundwater basin. Plummer et al. (2004) [49], Plummer et al. (2004) [50], Plummer et al. (2004) [51], Sanford et al. (2004) [47] and Sanford et al. (2004) [48] provide an example of such an application in an investigation of the hydrogeology of the Middle Rio Grande Basin (see Chapter 12 for a case study on the Middle Rio Grande Basin). Their study calculated the effective modern and palaeorecharge rates for the basin. The minimal corrections needed to adjust for ¹⁴C dilution through geochemical reactions in the Middle Rio Grande Basin, and the extensive geochemical and hydrological data available were a great help in facilitating calibration of the flow model for the system. Several earlier efforts have also used radiocarbon dating, measured ¹⁴C values and geochemical modelling, to help determine regional recharge rates and the transmissivity of aquifers on large regional scales. Some notable examples of such studies include Phillips et al. (1989) [39], Plummer et al. (1990) [145], and Plummer and Sprinkle (2001) [135]. In these efforts, the collection of an extensive set of chemical and isotopic analyses was often the key to obtaining confidence that calculated tracer model ages or velocities were reasonable. In the best situations, the ages obtained correlated with recharge palaeotemperatures derived from noble gas, N_2/Ar , ¹⁸O and ²H data.

4.10. GUIDELINES FOR RADIOCARBON DATING OF DISSOLVED CARBON IN GROUNDWATER SYSTEMS

Nine guidelines essentially decribe the application of radicarbon measurements to groundwater dating:

(1) Although it is sometimes possible to reconstruct the ¹⁴C content of DIC in water samples that are mixtures of young and old water, it is best to attempt radiocarbon dating on waters that are representative of in situ aquifer conditions. Well construction and/or drilling practices can compromise the integrity of the ¹⁴C content of the formation water. Tritium analyses and CFC analyses are useful in recognizing water samples or their mixtures that may be contaminated with fractions of post-bomb ¹⁴C and identifying those samples that may not be worthy of undergoing the expense of radiocarbon analysis. On the other side of the radiocarbon timescale, ³⁶Cl measurements may be useful for samples with low ¹⁴C to test for the possibility that the water is very old, but contains a small fraction of relatively young (radiocarbon timescale) water. Given (i) the local tritium and ¹⁴C input function for the bomb era; (ii) the interpretation of initial ¹⁴C in recharge processes; and (iii) geochemical reaction corrections, it may be possible to test various mixing scenarios of young and old water that potentially affect interpretation of ¹⁴C model age for a given locality.

- (2) Most radiocarbon laboratories report the measured ¹⁴C content according to that of Stuiver and Polach (1977) [110], which provides values of per cent modern (pM) carbon normalized for ¹³C of the sample (see the Appendix to Chapter 4). In radiocarbon dating of DIC (or TDC) in aquifers, it is best to use unnormalized ¹⁴C values, pmc and/or δ¹⁴C, and use geochemical models to construct the adjusted ¹⁴C content. Equations to convert the normalized ¹⁴C to non-normalized values are provided in the Appendix to Chapter 4. Geochemical adjustment models are then constructed, such as in Fontes and Garnier (1979) [116] or through use of the code NETPATH (Plummer et al. (1994) [120]) as described above, to adjust the initial ¹⁴C for water–rock reactions.
- (3) Determination of the initial ¹⁴C value, A_0 , in recharge areas of aquifers remains one of the most significant uncertainties in radiocarbon dating of DIC in groundwater. In systems open to CO₂ gas exchange during recharge, such as in some arid regions, A_0 can be near 100 pmc. In systems closed to CO₂ gas exchange following recharge, A_0 may be near 50 pmc if old carbonate rocks dissolve within the aquifer following recharge without further gas exchange with unsaturated zone air. Intermediate values, as well as values even lower than 50 pmc are also possible, depending on the extent of geochemical reactions occurring in the aquifer. The difference between open and closed system evolution the difference between approximately 100 and 50 pmc in A_0 alone introduces 5730 a uncertainty in the adjusted ¹⁴C model age. However, as long as conditions in the recharge area have not substantially varied, groundwater velocities down a flow path calculated from ¹⁴C model ages are not affected by the A_0 error after the first sample.

Two approaches have been taken in estimating A_0 : (i) the initial ¹⁴C value of DIC in the recharge area can be estimated by locating water samples in the recharge area that are low in tritium or CFC content (pre-nuclear detonation waters) and analysing the ¹⁴C content of DIC in these samples (Fig. 4.1); and (ii) the initial ¹⁴C value of DIC can be estimated by applying one or more of the 'traditional' adjustment models discussed above to the chemical data from recharge waters or to the water sample being studied, as in NETPATH. Alternatively, geochemical modelling techniques, such as in PHREEQC, can be used to estimate A_0 values pertaining to assumed conceptualizations of the geochemical evolution of initial waters.

- (4) Consideration should be given to the possibility that the chemical, isotopic and recharge conditions occurring today in the recharge area of the aquifer may not apply to the palaeoconditions prevailing at the time of recharge of the sample being dated with radiocarbon. Changes in climatic conditions could lead to changes in the thickness of the unsaturated zone, recharge rate and the extent of open or closed system conditions. The predominant plant type in the recharge area could shift from one photosynthetic pathway to another, resulting in a change in δ^{13} C of soil gas CO₂. As explained above, many of the models for reconstructing A_0 in recharge waters are sensitive to the assumed δ^{13} C of soil gas CO₂.
- (5) Constructing geochemical adjustments to initial radiocarbon values in aquifers can require considerable geochemical intuition related to water–rock reactions in a system. Data on the carbon isotopic composition of DIC, DOC, CH_4 and POC, and reacting carbon-bearing phases in the system are usually needed or must be estimated, both within the recharge zone and the aquifer system.
- (6) If initial and final water compositions can be proposed, geochemical mass balance reaction models can be used to adjust the initial ¹⁴C value for geochemical reactions along the flow path. The calculated ¹⁴C model age is the time required for decay of the reaction corrected initial ¹⁴C value to the measured (non-normalized) value in the final water. Inverse geochemical modelling codes such as NETPATH and PHREEQC can estimate the effects of hydrodynamic mixing and geochemical processes on the dilution of observed ¹⁴C values. It may be possible to apply some analytical solutions to estimate the importance of matrix diffusion on ¹⁴C model ages.
- (7) In some cases, such as silicate aquifers where geochemical adjustments to A_0 can be small, it may be warranted to apply radiocarbon calibration scales to convert radiocarbon years to calendar years. Before radiocarbon calibration can be applied, radiocarbon ages that have been calculated

by using the modern ¹⁴C half-life (5730 a, as in NETPATH) need to be converted to Libby half-life (5568 a) by using the equation

$$t_{\rm Libby} = 0.972t_{5730} \tag{4.55}$$

This produces the adjusted ¹⁴C model age based on the Libby half-life. Calibrated radiocarbon ages, where warranted, are probably more reliably used in conjunction with numerical models of groundwater flow, as in Sanford et al. (2004) [47].

- (8) Efforts should be made to corroborate radiocarbon ages. Measurements of tritium and/or CFCs should always be made in conjunction with radiocarbon measurements, as discussed above. Measurements of ³⁶Cl can identify mixing of pre-nuclear detonation water with very old groundwater (water on the 100 ka timescale). If the radiocarbon age places the sample near the LGM (18 ka radiocarbon age), comparison with data on the stable isotope composition of the water (Rozanski (1985) [209]) or of the dissolved gas N₂/Ar (Heaton (1981) [210]; Heaton et al. (1983) [56]; Heaton and Vogel (1981) [211]), or recharge temperatures (Herzberg and Mazor (1979) [212]; Stute et al. (1995) [213]; Stute et al. (1995) [214]; Stute and Schlosser (2000) [215]; Stute et al. (1992) [42]) can be used to corroborate the age. Examining the radiocarbon data spatially throughout the aquifer in relation to conceptualization of groundwater flow can also help to corroborate or possibly invalidate some radiocarbon ages. Measurement of vertical ¹⁴C gradients in unconfined or deep aquifers and/or ¹⁴C gradients along flow paths complement geochemical correction procedures, for example, in estimating the initial ¹⁴C value, and determining recharge rates (see Chapter 12). The gradient in ¹⁴C concentration can help to evaluate whether a ¹⁴C decrease with flow distance is due to radioactive decay or the combined effect of decay, retardation and geochemical processes. The process of refining age interpretation can be aided by use of numerical models of groundwater flow, recognizing ages that are consistent with the model and those that are not.
- (9) The complexity of a hydrogeological setting may require more sophisticated full featured numerical simulation tools. The use of these tools will truly be warranted only when there is sufficient information and data available to describe the groundwater system under investigation. If this is the case, ¹⁴C model ages can be used in conjunction with geochemical characterization to help calibrate flow and transport simulations of a groundwater system.

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APPENDIX TO CHAPTER 4

The following appendix provides details that may be of use to hydrologists requiring additional background information. It summarizes the various reporting units of radiocarbon and their interrelationships, reviews isotopic fractionation in carbonate systems open and closed to CO_2 gas, summarizes radiocarbon calibration and its possible application to radiocarbon dating of DIC in groundwater, provides information on methods of collection of radiocarbon samples, provides sources for selected geochemical and radiocarbon software, and contains information on locating radiocarbon laboratories.

A.1. RADIOCARBON REPORTING UNITS

Radiocarbon measurements are reported following specific recommendations (Stuiver and Polach (1977) [110]). These authors recommend that in reporting ¹⁴C measurements, all values should be normalized for isotope fractionation effects to a common δ^{13} C value of -25%. These recommendations have been adopted by most radiocarbon laboratories worldwide, providing conformity in reporting units between the various radiocarbon laboratories and continuity of results with previously reported data.

The practice of normalization of ¹⁴C measurements is well established in the radiocarbon community, and is an appropriate step in converting radiocarbon years to calendar years. Geochemists and hydrologists sometimes lose sight of the fact that radiocarbon dating of DIC in groundwater (Eq. (4.3)) is based on non-normalized ¹⁴C specific activity values (Kalin (1999) [111]; Mook and van der Plicht (1999) [216]; Stuiver and Polach (1977) [110]). By international convention, specific activities are compared to a standard activity, A_{ox} , where $A_{ox} = 0.95$ times the specific activity of NBS oxalic acid (0.95 × 13.56 dpm/g C, in the year A.D. 1950). The initial ¹⁴C specific activity, A_o , and the measured ¹⁴C specific activity of a sample, A, can be expressed as a percentage of this standard activity in pmc, where pmc = $(A/A_{ox}) \times 100$ (Mook (1980) [109]). Here, the notation pmc is used for the non-normalized 'per cent modern carbon' and 'pM' for the commonly reported normalized ¹⁴C value, denoted 'per cent modern'. The ¹⁴C values in pM have been modified (normalized) for assumed ¹³C isotope fractionation from an assumed initial value of -25% to the measured δ^{13} C of the sample.

In some cases, such as in studies of ¹⁴C in plants, bones and tree rings, it is convenient and scientifically justifiable to normalize ¹⁴C values to a common δ^{13} C value of –25‰, to correct for in vitro fractionation processes that affect both ¹³C and ¹⁴C. However, in groundwater, most of the isotopic variation in δ^{13} C of DIC is caused by water–rock interaction or geochemical reactions occurring in the aquifer. For example, the δ^{13} C of DIC is typically more positive than –25‰ (such as for C₃ plants) due to: (i) isotope fractionation between soil gas CO₂ and HCO₃ in recharge water; and (ii) isotope dilution from dissolution of carbonate rocks that are enriched in ¹³C, and not due to in vitro fractionation processes. When dating DIC in groundwater, the actual number of ¹⁴C atoms in the DIC is needed to determine the time elapsed since the DIC was isolated from the modern reservoir (that is, the soil CO₂ derived from plants and air) and its ¹⁴C atoms were recharged. Corrections (adjustments) to the ¹⁴C of DIC are normally made through geochemical calculations, as discussed in this chapter.

Currently, most radiocarbon measurements are made using AMS, which determines radiocarbon ages from a measured isotope ratio (${}^{14}C/{}^{13}C$) or (${}^{14}C/{}^{12}C$). For example, at the University of Arizona AMS facility, radiocarbon ages are determined from the measured ${}^{14}C/{}^{13}C$ ratio in a sample by comparing that ratio with a similar ratio measured in known standards (Linick et al. (1986) [217]). The measured ratios of standards and samples are corrected (normalized) to values corresponding to $\delta^{13}C$ of -25% by using ${}^{13}C/{}^{12}C$ ratios measured in a stable isotope mass spectrometer and the 'fraction of modern', *F*, of the sample, *S*, is found using the Eq. (A.1), where the notation is that of Donahue et al. (1990) [218]:

$$F = \frac{(14/13)_{S[-25]}}{(14/13)_{1950[-25]}} \tag{A.1}$$

where

 $(14/13)_{S[-25]}$ denotes the ¹⁴C/¹³C atom ratio in the sample, *S*, normalized to a δ^{13} C of -25‰; (14/13)_{1950[-25]} is the ¹⁴C/¹³C atom ratio in a standard normalized to -25‰ in the year 1950.

The conventional radiocarbon age (denoted 'Age') of the sample is then:

$$Age = -\tau \ln F \tag{A.2}$$

where τ is the Libby mean life (8033 a; $\tau = 5568/\ln(2)$ and 5568 is the Libby half-life of ¹⁴C).

Donahue et al. (1990) [218] present equations for the conversion of measured isotope ratios to forms that can be used in Eqs (A.1) and (A.2).

Many other AMS radiocarbon laboratories measure the ${}^{14}C/{}^{12}C$ isotope ratio rather than the ${}^{14}C/{}^{13}C$ ratio. Equations are summarized below for results based on either the ${}^{14}C/{}^{12}C$ or ${}^{14}C/{}^{13}C$ ratio.

A.1.1. Recommended reporting units

For consistency with past practice, and following the recommendations of Stuiver and Polach (1977) [110], Mook and van der Plicht (1999) [216] and Donahue et al. (1990) [218], ¹⁴C values will continue to be reported as pM, which has been normalized for ¹³C isotopic fractionation, and its associated $\pm 1\sigma$ value along with the ¹³C value used to normalize pM. The nomenclature used here is as follows (Table A.1).

A.1.2. Relation between radiocarbon reporting units

The equations that follow are based on those of Stuiver and Polach (1977) [110], and were originally intended for ¹⁴C measurements made by counting beta decay in which the ¹⁴C specific activity was measured in disintegrations per minute per gram of carbon. As that gram of carbon contains, to within about 1/10 000, almost entirely ¹²C atoms, the radiocarbon specific activity measured by beta

Value	Unit	Uncertainty	Unit	Description
$\Delta^{14}C$	‰	$\pm 1\sigma$	‰	Per mille depletion or enrichment relative to the NBS I oxalic acid standard normalized for ¹³ C isotopic fractionation
$\delta^{14}C$	‰	$\pm 1\sigma$	‰	Per mille depletion or enrichment relative to the NBS I oxalic acid standard, not normalized for ¹³ C isotopic fractionation
рМ	%	$\pm 1\sigma$		Per cent modern (pM) relative to the NBS I oxalic acid standard, normalized for ¹³ C isotopic fractionation
pmc	%	$\pm 1\sigma$	%	Per cent modern carbon (pmc) relative to the NBS I oxalic acid standard, not normalized for ¹³ C isotopic fractionation
Т	years	$\pm 1\sigma$	years	Conventional radiocarbon age, years before 1950

TABLE A.1. NOMENCLATURE USED IN REPORTING ¹⁴C VALUES

decay can be expressed as the ratio of ${}^{14}C/{}^{12}C$. The terms 'fraction of modern', *F*, and conventional radiocarbon age can be defined similarly as in the first two equations above, which use the ${}^{14}C/{}^{13}C$ ratio, that is, 14/13 is replaced with 14/12. However, in further calculations, such as those necessary for denormalization of reported values of *F* or pM, it is necessary to know which isotope ratio was measured in the AMS facility. The equations below are based on ${}^{14}C/{}^{12}C$ measurements, leading to squared terms in correcting for ${}^{14}C$ fractionation. The exponent is changed from 2 to 1 when the isotope ratio ${}^{14}C/{}^{13}C$ is measured. Donahue et al. (1990) [218] provided equations that relate radiocarbon AMS measurements based on ${}^{14}C/{}^{13}C$ and ${}^{14}C/{}^{12}C$.

In radiocarbon dating of DIC, it may be desirable to make calculations based on δ^{14} C or pmc, which have not been normalized with ¹³C differences from –25‰. As most radiocarbon laboratories report normalized values, it is sometimes necessary to 'denormalize' the reported value in making radiocarbon age calculations in groundwater environments. The actual equations used for 'denormalization' depend on which isotope ratio was measured at the AMS facility, for example ¹⁴C/¹²C or ¹⁴C/¹³C. In either case, the value of pmc is related to δ^{14} C by:

$$pmc = \left(\frac{\delta^{14}C}{1000} + 1\right) 100$$
(A.3)

If the measurement is based on the ${}^{14}C/{}^{12}C$ isotope ratio, then $\delta^{14}C$ is related to the normalized ${}^{14}C$ by Stuiver and Robinson (1974) [219]:

$$\delta^{14} C = \left(\frac{1 + \Delta^{14} C / 1000}{0.975^2 / (1 + \delta^{13} C / 1000)^2} - 1\right) 1000$$
(A.4)

If the basic measurement is from the ${}^{14}C/{}^{13}C$ isotope ratio, the denormalization is:

$$\delta^{14} C = \left(\frac{1 + \Delta^{14} C / 1000}{0.975 / (1 + \delta^{13} C / 1000)} - 1\right) 1000$$
(A.5)

The pM relative to the NBS I oxalic acid standard, normalized for ¹³C isotope fractionation is:

$$pM = \left(\frac{\Delta^{14}C}{1000} + 1\right) 100 \tag{A.6}$$

The conventional radiocarbon age, t, is expressed in years before present (BP), where present is the year 1950, and is normalized for ¹³C differences from -25%:

$$t = -\tau \ln\left(\frac{A_{\text{SN}(\text{in1950})}}{A_{\text{ON}(\text{in1950})}}\right) = -\tau \ln\left(\frac{pM}{100}\right) = -\tau \ln F$$
(A.7)

where $A_{SN(in1950)}$

is the specific activity of ¹⁴C in the sample in the year 1950, normalized for ¹³C fractionation;

 $A_{ON(in 1950)}$ is the specific activity of the standard in 1950.

The conventional radiocarbon age applies best to the dating of wood or other forms of organic matter, or in the dating of DIC in some groundwater systems where the initial ¹⁴C specific activity during recharge is near modern, and geochemical reactions affecting DIC in the aquifer can be ignored, such as in some silicate aquifers (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]; Plummer et al. (2004) [51]). However, generally, the conventional radiocarbon age is biased to old in the dating of DIC in groundwater due to geochemical reaction effects (referred to as 'reservoir effects' in radiocarbon literature).

In some cases, it is necessary to 'denormalize' the commonly reported normalized ¹⁴C pmc value (Mook and van der Plicht (1999) [216]). Normalized ¹⁴C pM values can be converted to non-normalized pmc values by the equation provided by Mook and van der Plicht (1999) [216], for measurements based on the ¹⁴C/¹²C ratio:

$$pmc = pM\left[\left(1 + {}^{13}\delta/1000\right)/0.975\right]^2$$
(A.8)

where ¹³ is the $\delta^{13}C$ of the DIC.

For ¹⁴C measurements based on the ¹⁴C/¹³C ratio:

$$pmc = pM\left[\left(1 + {}^{13}\delta/1000\right)/0.975\right]$$
(A.9)

A.1.3. Relationships derived from the fraction of modern, F

In cases where radiocarbon measurements are reported in the normalized 'fraction of modern', F, terminology, the following equations can be used to deduce the parameters of Table A.1 from the values of F and δ^{13} C.

Terminology:

F = fraction of modern, normalized for ¹³C variations f = fraction of modern, not normalized for ¹³C variations Age = conventional radiocarbon age normalized for ¹³C variations (BP) age = conventional radiocarbon age not normalized for ¹³C variations (BP) pM = normalized per cent modern carbon pmc = not normalized per cent modern carbon $\delta^{14}C$ = not normalized $\Delta^{14}C$ = normalized

 $\Delta^{14}C = \text{normalized}$ $Measured as {}^{14}C/^{12}C$ $Age = -8033 \ln F$ $age = -8033(\ln F - 2\ln(0.975) / (1 + \frac{\delta^{13}C}{1000}))$ $ge = -8033(\ln F - \ln(0.975) / (1 + \frac{\delta^{13}C}{1000}))$ $f = \exp(age / -8033)$ $f = \exp(age / -8033)$ $pmc = \exp(-age / 8033)100$ $pM = \exp(-Age / 8033)100$ $pM = \exp(-Age / 8033)100$ $pM = \exp(-Age / 8033)100$ $\delta^{14}C = (\frac{pmc}{100} - 1)1000$ $\Delta^{14}C = (\frac{pM}{100} - 1)1000$ $\Delta^{14}C = (\frac{pM}{100} - 1)1000$

Example:

Parameter	Calculated
F	0.8633 (reported)
δ ¹³ C (‰)	-13.1 (reported)
F	0.8738
Age (years BP)	1181
age (years BP)	1083
pmc	87.38
pМ	86.33
δ ¹⁴ C (‰)	-126
Δ ¹⁴ C (‰)	-137

Given that F = 0.8633 and $\delta^{13}C = -13.1\%$ (based on measurement of the ${}^{14}C/{}^{13}C$ ratio):

A.1.4. Absolute per cent modern carbon

Absolute pM and absolute pmc refer to the normalized and non-normalized values of per cent modern carbon that have been calculated, taking into account the decay of the oxalic acid standards for the elapsed time between 1950, when the standard was defined, and the date of collection of the sample. Such corrections are on the order of 50 years and are unnecessary when dealing with geological samples; they are not included here. Further details are provided in Stuiver and Polach (1977) [110], and Mook and van der Plicht (1999) [216].

A.1.5. Age error from use of normalized ¹⁴C values

Although there are many uncertainties in radiocarbon dating of DIC in groundwater, an unnecessary error is introduced if ages are based on the normalized pM value rather than the denormalized ¹⁴C pmc value. This difference is not always recognized but, fortunately, the error resulting from use of pM rather than pmc is relatively small. Figure A.1 shows that the error in age varies almost linearly with the value of δ^{13} C of the DIC. If δ^{13} C of the DIC is greater than -25‰, the calculated radiocarbon age based on pM will be too old relative to the age properly based on pmc. When $\delta^{13}C$ is more negative than -25%, the calculated radiocarbon age will be too young relative to the age properly based on pmc. The δ^{13} C of DIC in most groundwater is more positive than -25%, and commonly in the range of -20 to approximately 0% (Vienna Peedee belemnite scale). For this range of δ^{13} C values, the age based on pM is approximately 100-400 a too old, respectively. Considering the overall uncertainties in radiocarbon dating of DIC in groundwater, these errors are not generally significant, but do introduce an unnecessary bias in the radiocarbon age. In a few environments, such as where organic carbon is undergoing methanogenesis, the DIC may be significantly enriched in δ^{13} C, and ages based on pM could be as much as 1000 a too old. In environments where the DIC is derived from oxidation of highly depleted carbon sources, such as methane, the radiocarbon age can be as much as 1000 a too young if based on pM rather than correctly on pmc (Fig. A.1).

In summary, radiocarbon dating of DIC in groundwater should be based on the measured ¹⁴C specific activity relative to the modern standard, and can be expressed in δ^{14} C or pmc values. Small errors result if radiocarbon age is evaluated from normalized ¹⁴C values, Δ^{14} C or pM. Measurements of pM should always be accompanied by the measured δ^{13} C and associated 1 σ errors.



FIG. A.1. Age error resulting from use of pM instead of pmc in radiocarbon dating as a function of δ^{13} C of DIC in the water sample.

A.2. ISOTOPIC FRACTIONATION IN CARBONATE WATERS

A.2.1. Definitions

Some of the basic definitions are listed that are mostly assumed in the treatment given here. Further information can be found in texts such as Clark and Fritz (1997) [52], and Mook (2005) [119].

R refers to an isotope ratio and it is defined as the ratio of the abundance of the rare isotope divided by the abundance of the abundant isotope:

 $R = \frac{\text{abundance of rare isotope}}{\text{abundance of abundant isotope}}$

Examples for ¹³C and ¹⁴C would be as follows:

$${}^{13}R = \frac{{}^{13}C}{{}^{12}C}; \qquad {}^{13}R_{CO_2} = \frac{{}^{13}CO_2}{{}^{12}CO_2}; \qquad {}^{14}R_{CO_2} = \frac{{}^{14}CO_2}{{}^{12}CO_2}$$
(A.10)

Isotope abundance is usually expressed in δ notation, which expresses the value of an isotope ratio of an element in a sample, *s*, relative to that ratio in a standard:

$$\delta_{\text{A-ref}} \left(= \frac{R_{\text{A}}}{R_{\text{ref}}} - 1 \right) \times 10^3 \text{ per mille}$$
(A.11)

As values of δ are small dimensionless numbers, they are usually multiplied by 10^3 %:

$${}^{13}\delta = \left(\frac{({}^{13}C/{}^{12}C)_{s}}{({}^{13}C/{}^{12}C)_{ref}} - 1\right) \times 10^{3}; \qquad {}^{14}\delta = \left(\frac{({}^{14}C/{}^{12}C)_{s}}{({}^{14}C/{}^{12}C)_{ref}} - 1\right) \times 10^{3}$$
(A.12)

Isotope fractionation is mathematically expressed by comparing the isotope ratios of two compounds that are in isotopic equilibrium. The isotope fractionation factor, α_{B-A} , is:

$$\alpha_{\rm B-A} = \frac{R_{\rm (B)}}{R_{\rm (A)}} \tag{A.13}$$

which expresses the isotope ratio of the phase or compound B relative to that in A. Combining Eqs (A.11, A.13), it can be shown that:

$$\alpha_{\rm B-A} = \frac{1000 + \delta_{\rm (B)}}{1000 + \delta_{\rm (A)}} \tag{A.14}$$

Generally, fractionation factors, α , are near unity. Therefore, the deviation of α from 1 is commonly expressed as an 'enrichment factor', also referred to as an 'additive fractionation factor', because of an approximation that is described below. The 'enrichment factor', ε (in ‰) is related to α by:

$$\varepsilon_{\rm B-A} = (\alpha_{\rm B-A} - 1)(10^3) = \left(\frac{R_{\rm (B)}}{R_{\rm (A)}} - 1\right) \times 10^3$$
(A.15)

 ε_{B-A} is referred to as the 'additive fractionation factor' because:

$$\delta_{\rm B} \cong \delta_{\rm A} + \varepsilon_{\rm B-A} \quad \text{or} \quad \delta_{\rm B} - \delta_{\rm A} \cong \varepsilon_{\rm B-A}$$
(A.16)

Approximations of the form of Eq. (A.16) have been applied in the derivation of some of the traditional adjustment models for estimation of A_0 described in this volume. All isotopic calculations in NETPATH and PHREEQC are made in terms of *R* and α , without introduction of this approximation.

A further complication that arises in making isotopic calculations in CO₂–water systems stems from the fact that what is measured is the ¹³C or ¹⁴C isotopic composition of the total DIC in the groundwater sample. There is no means of routinely measuring the isotopic composition of individual molecules of CO₂(aq), HCO₃ or CO₃²⁻ in solution. Yet, isotopic fractionation occurs between molecules and phases, for which the isotopic fractionation factors are defined. A transformation is made to redefine pH dependent values of α (and ε) relative to the average isotopic composition of the solution. Accordingly, ¹³ R_{DIC} is:

$${}^{13}R_{\rm DIC} = \frac{\left[CO_{2aq}\right]{}^{13}R_{\rm CO_{2aq}} + \left[HCO_{3}^{-}\right]{}^{13}R_{\rm HCO_{3}^{-}} + \left[CO_{3}^{2^{-}}\right]{}^{13}R_{\rm CO_{3}^{2^{-}}}}{\left[CO_{2aq}\right] + \left[HCO_{3}^{-}\right] + \left[CO_{3}^{2^{-}}\right]}$$
(A.17)

Dividing Eq. (A.17) by ${}^{13}R_{\text{HCO}_{3}}$, and because ${}^{13}\alpha_{i-\text{HCO}_{3}} = {}^{13}R_{i}/{}^{13}R_{\text{HCO}_{3}}$

$$\frac{{}^{13}R_{\rm DIC}}{{}^{13}R_{\rm HCO_3^-}} = \frac{\left[CO_{2\rm aq}\right]{}^{13}\alpha_{\rm CO_{2\rm aq}-HCO_3^-} + \left[HCO_3^-\right] + \left[CO_3^{2-}\right]{}^{13}R_{\rm CO_3^{2-}}}{DIC}$$
(A.18)

Using Eq. (A.14) and defining the fraction of the concentration of the *i*th carbonate species to the total concentration of DIC, $\chi_i = [i]/DIC$:

$$\delta^{13}C_{HCO_{3}^{-}} = \frac{1000 + \delta^{13}C_{DIC}}{\chi_{CO_{2aq}}^{-13}\alpha_{CO_{2aq}}^{-} + \chi_{HCO_{3}^{-}} + \chi_{CO_{3}^{-}}^{-13}\alpha_{CO_{3}^{-} - HCO_{3}^{-}}}$$
(A.19)

Similarly, the fractionation factor for calcite relative to DIC can be written as:

$${}^{13}\alpha_{\text{calcite-DIC}} = \frac{{}^{13}\alpha_{\text{calcite-HCO}_3^-}}{\chi_{\text{CO}_{2aq}}{}^{13}\alpha_{\text{CO}_{2aq}}{}^{-HCO_3^-} + \chi_{\text{HCO}_3^-} + \chi_{\text{CO}_3^{--}}{}^{13}\alpha_{\text{CO}_3^{--}-HCO_3^-}}$$
(A.20)

and for CO₂ gas relative to DIC as:

$${}^{13}\alpha_{CO_{2gas}-DIC} = \frac{{}^{13}\alpha_{CO_{2gas}-HCO_{3}^{-}}}{\chi_{CO_{2aq}}{}^{13}\alpha_{CO_{2aq}}{}^{-HCO_{3}^{-}} + \chi_{HCO_{3}^{-}} + \chi_{CO_{3}^{2-}}{}^{13}\alpha_{CO_{3}^{2-}-HCO_{3}^{-}}}$$
(A.21)

A.2.2. Fractionation factors

Two sets of fractionation factors in the calcite– CO_2 –water system are commonly in use and available in NETPATH (Plummer et al. (1994) [120]). These are identified as the 'Mook set' and the 'Deines set' of fractionation factors. The Mook set (Mook (2005) [119]) was derived from experimental data obtaining temperature dependent expressions for the additive fractionation factors (enrichment factors) as follows:

Values of ε_{i-j} over the temperature range of 0–40°C are shown in Table A.2.

Deines et al. (1974) [122] provide the following relations for the temperature dependence of selected fractionation factors in the calcite– CO_2 water system:

$$1000 \ln^{13} \alpha_{\rm CO_{2aq}-CO_{2gas}} = -0.91 + \frac{6300}{T^2}$$
(A.22)

$$1000 \ln^{13} \alpha_{\rm CO_3^{2-}-CO_{2gas}} = -3.4 + \frac{870\,000}{T^2} \tag{A.23}$$

$$1000 \ln {}^{13}\alpha_{\text{calcite-CO}_{2gas}} = -3.63 + \frac{1\,194\,000}{T^2} \tag{A.24}$$

TABLE	A.2.	SUMMARY	OF	EXPRESSIONS	FOR	TEMPERATURE	DEPENDEN	ICE OF	ADDI	ITIVE
FRACTI	ONA	TION FACTO	RS II	N THE CALCITE-	$-CO_2V$	WATER SYSTEM '	MOOK SET'	(MOOK	(2005)	[119])

Equation	Reference
$\overline{\varepsilon_{\rm g-b}} = -9483/\mathrm{T} + 23.89\% (1)$	Mook et al. (1974) [220]
$\varepsilon_{a-g} = -373/T + 0.19\%$ (2)	Vogel et al. (1970) [138]
$\varepsilon_{a-b} = -9866/T + 24.12\%(3)$	From (1) and (2)
$\varepsilon_{c-b} = -867/T + 2.52\%$ (4)	Thode et al. (1965) [221] and (1)
$\varepsilon_{\text{cal-b}} = -4232/\text{T} + 15.10\%(5)$	Mook (2005) [119] ^a
$\varepsilon_{\text{cal-g}} = +5380/\text{T} - 9.15\%$ (6)	From (1) and (5)

^a Based on evaluation of original data from Rubinson and Clayton (1969) [222], and Emrich et al. (1970) [223].

TABLE A.3. VALUES OF $\varepsilon_{i \! \! - \! j}$ CALCULATED FROM THE 'MOOK SET' OVER THE TEMPERATURE RANGE OF 0–40°C

Temperature (°C)	$\mathcal{E}_{\mathrm{g-b}}$	\mathcal{E}_{a-g}	$\mathcal{E}_{\mathrm{a-b}}$	$\mathcal{E}_{\mathrm{c-b}}$	ε_{cal-b}	$\varepsilon_{\mathrm{cal-g}}$
0	-10.83	-1.18	-12.00	-0.65	-0.39	10.55
5	-10.20	-1.15	-11.35	-0.60	-0.11	10.19
10	-9.60	-1.13	-10.72	-0.54	0.15	9.85
15	-9.02	-1.10	-10.12	-0.49	0.41	9.52
20	-8.46	-1.08	-9.54	-0.44	0.66	9.20
25	-7.92	-1.06	-8.97	-0.39	0.91	8.89
30	-7.39	-1.04	-8.42	-0.34	1.14	8.60
35	-6.88	-1.02	-7.90	-0.29	1.37	8.31
40	-6.39	-1.00	-7.39	-0.25	1.59	8.03

Note: $g = CO_2$ (gas); $a = CO_2$ (aq); $b = HCO_3^-$; $c = CO_3^{2-}$; cal = calcite.

Temperature (°C)	$\varepsilon_{\mathrm{g-b}}$	$\varepsilon_{\mathrm{a-g}}$	$\varepsilon_{\mathrm{a-b}}$	\mathcal{E}_{c-b}	$\varepsilon_{\text{cal}-b}$	$\varepsilon_{\rm cal-g}$
0	-10.14	-0.83	-10.95	-1.93	2.19	12.45
5	-9.62	-0.83	-10.44	-1.82	2.14	11.87
10	-9.13	-0.83	-9.95	-1.71	2.10	11.33
15	-8.66	-0.83	-9.48	-1.62	2.06	10.81
20	-8.21	-0.84	-9.04	-1.52	2.02	10.32
25	-7.79	-0.84	-8.62	-1.44	1.98	9.85
30	-7.39	-0.84	-8.23	-1.35	1.95	9.41
35	-7.01	-0.84	-7.85	-1.27	1.91	8.98
40	-6.64	-0.85	-7.48	-1.19	1.88	8.58

TABLE A.4. VALUES OF $\varepsilon_{i,j}$ CALCULATED FROM THE 'DEINES SET' OVER THE TEMPERATURE RANGE OF 0–40°C

Note: $g = CO_2$ (gas); $a = CO_2$ (aq); $b = HCO_3^-$; $c = CO_3^-$; cal = calcite.



FIG. A.2. The additive fractionation factor, $\varepsilon_{CO2 \text{ gas}-DIC}$, between CO_2 gas (g) and the isotopic composition of dissolved inorganic carbon (s) as a function of solution pH from 0 to 30°C, based on the Deines set of fractionation factors (from Wigley et al. (1978) [136]).

$$1000 \ln^{13} \alpha_{\rm HCO_3^--CO_{2gas}} = -4.54 + \frac{1099\,000}{T^2}$$
(A.25)

Table A.3 summarizes values of ε_{i-j} calculated from the Mook set over the temperature range of 0–40°C, which can be compared to the values from the Deines set (Table A.4).

Values of $\varepsilon_{CO_{2gas}-DIC}$ and $\varepsilon_{calcite-DIC}$ calculated from Eqs (A.20, A.21, A.15) as a function of temperature based on the Deines set of fractionation factors are provided in Figs A.2 and A.3.

Due to the mass difference between ¹³C and ¹⁴C atoms, it can be shown that the additive fractionation factors for ¹⁴C should be approximately twice those of ¹³C (Craig (1954) [143]):

$${}^{14}\varepsilon \cong 2 {}^{13}\varepsilon \tag{A.26}$$



FIG. A.3. The additive fractionation factor, $\varepsilon_{calcite-DIC}$, between calcite (p) and the isotopic composition of dissolved inorganic carbon (s) as a function of solution pH from 0 to 30°C, based on the Deines set of fractionation factors (from Wigley et al. (1978) [136]).

This relation is used in NETPATH (Plummer et al. (1994) [120]). There is some experimental and theoretical evidence that the additive fractionation factors for ¹⁴C may be approximately 2.3 times greater than those for ¹³C (Saliege and Fontes (1984) [224]; Wigley and Muller (1981) [225]).

A.2.3. Total dissolved carbon

If TDC is defined as
$$m_{\text{TDC}} = m_{\text{DIC}} + m_{\text{DOC}} + m_{\text{CH4}}$$
, then $\delta^{13}C_{\text{TDC}}$ becomes:

$$\delta^{13}C_{\rm TDC} = \frac{m_{\rm DIC}\delta^{13}C_{\rm DIC} + m_{\rm DOC}\delta^{13}C_{\rm DOC} + m_{\rm CH_4}\delta^{13}C_{\rm CH_4}}{m_{\rm TDC}}$$
(A.27)

If methane and/or DOC are present, the fractionation factors relative to the average isotopic composition of the solution need to be modified to reflect the presence of these additional species, even though they are not likely to be in isotopic equilibrium with any carbon-bearing aqueous species in the solution. Therefore, to estimate values of fractionation factors in the system of TDC, concentrations and isotopic composition of DOC and/or CH_4 must be measured or defined. Following the above examples for calcite and CO_2 gas, Eqs (A.20, A.21) become:

$${}^{13}\alpha_{\text{calcite-TDC}} = \frac{{}^{13}\alpha_{\text{calcite-HCO}_3^-}}{\chi_{\text{CO}_{2aq}} {}^{13}\alpha_{\text{CO}_{2aq}} {}^{-\text{HCO}_3^-} + \chi_{\text{HCO}_3^-} + \chi_{\text{CO}_3^{--}} {}^{13}\alpha_{\text{CO}_3^{--} {}^{-\text{HCO}_3^-}} + \chi_{\text{DOC}} {}^{13}\alpha_{\text{DOC}-\text{HCO}_3^-} + \chi_{\text{CH}_4} {}^{13}\alpha_{\text{CH}_4 {}^{-\text{HCO}_3^-}}$$
(A.28)

and

$${}^{13}\alpha_{\rm CO_{2gas}-TDC} = \frac{{}^{13}\alpha_{\rm CO_{2gas}-HCO_3^-}}{\chi_{\rm CO_{2aq}}{}^{13}\alpha_{\rm CO_{2aq}-HCO_3^-} + \chi_{\rm HCO_3^-} + \chi_{\rm CO_3^{2^-}} + \chi_{\rm DOC}{}^{13}\alpha_{\rm DOC-HCO_3^-} + \chi_{\rm CH_4}{}^{13}\alpha_{\rm CH_4-HCO_3^-}} (A.29)$$

In Eqs (A.28, A.29), $\alpha_{\text{DOC-HCO}_{3}}$ and $\alpha_{\text{DOC-HCO}_{3}}$ are treated as though they were empirical kinetic isotope fractionation factors and defined from the measured (or estimated) isotopic composition of DOC and CH₄ in the groundwater sample:



FIG. A.4. The $\delta^{13}C_{DIC}$ of dissolved inorganic carbon in the open system calcite– CO_2 –water, for $\delta^{13}C_{CO_2} = -23\%$ at 20°C (Mook's set of fractionation factors).

$$^{13} CH_4-HCO_3^- = \frac{1000 + \delta^{13}C_{CH}}{1000 + \delta^{13}C_{HCO^-}}$$
(A.30)

and

$${}^{13}\alpha_{\text{DOC-HCO}_{3}^{-}} = \frac{1000 + \delta^{13}C_{\text{DOC}}}{1000 + \delta^{13}C_{\text{HCO}_{3}^{-}}}$$
(A.31)

Values of $\delta^{13}C_{HCO_{\bar{3}}}$ are calculated from the measured $\delta^{13}C_{DIC}$ using Eq. (A.19).

Examples: Open system

Using the Mook set of additive fractionation factors in the inorganic calcite– CO_2 –water system, the $\delta^{13}C_{DIC}$ of DIC is calculated as calcite dissolves, maintaining isotopic equilibrium among all dissolved species and calcite at 20°C for a (constant) $\delta^{13}C_{CO_2 \text{ gas}}$ value of –23‰; pointing to evolution in a system open to soil gas CO₂ of ¹³C isotopic composition of –23‰. The following ε values are obtained from Table A.2, at 20°C: $\varepsilon_{g-b} = -8.46\%$; $\varepsilon_{a-g} = -1.08\%$; $\varepsilon_{a-b} = -9.54\%$; $\varepsilon_{c-b} = -0.44\%$; $\varepsilon_{cal-b} = 0.66\%$; $\varepsilon_{cal-g} = 9.20\%$.

Accordingly, for $\delta^{13}C_{CO_2gas}$, which was defined to be -23%, $\delta^{13}C_{calcite} = -13.8\%$, $\delta^{13}C_{HCO_5} = -14.5\%$, $\delta^{13}C_{CO_3} = -14.9\%$ and $\delta^{13}C_{CO_2aq} = -24.1\%$. Calculating the fractions of inorganic carbon species relative to DIC and using Eq. (A.19), it can be seen that the value of $\delta^{13}C_{DIC}$ will increase with increasing pH, as calcite dissolves, from about -24% at pH5 and increases to about -14.5% at pH8.5 where nearly all of the DIC is HCO₃ (Fig. A.4). A similar result is obtained from the 'Deines set' using the plot of Fig. A.2 where at 20°C and pH8.5, ε_{g-DIC} is approximately -8% and $\delta^{13}C_{DIC}$ is about -15%.

Next, an estimation is made of the initial ¹⁴C pmc value of DIC in groundwater in equilibrium with a soil gas CO₂ value of 100 pmc at 20°C. As ¹⁴ $\varepsilon_{g-DIC} \cong 2^{13}\varepsilon_{g-DIC} \cong -16\%$, A_o in an open system at 20°C is about 102 pmc:

$${}^{13}\varepsilon_{g-DIC} \approx -8 = {}^{13}\delta C_{g} - {}^{13}\delta C_{DIC}$$

$${}^{14}\varepsilon_{g-DIC} \approx 2 {}^{13}\varepsilon_{gDIC} \approx 2(-8) \approx {}^{14}\delta C_{g} - {}^{14}\delta C_{DIC} = -160$$

$${}^{14}\delta C_{DIC} = {}^{14}\delta C_{g} + 16$$

$${}^{14}\delta C_{g} = \left(\frac{pmc}{100} - 1\right)1000 = \left(\frac{100}{100} - 1\right)1000 = 00$$

$${}^{14}\delta C_{DIC} \approx {}^{14}\delta C_{g} + 16 = 0 + 16 = 160$$

$$pmc = \left(\frac{{}^{14}\delta C_{g}}{1000} + 1\right)100 = \left(\frac{16}{1000} + 1\right)100 = 101.6$$

A.3. RADIOCARBON CALIBRATION

Regardless of the extent of geochemical corrections, use of the Libby half-life permits use of radiocarbon calibration scales (Stuiver et al. (1998) [226]; Stuiver et al. (1998) [227]). Radiocarbon calibration scales correct for past variations in the strength of the Earth's geomagnetic field and strength of the solar flux. The ¹⁴C content of atmospheric CO₂ has varied in the past, and for the most part has been somewhat greater than 100 pM (Bard et al. (1993) [228]; Bard et al. (1990) [112]; Bartlein et al. (1995) [229]; Stuiver et al. (1986) [230]; Stuiver and Reimer (1993) [231]). By using the Libby half-life for ¹⁴C and making the appropriate corrections for geochemical reactions, calendar years BP can be derived using radiocarbon calibration scales (Stuiver et al. (1998) [226]; Stuiver et al. (1998) [227]). Figure A.5 shows a plot relating the conventional radiocarbon age (unadjusted for geochemical reactions) to calendar years BP (Stuiver et al. (1998) [226]; Stuiver et al. (1998) [227]). The correction to calendar years is fairly small for samples with radiocarbon ages of less than 10 ka. The correction increases for samples with radiocarbon ages of 10–20 ka. For example, if the radiocarbon age (Libby half-life, adjusted for all geochemical reactions) is 20 ka, the corresponding age in calendar years is nearly 24 ka (Fig. A.5). As adjusted radiocarbon ages are used as calibration criteria for some groundwater flow models, calendar years apply to the hydraulic timescale, not radiocarbon years.

Figure A.5 was extended to approximately 45 ka (radiocarbon years) by using lake varve chronologies (Kitagawa and van der Plicht (1998) [233]; Kitagawa and van der Plicht (1998) [234];



FIG. A.5. Radiocarbon calibration scale (based on data of Stuiver et al. (1998) [226] and Stuiver et al. (1998) [227]; see also Fairbanks et al. (2005) [232]).



FIG. A.6. Extended radiocarbon calibration to approximately 45 ka radiocarbon years (based on the data of Bard et al. (1998) [236]; Kitagawa and van der Plicht (1998) [233]; Kitagawa and van der Plicht (1998) [234]; Kitagawa and van der Plicht (2000) [235]; Stuiver et al. (1998) [226]; Stuiver et al. (1998) [227]). The blue line is from Eq. (A.33) from Plummer et al. (2004) [49] (see Fairbanks et al. (2005) [232]).

Kitagawa and van der Plicht (2000) [235]) (Fig. A.6). A polynomial (Eq. (A.32)) was fitted to the data of Fig. A.6 and used to estimate calendar years from the unadjusted radiocarbon age (Libby half-life):

calendar years BP =
$$-173.94 + 1.1713A - 2.0521 \times 10^{-5}A^2 + 4.0150 \times 10^{-9}A^3$$

- $2.4519 \times 10^{-13}A^4 + 5.7738 \times 10^{-18}A^5 - 4.6915 \times 10^{-23}A^6$ (A.32)

where A is the unadjusted radiocarbon age (Libby half-life) in years.

Although the radiocarbon calibration data obtained from tree rings (Stuiver et al. (1998) [226]; Stuiver et al. (1998) [227]) and ²³⁰Th/²³⁴U dating of corals (Bard et al. (1998) [236]) are relatively precise, larger uncertainties in radiocarbon calibration are associated with data obtained from varves (Kitagawa and van der Plicht (1998) [233]; Kitagawa and van der Plicht (1998) [234]). Recently, additional calibration data have been obtained from a stalagmite in the calendar year age range of 11–45 ka that indicate large variations in atmospheric ¹⁴C content of between 33 and 45 ka (Bard (2001) [237]; Beck et al. (2001) [238]). Although radiocarbon calibration to about 20 ka now seems well established for groundwater applications, extension of the calibration to the dating limits of the radiocarbon method (about 45 ka) has received considerable attention recently (Chiu et al. (2007) [108]; Chiu et al. (2005) [239]; Chiu et al. (2006) [240]; Fairbanks et al. (2005) [232]; Sanford et al. (2004) [47]; Sanford et al. (2004) [48]).

A.4. FIELD COLLECTION PROCEDURES

A.4.1. Well selection

Water samples for ¹⁴C determination have historically been obtained from a variety of groundwater sources, including municipal supply wells, monitoring wells, wells used for domestic or farm supply, windmills, flowing wells and springs. Prior to sampling, attention should be given to well construction,

depth and length of the interval open to an aquifer. Commonly, municipal supply wells are open to large intervals of an aquifer, resulting in mixing across ¹⁴C model age gradients. Samples pumped from fractured rock aquifers also tend to be mixtures. Preferred samples for radiocarbon dating are obtained from monitoring wells or flowing wells with a short open interval to the aquifer.

For recently constructed wells, a precaution is necessary; the possibility should be considered that the aquifer was contaminated with fluids used in the drilling process. During drilling, such as in mud-rotary drilling, and in well development after completing a well, water is often imported to the drilling site and pumped into the wellbore. If this imported water is not completely removed in well development, the DIC in the vicinity of the well opening can be contaminated. Plummer et al. (2004) [49] measured the concentrations of CFCs in water pumped from deep, recently completed monitoring wells in New Mexico to identify samples that were likely still contaminated with imported water used in drilling and well development. The most reliable radiocarbon data were obtained from monitoring wells that were free of CFCs, and from domestic supply wells that tended to have more use and relatively short open intervals. As a general guide, water from recently drilled monitoring wells is more likely to be contaminated than water from older wells that have a long history of sampling (or extended well development). The problem is particularly acute in sampling very old water because, due to low flow velocities in an aquifer, groundwater contaminated during drilling may still reside in the vicinity of a well screen even many years after drilling. Due to matrix diffusion into sediment pore spaces, many pore volumes may need to be pumped prior to sampling.

Flowing wells can be another good source of uncontaminated water if there is a long history of use. Finally, because of the possibility of mixing with young fractions, sampling for radiocarbon determination should always include determination of tritium (and possibly CFCs).

A.4.2. Sample collection

Water samples should be collected as close to the source as possible, and certainly before treatment, such as chlorination, ozonation or aeration, and only after sufficient flow to clear three wellbore volumes from the casing. In the case of domestic supply wells, it is recommended that samples be taken before water enters a pressure tank, where, in the case of a bladderless pressure tank, water would be exposed to a gas phase.

A.4.2.1. Tritium

Tritium samples are collected in a 1 L plastic-coated glass bottle with a polycone seal cap. A headspace of approximately 2–3 mL is left in the bottles during filling to accommodate expansion upon warming. Tritium analysis is used to detect contamination of old groundwater with water from the bomb era or contamination from drilling. In the case of very old water, as discussed here, tritium should be determined with a very low minimum detection level (<0.1–0.3 TU by electrolytic enrichment and liquid scintillation counting; or preferably <0.1 TU by the helium in-growth method (Bayer et al. (1989) [241]; Clarke et al. (1976) [242]).

A.4.2.2. Carbon-13 and carbon-14 of dissolved inorganic carbon

Water samples for the determination of δ^{13} C and 14 C of DIC should be filtered in the field (0.45 µm filter), collected in safety coated glass bottles, and capped with a polycone seal cap, leaving a small 2–3 mL headspace to accommodate water expansion. Alternatively, if a sample will be analysed within a few months, a Teflon/silicon septum cap can be used; excluding headspace is recommended. In this case, the septum is normally depressed as the cap is put in place to allow for water expansion. Although it



FIG. A.7. Guidelines indicating amounts of groundwater sample required for collection to obtain at least 5 mg C/L as a function of alkalinity (as CaCO₃) and pH (note: alkalinity (in mg/L as CaCO₃) = alkalinity (in mg/L as HCO₃) × 0.82014).

can be debated, addition of a preservative to stop possible microbial activity runs a risk of contamination of the sample with a fraction of modern ¹⁴C and is not recommended for old groundwater samples.

Although most AMS facilities can determine ¹⁴C content of DIC with as little as 1 mg of carbon, it is recommended that the volume of water sample collected be sufficient to contain a minimum of 5 mg of DIC (as C). For many water samples, a 250 mL sample will be sufficient. Figure A.7 provides guidelines for sample volumes required to provide a minimum of 5 mg DIC for a range of field alkalinities and pH. The two curves in the figure provide corresponding alkalinity and pH values for simple inorganic carbonate waters (at 25°C) that would contain 5 or 10 mg of DIC in a 250 mL volume. If, for example, the sample alkalinity is 150 mg/L (as CaCO₃) or greater, a 250 mL bottle fitted with a Teflon/silicon septum is sufficient for most pH. Sample volumes of 1 L or more will be needed if field alkalinity is less than 80 mg/L (as CaCO₃) and pH is greater than 7.0. If alkalinity is unknown at the time of sampling, it is recommended to fill two 1 L bottles.

A.4.3. Recommended method of collection (dissolved inorganic carbon)

Fill the appropriate bottle(s) fitted with a Teflon/silicon septum cap to provide at least 5 mg of DIC. Fill the sample container(s) from the bottom of the vessel. Use an in-line filter (0.45 μ m) to eliminate the possibility of contamination of the DIC with particulates containing carbonate minerals. If there is concern about DOC oxidation in the sample bottle, a silver filter can be used, though this is normally not needed. Minimize contact with air while filling the bottle(s). This can be accomplished by establishing a closed path from the water source, through the filter, to the bottom of the container. Fill from the bottom, allowing overflow of several litres of filtered water. For potentially low ¹⁴C samples (<10 pmc) or if relatively long times are required for filtering, place the sample bottle in a small bucket or beaker containing water from the same source, flush the sample bottle from the bottom of the bottle while still immersed in the bucket or beaker (allowing overflow of several litres) and cap with a Teflon/silicon septum cap under water. It is best to depress the septum slightly, without compromising the seal, as the cap is screwed onto the bottle to provide room for water expansion as the sample warms during transit and storage prior to analysis. Use plastic coated glass bottles fitted with a Teflon/silicon septum for most samples. The septum allows laboratory extraction of the water sample without contact with air.

A.4.4. Carbon-13 and carbon-14 of dissolved organic carbon

The procedure for collection of HMW and LMW fractions of DOC is provided in Murphy et al. (1989) [172] and is based on the original work of Thurman and Malcolm (1981) [180], and Murphy (1987) [181]. The sample is filtered (0.45 μ m) in the field and collected using a field column system. The fulvic acids (primarily HMW) typically make up about 30% of the DOC in groundwater, and are collected on XAD-8 resin. The LMW compounds are collected on Silicalite, a silica based molecular sieve. Prior to use, the Silicalite is preheated to 1000°C to remove organic contamination. The XAD-8 and Silicalite columns remove only about 30–60% of the total DOC in groundwater. To characterize the fulvic acid fraction completely, a minimum of 200 mg of material is typically needed, and sample volumes of the order of 100–200 L are usually processed. Further details are provided in Murphy et al. (1989) [172]. Other procedures for collection of total DOC can be found in Purdy et al. (1992) [173] and Burr et al. (2001) [184].

A.5. GEOCHEMICAL MODELLING SOFTWARE

United States Geological Survey (USGS) geochemical modelling software of use in interpreting radiocarbon data (NETPATH, NETPATH-WIN, NetpathXL, PHREEQC, PhreeqcI) and associated documentation can be downloaded from the web site:

http://wwwbrr.cr.usgs.gov/projects/GWC_coupled/ Other USGS geochemical software is available from: http://water.usgs.gov/software/geochemical.html The CALIB Radiocarbon Calibration Programme is available from: http://calib.qub.ac.uk/calib/

A.6. SELECTED ACCELERATOR MASS SPECTROMETRY FACILITIES FOR RADIOCARBON ANALYSIS

A list of active radiocarbon laboratories (conventional beta-counting facilities and AMS facilities), and known personnel is published annually in the journal Radiocarbon (see, for example, List of Laboratories, Radiocarbon **51**(4) (2009) 1187–1211 and http://www.radiocarbon.org/Info/lablist.html).

Chapter 5

KRYPTON-81 DATING OF OLD GROUNDWATER

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5.1. INTRODUCTION

5.1.1. Krypton in the environment

The abundance of krypton in the atmosphere has been quoted for nearly half a century as 1.14 ± 0.01 ppm, which corresponds to a total atmospheric inventory of 4.51×10^{12} m³ STP (Verniani (1966) [243]). A recent re-evaluation yielded a value of 1.099 ± 0.009 ppm_v, which is about 4% lower than the previously used value (Aoki and Makide (2005) [244]).

Krypton has six stable isotopes of which ⁸⁴Kr is the most abundant, comprising about 57% of natural Kr (Table 5.1). Eleven major radioactive isotopes of Kr exist but only ⁸¹Kr and ⁸⁵Kr, with halflives of 229 000 and 10.76 a, respectively, exceed 2 d and are, therefore, suitable for the investigation of environmental processes. Krypton-81 is produced in the atmosphere by cosmic ray induced spallation of heavier stable Kr isotopes and by the nuclear reactions ⁸⁰Kr(n, γ)⁸¹Kr and ⁸²Kr(γ , n)⁸¹Kr.

The atmospheric ⁸¹Kr/Kr ratio has been measured three times by different methods and research groups (Fig. 5.1; Collon et al. (1997) [245]; Kuzminov and Pomansky (1983) [246]; Loosli and Oeschger (1969) [247]). The mean value of $5.2 \pm 0.6 \times 10^{-13}$ corresponds to a specific activity in the modern atmosphere of 1.47 mBq \cdot L⁻¹ Kr.¹ Variations in the production rate, for example, due to modulations of the geomagnetic field intensities with a period of 10–30 ka (Plummer et al. (1997) [248]), are likely to be averaged out on the timescale of the ⁸¹Kr mean lifetime (the atmosphere is well mixed within a timescale of ~1 a). This, and the fact that the atmosphere represents the main terrestrial Kr reservoir, provides evidence that the ⁸¹Kr abundance in the atmosphere is rather constant over its applicable age dating range.

The production of ⁸¹Kr from ²³⁵U or ²³⁸U fission is expected to be very small because the nuclide is shielded by stable ⁸¹Br. The direct fission yield of ⁸¹Kr is estimated to be only 7×10^{-11} atoms ⁸¹Kr/atoms U_{decayed}. For this reason, anthropogenic sources such as nuclear weapon testing and releases from the nuclear industry are probably insignificant. This has been confirmed by the comparison of post-bomb and pre-bomb atmospheric samples, for which the most recent measurements resulted in an agreement at the 8% precision level (Du et al. (2003) [249]). Likewise, subsurface production of ⁸¹Kr in rocks is expected to be very small; the equilibrium concentration of ⁸¹Kr from fission production is 5×10^{-6} ⁸¹Kr atoms \cdot kg⁻¹_{rock} \cdot ppm⁻¹ U. Production due to neutron capture by ⁸⁰Kr is probably of the same order of magnitude (Lehmann et al. (1993) [250]).

¹ 10⁻³ dis \cdot s⁻¹ \cdot L_{STP}⁻¹ Kr.



FIG. 5.1. Measurements of the modern atmospheric ⁸¹Kr/Kr ratio.

5.1.2. Krypton in hydrology

5.1.2.1. Dating principles

During recharge, water approaches solubility equilibrium with the atmosphere according to the local temperature and barometric pressure at the water table (Fig. 5.2). Gas partitioning at the free air–water interface is described by Henry's law:

$$c_{\rm gas}/c_{\rm water} = H(T, S) \tag{5.1}$$

where

 c_{gas} and c_{water} denote the concentration of a given gas species in the gas phase and water phase, respectively;

H(T, S) is the dimensionless Henry coefficient, which depends on water temperature T and salinity S.

Water in equilibrium with the atmosphere at 10°C and 1 atm contains ~1300 atoms ⁸¹Kr/L water (Table 5.1). This is more than seven orders of magnitude larger than the equilibrium concentration of fission ⁸¹Kr in the crust (see above), indicating that subsurface production of ⁸¹Kr is negligible compared with the groundwater source. In the (unlikely) case of a 100% ⁸¹Kr release rate from the rock into the water filled pore volume, for a rock porosity of 30% and a uranium concentration of 50 ppm, a ⁸¹Kr activity in the water of less than 1‰ of the modern level would result. For a temperature of 10°C, a mean ocean salinity of 35‰ and a total world ocean water volume of 1.4×10^{18} m³, a total ocean Kr inventory of 10¹¹ m³ is estimated, which corresponds to about 2% of the global inventory. Therefore, exchange between ocean and atmosphere (e.g. as a result of changing temperature) has little impact on the atmospheric Kr inventory.

During recharge, Kr (and other atmospheric gases) may additionally be introduced by the dissolution of excess air (Fig. 5.2) (Heaton and Vogel (1981) [211]). In contrast to other gaseous tracer methods, which rely on absolute concentrations of dissolved constituents (such as ${}^{3}H/{}^{3}He$, SF₆ or ${}^{4}He$), ${}^{81}Kr$ and ${}^{85}Kr$ (and ${}^{39}Ar$), gas tracers are insensitive to absolute concentration that is affected by the addition of excess air, degrees of degassing (both in nature and during sampling; see also Chapter 8) and recharge conditions because these methods are based on isotope ratios of the same element (${}^{81}Kr/Kr$, ${}^{81}Kr/Kr$, ${}^{39}Ar/Ar$, etc.).

Kr species/physical characteristic	Value	Unit	Reference
Kr concentration in the atmosphere	1.1	ppm	Aoki and Makide (2005) [244]
Isotopic composition (stable)			
Kr-78	0.35	%	Ozima and Podosek (2002) [251]
Kr-80	2.26	%	Ozima and Podosek (2002) [251]
Kr-82	11.52	%	Ozima and Podosek (2002) [251]
Kr-83	11.48	%	Ozima and Podosek (2002) [251]
Kr-84	57	%	Ozima and Podosek (2002) [251]
Kr-86	17.4	%	Ozima and Podosek (2002) [251]
Kr-85/Kr (2008)	2.4	×10 ⁻¹¹	Winger et al. (2005) [252]
Kr-81/Kr (air)	5.2 ± 0.6	×10 ⁻¹³	Du et al. (2003) [249]; Collon et al. (1997) [245]
Kr-85/Kr-81 (2008)	46.2		Du et al. (2003) [249]; Collon et al. (1997) [245]
Half-life Kr-85	10.76	а	Firestone and Shirley (1996) [253]
Half-life Kr-81	229 000	а	Firestone and Shirley (1996) [253]
Kr. 85 atoms/L water (2008)	57 845		Du et al. (2003) [249];
KI-85 atoms/L water (2008)	57 845		Collon et al. (1997) [245]
Kr-81 atoms/L water (modern)	1253		Du et al. (2003) [249]; Collon et al. (1997) [245]
Kr solubility in water (10°C)	0.081	$cm^{3}_{STP} \cdot cm^{-3}_{water} \cdot atm^{-1}$	Weiss and Kyser (1978) [254]
Diffusion coefficient of Kr in air (20°C)	~0.13	cm ² /s	Weast (1981) [255]
Diffusion coefficient of Kr in water (20°C)	~6.2	$10^{-5} \text{ cm}^2/\text{s}$	Weast (1981) [255]

TABLE 5.1. KRYPTON IN THE ENVIRONMENT: SOME USEFUL NUMBERS

After the air saturated water parcel has moved to depths of greater than about 20 m, the ⁸¹Kr (or ³⁹Ar) exchange with the source (atmosphere) stops and the ⁸¹Kr/Kr ratio decreases due to radioactive decay (Fig. 5.2). According to the exponential decay law, the time elapsed since the water was in contact with the atmosphere can be calculated according to:

$$t_{Kr} = -\frac{1}{\lambda_{\rm s1}} \ln \left(\frac{R_{\rm sample}}{R_{\rm air}} \right)$$
(5.2)

where

 $λ_{81}$ is the ⁸¹Kr decay constant (3.03 ± 0.14 × 10⁻⁶/a); R_{sample} and R_{air} are the ⁸¹Kr/Kr ratios of the sample and modern air respectively (Table 5.1).


FIG. 5.2. Scheme of relevant processes for radio-noble gas dating. Cosmic ray induced production in the atmosphere, gas dissolution in the recharge water due to solubility equilibrium and trapped air bubbles in the quasi-saturated soil zone (excess air) and radioactive decay in the subsurface.

 R_{sample} can also be expressed as $\%_{\text{modern}}$ in relation to $R_{\text{air}} = 100\%_{\text{modern}}$. As underground production can be neglected, the only process other than decay that might change the isotopic ratio in the groundwater system is mixing driven by diffusive/dispersive processes (especially with aquitards) and/or convergent flow (Lehmann et al. (2003) [256]).

The suitable dating range of 0.2×10^5 – 10^6 a (~5 half-lives), the presumably constant and known input concentration, the potential absence of underground production and the fact that dating is based on an isotope ratio (⁸¹Kr/Kr_{total}) which is not sensitive to climate variations and phase transition processes, makes ⁸¹Kr an ideal tracer for dating old groundwater or ice. The fundamental limitation hindering the routine use of ⁸¹Kr in environmental science is the analytical challenge of sampling and measuring ⁸¹Kr concentrations at natural levels.

5.1.2.2. Diffusive exchange with stagnant zones

There are only a few processes that may affect the interpretation of ⁸¹Kr activities in terms of groundwater age. The two most potentially critical processes are: (i) mixing of different water flow path components as for any radiometric dating tracer and (ii) diffusive exchange between the aquifer (active flow zone) and the less permeable adjacent aquitards ('stagnant zones'). In (i), ages calculated on the basis of the radioactive decay law yield a lower age limit for mixtures due to the concave shape of the exponential function (see Chapters 3 and 9). For (ii), diffusive loss of ⁸¹Kr atoms into stagnant zones of the system, on the other hand, dilutes tracer concentration in the active flow zone and results in tracer model ages which are too old compared with pure decay based idealized ages (see also Section 4.9.3). The larger the tracer diffusion accessible volume in relation to the advective system volume,



FIG. 5.3. Diffusive tracer retardation in simplified double porous media. The advective flow system with aperture a and porosity n_a may either be a fracture ($n_a = 1$ in this case) surrounded by a rock matrix (with porosity n_b) or an aquifer between two aquitards, each with thickness b. The process is depicted at a specific location as a function of time increasing from left to right.

the older the tracer model age becomes compared with the hydraulic age. The ratio of tracer model age to hydraulic age is expressed by the effective retardation factor *R* (Małoszewski and Zuber (1985) [257]). Both processes are competitive in terms of their effect on ⁸¹Kr model age (Fig. 5.3). The top image in Fig. 5.3 depicts the evolution of a stable tracer (in blue). The initially tracer free stagnant zone is increasingly penetrated due to the concentration gradient between the active and stagnant zones. Steady state is achieved when concentration gradients are equalized in the whole system. The bottom image depicts the diffusion limit of a radioactive tracer (brown) with a diffusion length L < b/2 (Fig. 5.3 modified after Cook et al. (2005) [208]).

The accessible system volume is tracer (half-life) specific and depends on the effective tracer diffusion coefficient D_{eff} in the pore space of the stagnant zones. For a stable tracer, the diffusion path length L(t) increases steadily and indefinitely as a function of time (Einstein (1905) [258]):

$$L(t) \cong \sqrt{D_{\text{eff}}t} \tag{5.3}$$

For radioactive tracers on diffusion, length at steady state is constrained by the mean lifetime $\tau = 1/\lambda$ of the tracer.

$$L_{\rm ra} \cong \sqrt{D_{\rm eff}\tau} = \sqrt{\frac{D_{\rm eff}}{\lambda}}$$
(5.4)

The situation is illustrated in Fig. 5.3 for an idealized system of parallel flow and stagnant zones with thicknesses a, b and porosities n_a , n_b , respectively. It is assumed that the tracer concentration in

the stagnant zone is initially zero and that sorption reactions are negligible. The retardation factor R is provided by the ratio of the total tracer accessible pore volume to the mobile water volume.

$$R(t) \cong \frac{a \cdot n_{a} + 2 \cdot L(t) \cdot n_{b}}{a \cdot n_{a}}$$
(5.5)

For short flow times and/or slow diffusion L(t) becomes small and the retardation factor IR(t) is ~1 (Fig. 5.3, t_1). With increasing flow time, L(t) increases according to Eq. (5.3) and the tracer delay R(t) increases as well (t_2 - t_3). The steady state situation depends on the half-life of the tracer, the diffusion coefficient and the spacing b between the mobile zones. A diffusion length L(t) or L_{ra} exceeding b/2 (Fig. 5.3, t_{∞} top) will result in a retardation factor R which is simply provided by the ratio of total system porosity to the porosity of the advective flow system (Małoszewski and Zuber (1985) [257]):

$$R \cong \frac{a \cdot n_{\rm a} + b \cdot n_{\rm b}}{a \cdot n_{\rm a}} \tag{5.6}$$



FIG. 5.4. Plots of the logarithm of steady state retardation factor R_{ss} as a function of the logarithm of the thickness of the stagnant zone (b) and the thickness of the transmissive zones (a). The relations are shown for ³H, ¹⁴C and ⁸¹Kr assuming reasonable effective diffusion coefficients and a porosity of the flow zone of 0.3 (Sanford (1997) [207]). The system characteristics of the Great Artesian Basin (Section 5.5) and the Nubian aquifer (Chapter 14) are also indicated in the ⁸¹Kr plot.

For fast decaying radioactive tracers and/or slow diffusion in large impermeable zones ($L_{ra} < b/2$), the retardation factor is limited to a maximal steady state value R_{ss} (Fig. 5.3, Case D bottom).

$$R_{\rm ss} \cong \frac{a \cdot n_{\rm a} + 2 \cdot L_{\rm ra} \cdot n_{\rm b}}{a \cdot n_{\rm a}} \tag{5.7}$$

with L_{ra} given in Eq. (5.3). The mobile and stagnant zones can be interpreted either as aquifers surrounded by aquitards or as fractures within a rock matrix. In the latter case, $n_a = 1$.

Steady state retardation factors for ³H, ¹⁴C and ⁸¹Kr are shown in Fig. 5.4 as functions of the system parameters *a* and *b* for reasonable porosities and effective tracer diffusion coefficients (Sanford (1997) [207]). As deduced above, diffusive retardation is small for thick aquifers (large *a*) with thin aquitards (small *b*; blue area) and increases with increasing *b* for constant *a*. If the extension of the stagnant zones exceeds the tracer diffusion length L_{ra} (the location of the sharp bend on the *b* axes), *R* levels off with increasing *b*. The longer the diffusion length (or half-life of the tracer), the higher the maximal retardation factor for a given geometry of the system. Fractures with small apertures (*a*) and long flow times may produce retardation factors *R* of up to 10³ (Fig. 5.4; Cook et al. (2005) [208]). For several hundred metre thick regional aquifers such as the J-sandstone aquifer in the Great Artesian Basin or the Nubian aquifer in Egypt (see case studies), relatively moderate steady state ⁸¹Kr retardation factors can be expected (coloured boxes in Fig. 5.4). Equations (5.5–5.7) probably, in most circumstances, overestimate the retardation *R* of the tracer. This is because (i) the permeability in 'stagnant zones' in most cases still allows some advective flow and (ii) because timescales may be too short to achieve a steady state equilibrium between the active and passive flow systems.

5.1.2.3. Additional noble gas tracers (⁸⁵Kr, ³⁷Ar and ³⁹Ar)

With the current status of analytical techniques, ⁸¹Kr sampling and measurement require large volume water degassing in the field (see next sections). The collected gas offers the possibility to measure not only ⁸¹Kr but also three other shorter lived noble gas radionuclides that may provide additional valuable information.

Krypton-85

Krypton-85 is the second radioactive Kr isotope that is suitable for groundwater dating for reasons similar to that of ⁸¹Kr. However, the shorter half-life ($t_{1/2} = 10.76$ a) limits the dating range of ⁸⁵Kr to <50 a. Krypton-85 is produced as a fission product of uranium and plutonium decay. Over the past 50 a, the increasing release of ⁸⁵Kr from nuclear fuel reprocessing plants (such as Sellafield, La Hague) has completely overwhelmed the natural activity of about 10^{-7} Bq/cm³_{STP} Kr (Lehmann and Loosli (1984) [259]). The current specific activity in the atmosphere is about 1.4 Bq/cm³_{STP} Kr, which corresponds to an atomic ratio of ⁸⁵Kr/Kr_{total} of 2 × 10⁻¹¹ (see also Fig. 5.10). Air saturated water (10°C, 1 atm) contains about 58 000 ⁸⁵Kr atoms/L water (Table 5.1). Krypton-85 detected in gas extracted from groundwater indicates either the admixture of young groundwater (Althaus et al. (2007) [260]) or, in the case of very old groundwater, can be used as an indication of atmospheric air contamination during sampling and gas purification (Loosli et al. (2000) [261]).

Argon-39

Argon-39 is produced through the interaction of cosmic rays with nuclides of potassium and argon in the atmosphere. The resulting atmospheric equilibrium activity is constant at 1.67×10^{-2} Bq/m³ of air (Loosli (1983) [262]), corresponding to an atmospheric ³⁹Ar/Ar ratio of ~10⁻¹⁵ (anthropogenic sources are neglible). With a half-life of 269 a, ³⁹Ar fills the dating gap between young residence time indicators (CFC, ³H/³He, etc.) and the radiocarbon method (Corcho et al. (2009) [263]; Corcho et al. (2007) [264]). Owing to the very low isotopic abundance of ³⁹Ar, a relatively large amount of water (~2000 L) has to be degassed in the field to obtain a sufficient number of ³⁹Ar atoms. Although first attempts have been made to use the accelerator mass spectrometry (AMS) technique which would reduce this volume (Collon et al. (2004) [265]), and laser atom trap methods are currently being developed (Williams et al. (2010) [266]), the detection of ³⁹Ar is currently only practical using the radioactive decay counting technique (Loosli (1983) [262]). The ³⁹Ar activity of the argon separated from groundwater is measured in high pressure proportional counters in an ultra-low background environment (see Section 5.4.1).

The interpretation of ³⁹Ar activities in terms of groundwater residence time may be complicated because of subsurface production of ³⁹Ar via the ³⁹K(n, p)³⁹Ar reaction (Loosli et al. (1989) [267]). In such rarely occurring cases, more care has to be taken in the interpretation of the data (Purtschert et al. (2001) [268]).

In the investigation of very old groundwater systems, ³⁹Ar can be useful (i) as an indicator of the presence of water components in the age range 60–1000 a which cannot be identified by ³H, ⁸⁵Kr or CFC measurement, and (ii) as a formation specific indicator with a 'flow history memory' of a few hundred years (Purtschert et al. (2001) [268]).

Argon-37

Argon-37 is produced in the atmosphere by cosmic rays in spallation reactions. The resulting specific activity is about 1 mBq/m³_{air} (see also Fig. 5.10), corresponding to an ³⁷Ar/Ar ratio of $\sim 2 \times 10^{-20}$. Because of the short half-life of ³⁷Ar ($t_{1/2} = 35$ d), any atmospheric components would have decayed in water which was underground for more than about half a year. Owing to the similarities in ³⁹Ar and ³⁷Ar production, ³⁷Ar provides a monitor for the strength of underground production of ³⁹Ar. This underground release strength is also an important factor for the interpretation of helium data (Chapter 8).

5.2. LARGE VOLUME GAS SAMPLING TECHNIQUES

5.2.1. Sampling requirements

Although future increases in the detection efficiency of ⁸¹Kr are likely to eventually decrease the sample size to practically transportable amounts (less than tens of litres of water), existing studies of ⁸¹Kr have used gases obtained from 17 t (Lehmann et al. (2003) [256]) to 3 t (Sturchio et al. (2004) [5]) of water, requiring gas extraction in the field. Such a degassing system has to (i) be leaktight to avoid sample contamination by modern air, (ii) have a high extraction yield to reduce sampling and extraction time and also the volume of water necessary, and (iii) be suitable for fieldwork (e.g. be simple, light and robust). The performance of a gas extraction system is determined by the extraction efficiency at a given water flow rate. Maximal water flow rate is limited by the productivity of a well and the pressure drop through a system.

As old water usually has lower tracer concentrations than the atmosphere, a very small amount of air contamination could seriously affect dating results. A rigorous leak check is, therefore, mandatory (see box for an example of a leak check method).

There is a series of technical measures for efficiency optimization if an extraction is carried out in a laboratory or on a research ship (Smethie and Mathieu (1986) [269]). It is also possible to pre-enrich extracted gases in the field (Sidle and Fischer (2003) [270]). However, the operational practicality is more critical for groundwater hydrology, which demands sampling at remote locations.

Method of leak checking

Prior to gas collection, the entire degassing system needs to be evacuated, and carefully checked for leaks. Commonly, the system is evacuated in the field and pressure increase is monitored to evaluate the leak rate of the entire system. To guarantee a leak rate of less than X%, the following conditions have to be fulfilled:

$$\frac{\Delta p}{\Delta t} \cdot V < Q \cdot c \cdot e \cdot X\%$$

where

 $\begin{array}{lll} \Delta p & \text{is the pressure increase (mbar) in time } \Delta t \text{ (min);} \\ V & \text{is the volume of the gas part of the system (L);} \\ Q & \text{is water flux (L/min);} \\ c & \text{is gas content of water (cm}^{3}\text{_{STP}}/\text{L});} \\ e & \text{is extraction yield (%).} \end{array}$

The typical parameters for an extraction system such as those used by Patterson et al. (2005) [43], are a water flow rate of 20 L/min, a gas content of 16 $\text{cm}^3_{\text{STP}}/\text{L}$ (ASW 10°C), an extraction yield of 80% and a volume of the extraction system (including sample container) of 30 L. For <1% air contamination, the pressure increase during a leak test must be less than 0.1 mbar/min or 2.5 mbar/30 min. A leak test of at least 30 min is, therefore, adequate in this case. During a leak test, all gas pumps and compressors should be in operation in a closed circuit (active test).

After a leak test, the system must be flushed with sample water and gas for at least three system volumes. Alternatively, a flushing gas such as helium or pure N_2 may be used.

5.2.2. Physical principles of gas extraction

Physical extraction of ⁸¹Kr from water requires the opposite process of the air equilibration process discussed earlier. According to Henry's law, the amount of gas dissolved in a liquid is proportional to the partial pressure of the gas in equilibrium with the liquid at a constant temperature, i.e. gas and liquid phases in contact will eventually reach solubility equilibrium. At recharge, groundwater dissolves atmospheric gases at atmospheric pressure (\approx 1 bar). By exposing the air saturated water to a gas phase having lower partial pressure of a component than the previous equilibrium, the dissolved gas component becomes repartitioned into the gas phase to attain a new solubility equilibrium. In practice, low Kr partial pressure is achieved either by applying a vacuum so that the partial pressure of any dissolved gas component is lower than that of the atmospheric air previously equilibrated with the sampled groundwater, or by putting the water in contact with a pure and inert gas phase such as He or N₂ in which Kr partial pressure is nominally zero.

The efficiency of gas extraction from groundwater, therefore, depends on: (i) the partial pressure of the gas phase in equilibrium with the water, (ii) the solubility of Kr in the water, and (iii) the rate of gas transfer. The pressure in the gas phase depends on the capability of the pump and the gas flux, which is a function of the water flux and the gas content of the water. The limiting factor of the gas transfer rate from water to gas phase is the rate of gas diffusion in water. The most effective method of enhancing the efficiency of the apparatus is to increase the specific gas–water interfacial surface area by spraying the water or by using a membrane contactor characterized by a large surface area. During these gas extraction processes, the elemental and isotopic ratios of noble gases are expected to fractionate, depending on their solubility. Extraction efficiency of two substances i and r (E_i and E_r) with solubility S_i and S_r are expected to follow a relation:

$$S_{\rm r} \frac{E_{\rm r}}{1 - E_{\rm r}} = S_{\rm i} \frac{E_{\rm i}}{1 - E_{\rm i}}$$
(5.8)

in the case where solubility equilibrium is attained. A theoretical limit on the maximum possible isotopic fractionation is provided by assuming Rayleigh fractionation using the square root of the mass ratio as the isotopic fractionation factor. For an extraction efficiency of >50%, the isotopic fractionation of the 81 Kr/ 84 Kr ratio is expected to be <1%, much smaller than the uncertainty of the current measurements. Thus, the measured isotopic abundance of 81 Kr does not require any correction for isotopic fractionation during sample processing and the same applies to other noble gas radionuclides of interest.

5.2.3. Gas extraction system designs

Two categories of systems have been applied in the field for large volume gas extraction: (i) vacuum extraction using an extraction chamber and (ii) membrane contactors. In both systems, sample water is transferred from the well into the system and discharged after gas extraction (Fig. 5.5). Large particles in the water are filtered out, and water flux and inlet pressure are monitored using a flow meter and a pressure gauge. Check valves are used to prevent flows of water or gas in undesired directions.

In the extraction units, the contact area between the water and the gas phase is increased either by producing small water droplets (spraying) or by means of hydrophobic microporous hollow fibre membrane contactors. In the vacuum cylinder gas extraction system, the groundwater sample is sprayed through nozzles of optimal size (2–6 mm) into a transparent cylinder containing two phases, gas and water, separated by gravity. The water is continuously removed from the bottom of the cylinder at a desired rate regulated with magnetic floating sensors to maintain a range of water



FIG. 5.5. Schematic diagram of water degassing systems: (a) vacuum cylinder extraction; (b) membrane extraction (P0: water inlet pressure; P1: gas extraction pressure; P2: gas pressure in the sampling container).

levels while the gas–vapour phase is transferred to a sample container by a compressor (Fig. 5.5(a)). The hydrophobic microporous hollow-fibre membrane contactor has a cylindrical shape, and consists of two volume sections partitioned by the membrane material. Since the membrane is hydrophobic, it will not allow liquid water to pass through the pores, and diffusion of gas from the liquid water into the gas-filled pores is the mechanism by which gases are extracted from the groundwater (Wiesler (1996) [271]). Because water and gas phases are separated by the membrane instead of gravity, water level tuning is not required. The gas phase in contact with water is maintained at a pressure of 20–150 mbar (P1)², and the gas released from the water is pumped via pump/compressor into pre-evacuated sampling containers (P2, Fig. 5.5). The gas handling portion of the extraction apparatus is commonly constructed of stainless steel tubing connected with stainless steel Swagelok fittings. Pressure gauges monitor the sampling condition (P1, pressure of the gas phase in equilibrium with water) and gas yield (P2, total pressure of the sampled gas).

5.2.4. Specific parameters, remarks and extraction efficiencies

5.2.4.1. Vacuum cylinder extraction system

The extraction cylinder is 20 cm in diameter and 100 cm in height, made of an acrylic tube with PVC end caps. For air saturated water and a water flux of 20 L/min, a typical extraction pressure of 20–50 mbar is reached (Fig. 5.6). This leads to an extraction efficiency of 80–90% for a water temperature of 10°C (Kropf (1996) [272]). The flow rate and, thus, the sampling capacity of the system is primarily limited by the pump rate of the drainage pump (WP2), which is about 30 L/min.

A number of technical features have been devised for enhanced sampling efficiency with minimal problems. An additional centrifugal pump (WP1) is used to increase inlet water pressure (up to 26 bar), and thus the flow rate, to supplement the pressure drop (4–8 bar) caused by the spray nozzle. The differential range of attainable pressure is widened significantly, both on the vacuum (20 mbar) and pressure side (12 bar), by installing two pump/compressors of different pressure capacities in series. An emergency stop function is also installed, which is triggered either by manual switching or by a forbidden physical parameter (such as rising water levels in the extraction cylinder) to protect the system and the sample.

The vacuum cylinder extraction system, which has been used successfully in several field campaigns for large volume ³⁹Ar, ⁸⁵Kr and ⁸¹Kr sampling (Corcho et al. (2007) [264]; Lehmann et al. (2003) [256]; Sturchio et al. (2004) [5]), was developed at the Physics Institute at the University of Bern. A similar apparatus has been used in oceanography (Smethie and Mathieu (1986) [269]) and is currently in operation at other institutes or environmental research companies (University of Freiburg, University of Leipzig, Hydroisotop GmbH).

5.2.4.2. Extraction system using membrane contactors

The availability of commercially available membranes facilitated the construction of compact field degassing systems (Ohta et al. (2009) [273]; Probst et al. (2007) [274]). The membrane contactor currently used at the University of Illinois in Chicago (Liqui-Cel® Extra-Flow 4×28) handles water flow rates up to 30 L/min. For air saturated water with a water flux of 20 L/min at a typical vacuum pressure of 130 mbar, the extraction efficiency is 80–90% for Ar and O₂ and >70% for Kr. No significant Kr isotopic fractionation has been observed through this extraction process. The operating pressure of the vacuum is limited to >65 mbar to avoid damaging the membrane structure, which sets a theoretical limit on extraction efficiency. The original system (EDGAR: Extraction of Dissolved Gases for Analysis of Radiokrypton) weighed about 180 kg (Probst et al. (2007) [274]), whereas a recent modification

² Depending on the performance of the pump system and the water and gas fluxes, respectively.



FIG. 5.6. Vacuum cylinder apparatus for field gas extraction of dissolved gases. Components indicated with dotted lines are optional (see text). In the water part (left side), the water is filtered and transferred to the extraction cylinder from where it is pumped out after degassing. An emergency valve (EV1) protects the cylinder from overflow (closed when the water level reaches LE). The gas is extracted with a vacuum pump (GP1) compressed (K1) into the sampling container. An additional compressor (K2) can be attached if higher pressures are required because of high gas contents and/or small sample containers ($P_{max} \sim 15$ bar).

halved the size. Smaller membrane contactors are now available with lower water flow capacity (<5 L/min), and may be applied for smaller sampling (Ohta et al. (2009) [273]).

5.2.5. Optimal design of gas extraction units

The systems described above are complementary, and a suitable or optimal gas extraction method needs to be adjusted according to the local environmental conditions at the sampling site, the required sample size and the isotope of interest. Table 5.2 summarizes the most important features, benefits and disadvantages of the two systems.

5.3. GAS PREPARATION AND PURIFICATION

5.3.1. Introduction

Existing analytical methods for ⁸¹Kr (and ³⁹Ar) require relatively large quantities (~15 μ L) of pure Kr gas. The gas phases extracted in the field have to be processed and purified in the laboratory. Alternatively, an initial noble gas pre-enrichment can already be achieved in the field (Sidle and Fischer (2003) [270]). The composition of dissolved gas in groundwater can be highly variable (Fig. 5.7). The air saturated seepage water may acquire different amounts of excess air through the partial or complete dissolution of air bubbles that are trapped at the capillary fringe in the unsaturated soil zone. Carbon dioxide can be accumulated from different sources in the unsaturated (biogenic CO₂) or

Benefits	Disadvantages						
Extraction chamber							
Insensitive to chemical and physical water composition (pH, temperature, hydrocarbons, suspended matter, etc.)	Requires low extraction pressure and is, therefore, more sensitive to leaks						
Easy to repair by experienced personnel in case of breakdown (important in remote areas)	Careful leak testing and set-up requires experienced personnel						
Operational for a large range of water fluxes	Relatively high flow resistance may limit water flow rate						
Allows a low extraction pressure, thus higher extraction efficiency	Not commercially available and, therefore, expensive to construct						
Benefits	Disadvantages						
Membrane contactors							
Commercially available membrane contactors, relatively inexpensive Modular: several contactors can be combined in parallel (increased water flux) and/or in series (increasedextraction efficiency)	Sensitive to chemical and physical water composition:						
	Not suitable in the presence of substances which reduce the surface tension of water						
	Not suitable for a high temperature environment (i.e. >70°C)						
Compact and relatively easy to operate in the field	Suspended or precipitated matter may clog the pores						
Low inlet water pressure facilitates high water flux; operational over large flux range	A damaged membrane requires a relatively complex regeneration processes						

TABLE 5.2. COMPARISON OF DIFFERENT GAS EXTRACTION SYSTEMS

the saturated zone (biogenic, chemogenic or thermogenic). Under reducing conditions, O_2 is consumed and CH_4 can be produced by methanogenesis or CO_2 reduction (Klass (1984) [275]). As a result of denitrification, N_2 is another common subsurface gas source in many aquifers. Thus, a Kr purification system must be able to separate Kr efficiently from large quantities of gas of variable composition. In the case of multitracer studies, including, for example, additional ³⁹Ar measurements, a combined Kr and Ar purification process is necessary. There are several methods of separating noble gases from gas mixtures. Some of the most common processes used in large volume Kr–Ar purification systems are outlined below.

Distillation

Isolating and/or enriching components from a gas mixture based on differences in condensation points of the gas components (such as cooling traps for CO_2 or water vapour removal from the gas mixture).

Adsorption

Separating gas mixtures using microporous solids (adsorbents) that have strong affinities for one or more of the components in the mixtures at variable temperature and partial pressure.



FIG. 5.7. Composition of atmospheric air (\bigstar) relative to the Kr concentration in air and subsurface processes (arrows) affecting the composition of dissolved gases in groundwater.



FIG. 5.8. Krypton sampling and purification techniques as a function of water sample volume (L). The reduction in the required sample volume is triggered by the increased sensitivity of analytical methods for ⁸¹Kr detection.

Absorption

Selective physical solution or chemical bonding of chemically active species, mainly used to remove substances other than noble gases. The process can be reversible (e.g. oxidation of copper to remove O_2 and the subsequent reduction of the CuO using H_2 gas) or irreversible (such as with Ti-getters).

New gas purification techniques and materials (membranes, nanotubes, cation exchanged zeolites, etc.) have recently been developed, and as the efficiency of ⁸¹Kr measurements increases and required sample size decreases, separation and purification techniques will converge towards techniques

that are in use for stable noble gas isotopic analyses (Beyerle et al. (2000) [276]). The procedures described here or elsewhere in recent literature (Loosli and Purtschert (2005) [277]; Smethie and Mathieu (1986) [269]; Yokochi et al. (2008) [278]) are, therefore, to be regarded as a 'snapshot' of the present capability. In the following sections, two selected large volume noble gas purification systems will be presented in more detail.

5.3.2. Purification system at the University of Bern

The low level counting laboratory at the Physics Institute of the University of Bern has a long history in the separation and analysis of noble gas radionuclides through low level counting (LLC) (Loosli (1983) [262]; Loosli et al. (2000) [261]; Loosli et al. (1986) [279]; Loosli and Purtschert (2005) [277]). The required amount of gas extracted from groundwater for LLC is constrained by the decay rate of the isotope of interest. Measuring ⁸¹Kr in groundwater via decay counting is not feasible, but LLC was used for the first detection of ⁸¹Kr in the atmosphere (Loosli and Oeschger (1969) [247]). The powerful combination of ⁸⁵Kr and ³⁹Ar dating in hydrology (Corcho et al. (2007) [264]; Purtschert (2008) [280]) requires purification of both Ar and Kr. If Ar or Kr is exclusively of interest, the procedure can be optimized and simplified accordingly. With the separation system of the LLC laboratory in Bern, samples with a gas volume between ten (for ⁸⁵Kr measurements) and several hundred litres can be processed serially in portions of about 2 L.

Combined Ar–Kr separation procedure

The gas is transferred from the sample cylinder into a first cooling trap filled with activated charcoal (AC). Using the bulk gas as a carrier, water vapour and CO₂ are removed using a molecular sieve 5A, and O₂ is removed by oxidation of Cu to CuO in a Cu furnace at 600°C. The sample is then released into a buffer volume, and injected as a sequence of 2 L aliquots into the gas chromatograph (GC) separation system. The two large packed columns of the GC (1 m long, 7 cm diameter, T = 20°C) are filled with AC and with a molecular sieve 5A, respectively, and sequentially. Helium is used as a carrier gas, and the gas effluent is analysed by a thermal conductivity detector. The fractions containing Ar and Kr are collected separately in cooling traps filled with AC at N₂(l) temperature. This procedure separates Ar from Kr, so that the Kr in the Ar fraction is reduced by a factor of at least 10⁴ to eliminate present day atmospheric ⁸⁵Kr activity. The argon fraction is then passed a second time through the GC columns and finally purified from any remaining traces of O₂ and N₂ in a Ti-furnace at 800°C. If present, a fraction of CH₄ is collected together with Kr because the Kr and CH₄ retardation times overlap if more than 1 cm³ STP CH₄ was present in the original sample. The final Kr purification is done with a separation system optimized for Kr. Any traces of radon (released, for example, from AC in the system) are removed in a cold finger filled with glass pellets at N₂(l) temperature.

Krypton purification

Krypton typically extracted from 300–500 L of water, or from the residual gas from the Ar–Kr system described above (the Kr enriched portion), is separated by three GC separation steps. If only Kr (for ⁸⁵Kr or ⁸¹Kr measurements) is of interest, the procedure starts at this point (Collon et al. (2000) [281]).

The sample gas is exposed to a molecular sieve (5A (MS1)) bed for water vapour and CO₂ removal and subsequently adsorbed on an AC cold finger (AC1).

The trap (AC1) is then heated to room temperature, and the desorbed gases (mainly N_2 and Ar) are pumped away during the first five minutes. The trap is then flushed with the carrier gas (He) and the effluent is monitored using a thermal conductivity detector. After the Ar(O₂) and N₂ peaks have



FIG. 5.9. Krypton purification system (for details, see text). Pure Kr is obtained by several GC separation steps (a). Krypton is then transferred into a cooling trap (AC2), purified, mixed with P10 gas, and finally fed into the proportional counter (b).

passed, the two way valve is switched to divert the gas flow through the second trap (MS2) filled with a 5A molecular sieve cooled at N₂(l) temperature. From this trap, the desorption procedure is repeated to further purify and freeze Kr in the third cooling trap (AC2), filled with AC. In each step, the gas volume is reduced by a factor of ~10 and the remaining gas volume in AC2 is about 20–100 μ L STP (Collon et al. (2000) [281]). AC2 is then removed from the system and connected to a commercial GC system (Varian Star 3400) where the Kr is further purified, mixed with a P10 mixture as a quench gas (90% argon and 10% CH₄) and finally transferred into the low level counter for activity measurement in the underground laboratory (Fig. 5.9(b)). If the Kr and CH₄ abundances in the sample are comparable, they can be easily separated and the final amount of recovered Kr is determined from the area of the Kr peak. If the methane and Kr peaks cannot be separated, the Kr content in the counter gas has to be measured after the activity measurement by mass spectrometry.

Large CH_4 concentration in the sample gas requires further measures in order to purify Kr. For example, CH_4 can be used as a carrier gas for GC separation (Sidle and Fischer (2003) [270]). In the laboratories of the University of Bern, CH_4 is oxidized in a CuO coated furnace at 800°C, followed by the separation of the resulting CO_2 and H_2O .

5.3.3. Purification system at the University of Illinois, Chicago

Major constituents of the atmosphere, N₂, O₂ and Ar, have much higher vapour pressure than Kr. Consequently, cryogenic distillation enriches the residual phase in Kr. Large scale cryogenic distillation with refined engineering control has indeed been the most widely applied method of producing pure gas substances from the atmosphere. Eliminating sophisticated engineering controls, a simple method of cryogenic Kr enrichment at an easily attainable constant temperature (77 K) was developed at the University of Illinois, Chicago (Yokochi et al. (2008) [278]). Pure Kr is obtained through subsequent GC separation and Ti-gettering. The system uses a quadrupole mass spectrometer (QMS) to monitor gas effluent composition during separation, which enables (i) small scale cryogenic distillation in a controlled manner, (ii) gas chromatographic separation of parts per million by volume (ppm_v) level

of Kr from a significantly large quantity of gas (up to a few litres), and brings (iii) the applicability of the method to natural groundwater samples characterized by variable chemical compositions.

After H_2O and CO_2 removal using a molecular sieve 4A, sample gas is condensed in an empty container at liquid N_2 temperature, then distilled at that temperature assisted by a vacuum compressor. The rate of the cryogenic distillation is about 3 L/min for a system dominated by N_2 , and 0.5 L/min for a system dominated by O_2 . The N_2/Ar ratio of the distillation gas effluent is continuously monitored to determine the progress of the distillation based on a model calculation assuming gas–liquid equilibrium partitioning. Efficient separation of Kr and CH₄ from Ar, O_2 and N_2 can be achieved for up to a few litres of the distillation residue gas by using an AC column (AC2) at room temperature. The Kr peak following these major species overlaps with the peak tails, but the use of a QMS for monitoring gas composition enables identification and further selective processing of the Kr enriched portion. A molecular sieve 5A separates Kr from CH₄ (up to a few hundred cubic centimetres STP) at low temperature (around -20° C). Pure Kr is collected in a small (0.7 cm³) stainless steel container filled with AC.

5.4. DETECTION METHODS OF NOBLE GAS RADIONUCLIDES

Despite their excellent tracer properties, radioactive noble gases are still not used on a routine basis in environmental science; for ⁸¹Kr, only three field investigations have been completed to date (Lehmann et al. (1991) [282]; Lehmann et al. (2003) [256]; Sturchio et al. (2004) [5]). The main issue limiting the widespread use of noble gas radionuclides has been a lack of convenient analytical methods to measure these isotopes at natural concentrations. The problem is depicted in Fig. 5.10, where typical values of atmospheric activities, concentrations and specific isotope ratios are plotted as a function of the half-lives of corresponding noble gas isotopes. The numbers can vary depending on the specific situation, but correspond roughly to modern waters under average environmental conditions. First, the extremely low isotopic abundances (<10⁻¹¹) of these noble gas radionuclides far exceed the dynamic range of conventional gas source mass spectrometers. The activities in 1 L of water for ³⁷Ar, ³⁹Ar, ⁸⁵Kr and ⁸¹Kr are 10⁻⁴, 10⁻¹, 10⁻³ and 10⁻⁷ mBq, respectively. While the ⁸⁵Kr activity of a modern sample



FIG. 5.10. Typical values of atmospheric activities (squares), concentrations (circles) and specific isotope ratios (e.g. ⁸¹Kr/Kr; triangles) dissolved in 1 L of water at 10°C versus half-life of noble gas radionuclides (Lehmann and Loosli (1984) [259]).

can be measured in a number of laboratories worldwide, ³⁹Ar and ³⁷Ar can currently only be measured in one underground laboratory at the University of Bern, using Ar extracted from a few tons of water. As seen in Fig. 5.10, the specific ⁸¹Kr activity is out of range of any reasonable sampling and decay counting system, thus ⁸¹Kr has to be measured by other atom counting methods. AMS (Collon et al. (2000) [281]) and new ultrasensitive atom counting methods (Chen et al. (1999) [283]; Du et al. (2003) [249]) have been applied in studies of ⁸¹Kr in hydrology. The analytical methods that are suitable for noble gas radionuclides, particularly ⁸¹Kr, will be briefly discussed in the following section.

5.4.1. Low level counting

For decades, LLC was the only method for detecting radioisotopes of Ar and Kr at atmospheric levels. The first determination of ⁸¹Kr activity in the atmosphere was undertaken using proportional counting with 5 L of pre-bomb Kr (Loosli and Oeschger (1969) [247]). The current LLC laboratory at the University of Bern is shown in Fig. 5.11 (Acosta-Kane et al. (2007) [284]). The laboratory is located at a depth of 35 m, providing a reduction of the muon flux by a factor of ~10. The laboratory walls utilize special concrete selected for its low radioactivity content to minimize gamma ray flux within the laboratory. The proportional counters are built of high conductivity, oxygen free Cu and filled with the sample gas at a pressure of 2–30 bar, then placed in a cylindrical lead shield 5 cm thick. Only a fraction of the particle decay energy is released within the counter before it reaches the counter wall. The deposited energy increases with increasing pressure and is recorded by a 7-bit multichannel analyser (MCA) with a linear energy range of 0–35 keV. For further background reduction, the proportional counter is constructed with low background materials and uses an anti-coincidence proportional counter to reduce background. The small volume of the counters reduces the background



FIG. 5.11. Schematic of the set-up utilized to measure noble gas radionuclides at the Low Level Counting Underground Laboratory at the University of Bern. For ⁸⁵Kr measurements, the counters are filled with a P10 mixture (10% methane, 90% argon) at pressures in the range of 2–10 bar. The measurements are performed at a depth of 35 m. Low activity lead shielding and an anti-coincidence arrangement provide a further reduction in the background count rate.

because the counter surfaces, thus the influence of self-activity of the counter material (mostly Cu), are smaller. The assembly is inserted in a second, larger cylindrical proportional detector, which acts as an anti-coincidence counter. The passive shielding is complemented by an external lead shield approximately 12 cm thick. The lead shields were built using lead from from pre-industrial shipwrecks with very low intrinsic ²¹⁰Pb activity.

Gas purity may change slightly from one sample to the next; gas quality may also slowly worsen over a counting time of several weeks. To be able to apply exactly the same gas multiplication factor, 8 keV X ray radiation of Cu is induced in the wall of the counter by an external ²⁴¹Am source and fixed for each counting system at a given channel of the energy spectrum.

For ³⁹Ar, a precision of about 5% modern is reached for young samples, corresponding to an age uncertainty of ± 20 a. For ages comparable to the ³⁹Ar half-life, an error of about 7% modern is typical, corresponding to about ± 30 a. The limit of dating corresponds to a detection limit of about 5% modern, which results in an age indication of more than 1000 a (Pearson Jr. et al. (1991) [285]). The modern ⁸⁵Kr/Kr ratio can be measured with a precision of better than 3% using 5–10 L of atmospheric air or 200–500 L of water, respectively.

5.4.2. Accelerator mass spectrometry

When analysing long lived isotopes, atom counting has a number of advantages over decay counting (Collon et al. (2004) [265]). The efficiency and speed of atom counting is not fundamentally limited by the long half-lives of isotopes, nor is it affected by radioactive backgrounds in the environment or in samples.

In an AMS analysis, ions are first produced from a sample in an ion source, and are then passed through a first set of low energy analysing magnets in order to select those with the correct charge to mass ratio. The selected ions are accelerated and, in some cases, passed through a stripper foil which largely removes molecular isobars. The surviving ions are passed through an additional series of magnetic and electrostatic analysers before being further analysed and counted in a detector system (Fig. 5.12). The high sensitivity and selectivity of the method makes it possible to measure a trace nuclide at a rate of several counts per hour from a micorampere primary beam ($\sim 10^{16}$ ions/h) (Collon et al. (2004) [265]).

The main technical problems for the detection of ⁸¹Kr with AMS arise from (i) the inability of noble gases to form negative ions, which excludes the application of tandem accelerators, and (ii) the high background due to isobaric, stable and abundant ⁸¹Br. This was recently overcome by Collen et al. (1997) [245] using the full stripping technique. Once all of the electrons are removed, ⁸¹Kr³⁶⁺



FIG. 5.12. Schematic of the accelerator mass spectrometry experimental set-up at the National Superconducting Cyclotron Laboratory, Michigan State University (Collon et al. (1997) [245]).

(Z = 36) can be cleanly separated from ⁸¹Br³⁵⁺ (Z = 35). The AMS measurements of ⁸¹Kr in atmospheric Kr were performed using the K1200 Superconducting Cyclotron at Michigan State University, which accelerated ions to an energy (3.6 GeV) high enough for efficient full stripping. After the acceleration in the cyclotron, the ⁸¹Kr¹⁷⁺ ions were passed through a Be foil (18.8 mg/cm²), which provided a 70% stripping efficiency to reach the 36+ charge state. The fully stripped ⁸¹Kr³⁶⁺ was then separated from the ⁸¹Br³⁵⁺ using the A1200 mass spectrometer, and detected with two Δ E–E telescope detectors (Collon et al. (1997) [245]).

The nuclear reaction products induced by the high ⁸¹Br¹⁷⁺ background in the stripper foil heavily dominated the final spectrum and had to be suppressed by several orders of magnitude before ⁸¹Kr in natural samples could be detected. As Kr and Br have very different melting temperatures (-156.6° C and -7.2° C, respectively), Br in the sample was suppressed by freezing the sample with liquid nitrogen. In addition, tests revealed that the largest suppressor of ⁸¹Br was the support gas used in the ion source. By using Ar as a support gas, reductions in Br contamination by two orders of magnitude were obtained (Collon et al. (1999) [286]). These steps opened the door to possible measurements of ⁸¹Kr below the natural level of 5×10^{-13} . This AMS set-up was used to perform ⁸¹Kr dating of groundwater samples (Collon et al. (2000) [281]) and to compare pre-bomb and post-bomb abundances of atmospheric ⁸¹Kr/Kr (Collon et al. (1999) [286]).

5.4.3. Atom trap trace analysis

In atom trap trace analysis (ATTA), an atom of a particular isotope is selectively captured by a laser trap and then detected by observing its fluorescence while in the trap (Chen et al. (1999) [283]). A magneto-optical trap (MOT) — a type of robust and efficient atom trap — is used as a selective concentrator (Chen et al. (1999) [283]; Du et al. (2003) [249]). When the laser frequency is tuned to within a few natural line widths of the low frequency side of the targeted isotope resonance, only atoms of this particular isotope are trapped. Atoms of other isotopes are either deflected before reaching the trap or are allowed to pass through the trap without being captured. This method allows for the counting of single atoms with a high signal to noise ratio and, since selectivity depends exponentially on the number of photons detected in a burst, also ensures superb selectivity. Indeed, ATTA is practically immune to contamination from other isotopes, elements or molecules.

The vacuum system consists of the following components: the sample reservoir, the source chamber, the transverse cooling chamber and the trap chamber. A getter pump in the source chamber removes reactive gases, such as hydrogen, water, etc. from the vacuum system while leaving the Kr sample intact. Either a Ti-sapphire ring laser system or a diode laser system can be used to generate the 811 nm light needed to trap Kr atoms in the metastable 5 s [3/2]2 level by repeatedly exciting



FIG. 5.13. Schematic layout of the krypton ATTA-2 apparatus. Metastable krypton atoms are produced in the discharge. The atoms are then transversely cooled, slowed and trapped by laser beams, shown as solid red arrows. The total length of the set-up is about 2.5 m (Lu and Mueller (2010) [287]).



FIG. 5.14. Signal of a single ⁸¹Kr atom. The background is due to photons scattered off the surrounding wall of the vacuum chamber (Du et al. (2003) [249]).



FIG. 5.15. Correlation between the ⁸⁵Kr/⁸¹Kr ratios measured using ATTA and ⁸⁵Kr/Kr ratios measured using LLC. Line through open symbols: measured relation for modern Kr (Du et al. (2003) [249]). Solid symbols: ⁸¹Kr depleted values for ancient groundwater samples (Sturchio et al. (2004) [5]). Ratios of equal age are indicated by dashed lines.

the 5 s [3/2]2 - 5 p [5/2]3 cycling transition. A novel feature of the system is that it can be switched into a mode that recirculates the Kr atoms repeatedly through the system, which dramatically improves counting efficiency.

In an ATTA analysis, a Kr gas sample is injected into the system through a discharge region (Fig. 5.13), where approximately 1×10^{-3} of the atoms are excited into the metastable level 5s [3/2]2 via collisions with energetic electrons and ions. The thermal (300 K) atoms are then transversely cooled, decelerated using the Zeeman slowing technique and captured into an MOT (Fig. 5.13). The MOT can capture the abundant ⁸³Kr (isotopic abundance = 11.5%) at a rate of 1×10^{9} /s. Since an atom typically lasts 0.5 s in a trap before being bumped out in collisions with thermal background atoms or molecules, rare atoms are not accumulated in the trap; instead, they are usually captured and counted one at a time. A single trapped atom can be unambiguously observed with a signal to noise ratio of 40 by detecting its strong fluorescence induced by the trapping laser beams (Fig. 5.14).

The capture rates for ⁸¹Kr and of stable ⁸³Kr differ by 11 orders of magnitude. At present, the ⁸¹Kr/⁸³Kr ratio cannot be measured directly due to an inadequate dynamic range in the ATTA

detector system. Instead, a controlled amount of ⁸⁵Kr is introduced into the sample and the ⁸¹Kr/Kr ratio is determined based upon two measurements: the ⁸⁵Kr/⁸¹Kr ratio measured using ATTA and the ⁸⁵Kr/Kr ratio measured using LLC (Fig. 5.15). This ratio was measured for modern atmospheric Kr (Du et al. (2003) [249]). The obtained linear relation is the reference zero age line for ⁸¹Kr dating. The detection limit depends on the sampled Kr volume, the resulting ATTA and LLC counting statistics and the reliability of the spiking process. The current detection limit of ~5%_{modern} for ~2000 L water samples will likely be reduced in the near future with the next generation of ATTA instruments (see below).

An ATTA system developed at Argonne National Laboratory has been used to analyse ⁸¹Kr and ⁸⁵Kr in the atmosphere and in groundwater (Du et al. (2003) [249]; Sturchio et al. (2004) [5]). The counting efficiency of this second generation system (ATTA-2) was ~10⁻⁴, with a required Kr sample size of 50 μ L, corresponding to a water volume of about 3000 L. The elevated ⁸⁵Kr/⁸¹Kr ratios measured for six samples from the Nubian aquifer compared with the modern reference line (Fig. 5.15) are due to radioactive decay of ⁸¹Kr and were directly converted to groundwater ⁸¹Kr model age (Sturchio et al. (2004) [5]). As the absolute calibration of ⁸¹Kr/⁸⁵Kr and, thus, the ⁸¹Kr/Kr ratio was not feasible up until now, the atmospheric value measured by ATTA is not indicated in Fig. 5.1.

On the basis of the knowledge and experience provided by the ATTA-2 set-up, an optimized ATTA-2 apparatus is currently under development at several institutions, including the Argonne National Laboratory (Lu and Mueller (2010) [287]). Improvements in trapping and counting efficiency by two orders of magnitude aim to reduce the sample size required to less than 10 kg of water or ice (Fig. 5.8). This will considerably facilitate the gas sampling and purification procedures and finally open ⁸¹Kr dating method applications to a wide field of possibilities, thus answering many scientific questions.

5.4.4. Resonance ionization mass spectrometry

For many years, extensive efforts have been undertaken to measure ⁸¹Kr using laser resonance ionization mass spectrometry (RIS) (Lehmann (2000) [288]; Lehmann et al. (1985) [289]; Thonnard et al. (1987) [290]). Similar to the ATTA technique, Kr atoms are selectively excited and ionized with laser pulses. This process is very element sensitive, but generally not isotope selective, because the bandwidth of the pulsed ionization lasers is larger than the isotope effects in the Kr spectra. Isotope selectivity is achieved in combination with mass spectrometers. However, the very small isotope ratio requires rather complicated isotopic pre-enrichment procedures prior to the final measurement. Despite some encouraging results (Lehmann et al. (1991) [282]), problems remained unsolved and the RIS method has so far not successfully been applied to a multisample field investigation.

5.5. FIRST ATTEMPTS AT ⁸¹Kr DATING: THE MULTITRACER COMPARISON IN THE SOUTH-WESTERN GREAT ARTESIAN BASIN

5.5.1. Introduction

A pioneering attempt to use ⁸¹Kr for groundwater dating was performed at the Milk River aquifer in Canada at one selected well (Lehmann et al. (1991) [282]) as discussed in Chapter 11. Although the obtained ⁸¹Kr/Kr ratio measured using the RIS technique was indistinguishable within uncertainties in the ⁸¹Kr/Kr ratio of modern krypton, it was encouraging that a maximum ⁸¹Kr tracer age of 140 ka could be estimated (Lehmann et al. (1991) [282]), consistent with findings from ³⁶Cl/Cl data (Nolte et al. (1991) [291]).

In the south-western Great Artesian Basin of Australia, ⁸¹Kr was applied for the second time in a groundwater study but for the first time at more than one sampling location (Lehmann et al. (2003) [256]). Sites were chosen on the basis of hydraulic age estimates and ³⁶Cl data, which indicated groundwater ages on the order of several hundred thousand years (Love et al. (2000) [292]). The ⁸¹Kr/Kr

ratios of four wells were measured using the AMS technique (Collon et al. (2000) [281]; Section 5.4.2) and for the first time allowed for a check of the applicability of ⁸¹Kr methods and a cross-check with tracer ages and conclusions derived from ³⁶Cl and ⁴He data. The comparison of all data in such a multitracer study yields more information about the flow system than is possible from single tracer measurements. Moreover, limitations and uncertainties about individual tracer methods can be reduced and possibly quantified. Specifically, the following issues are addressed in the following pages.

Krypton-81 dating is a new method and its validity must be demonstrated in comparison to the more established ³⁶Cl and ⁴He methods. Although theoretical considerations indicate that variations in ⁸¹Kr input activity and underground production should be low (Lehmann et al. (1993) [250]), this has to be verified in field studies. The strength of diffusive exchange between an aquifer and its surrounding aquitards is another potential problem that needs further investigation (Section 5.1.2.2).

For ⁴He, the most critical factor is quantification of the local accumulation rate, which is composed of an 'on-line' in situ production rate (easy to calculate) and an influx of helium that was produced either external to the aquifer (Torgersen and Clarke (1985) [293]; Torgersen et al. (1992) [294]; Torgersen and Ivey (1985) [93]) or helium that accumulated 'off-line' in the past which is now being released within an aquifer via diffusion from rocks into pore spaces (Solomon et al. (1996) [295]; Chapter 8).

For ³⁶Cl dating, the 'initial value problem' (Davis et al. (1998) [296]) concerns the ³⁶Cl/Cl ratio at the recharge area's geographical location, as well as an estimate of the Cl concentration of recharging water, which depends strongly on prevailing climatic conditions which may change as a function of time. During groundwater flow, subsurface processes other than radioactive decay may alter the number of ³⁶Cl atoms and/or the number of Cl atoms dissolved in the water (Chapter 6).



FIG. 5.16. Location map of the south-west margin of the Great Artesian Basin, showing the locations of wells for ³⁶Cl dating (\bullet) (Love et al. (2000) [292]) and the four sites that have been sampled for ⁸¹Kr measurements (\star) (Lehmann et al. (2003) [256]). The shaded areas indicate the sandstone aquifer outcrop. The dashed line represents the transition from unconfined to confined conditions (where the water level of the aquifer is above the overlying Bulldog Shale).

The part of the Great Artesian Basin investigated here (see below) provides unfavourable conditions for the interpretation of ³⁶Cl data due to high and variable evaporation rates and the occurrence of subsurface Cl sources. The systematic use of helium as a dating tool is also complicated by the presence of different helium sources (Torgersen and Clarke (1985) [293]). It is, therefore, an ideal area to demonstrate the interrelation between different tracer methods in such 'real world scenarios' and the potential of multitracer studies. The intention is not to favour any of the applied methods or to explain the flow system in this hydrologically complex part of the Great Artesian Basin. Significantly more data would be required, including ⁸¹Kr, to reach this goal.

5.5.2. Study area

The study area is located in the Great Artesian Basin south-western flow system of the Eromanga Basin. Piezometric contours indicate that the major direction of groundwater flow is from the western margin towards the south-east and east (Fig. 5.16). Chlorine-36 dating was previously performed along two transects and based on these data the test sites for ⁸¹Kr measurements were chosen (Love et al. (2000) [292]). The southernmost site (RC) was sampled because other sites along the northern transect were inaccessible due to inclement weather and poor road conditions.

All wells tap the J-K sandstone aquifer that is overlain by the 200–400 m thick Bulldog Shale aquitard. The transects start in the outcrops and unconfined parts of the aquifer. Further downstream, the aquifer becomes confined or eventually artesian (Love et al. (2000) [292]).

5.5.3. Krypton-81 groundwater ages

The four wells, RC, OD, DH and WC (Fig. 5.16), were sampled during a field campaign in 1998 in collaboration with the Department of Water, Land and Biodiversity Conservation of South Australia, the Institute of Isotope Research Vienna (AMS measurements) and the University of Bern (sampling and sample preparation). The project was partly supported by the IAEA within the framework of a research programme called "Isotope Techniques for the Assessment of Slow Moving Deep Groundwaters". About 16 t of water was degassed in the field and the extracted gas was processed in the University of Bern laboratories according to the procedures explained above. The purified Kr samples (~0.5 cm³_{STP}) were shipped to the AMS laboratory at Michigan State University for ⁸¹Kr/Kr ratio determination.

Measured ⁸¹Kr activities expressed in terms of the air normalized ratio (⁸¹Kr/Kr)_{sample}/ (⁸¹Kr/Kr)_{modern air} range from 51% to 30%_{modern}. A simple age calculation using the exponential law for radioactive decay yields ⁸¹Kr model ages of between 230 and 400 ka (Table 5.3), in agreement with expectations from ³⁶Cl data (Love et al. (2000) [292]). The uncertainty in calculated groundwater tracer age is about 10–20% because of the analytical error in these first ⁸¹Kr measurements using cyclotron AMS. Contamination during sampling was excluded through ⁸⁵Kr measurements carried out on subsamples of the same gas used for AMS.

These ⁸¹Kr model ages are piston flow ages and, thus, neglect dispersion in the aquifer, possible diffusive exchange with aquitards and any underground production of ⁸¹Kr. The effect of dispersion is minor for tracers with a constant input because the concentration gradient is small in the direction of flow (in contrast to peak shape inputs as for ³H). For reasonable dispersivities (Gelhar et al. (1992) [297]), the effect would lead to an underestimation of groundwater age on the order of <15% for ⁸¹Kr piston flow ages <500 ka. Underground production is expected to be very likely <10%_{modern} and likely to be <4%_{modern} (Lehmann et al. (1993) [256]). However, upper limits for the subsurface production of ⁸¹Kr and its escape to groundwater still need to be established by field measurements. Underground production would lead to an underestimation of age if not considered in the model age calculation (the produced activity feigns a younger age). Diffusive exchange with stagnant aquitards (depleted in ⁸¹Kr compared with the studied aquifer) would cause an overestimation of model ages if not considered



FIG. 5.17. Steady state relative ⁸¹Kr model age differences between model ages considering diffusion and underground production and piston flow model (PFM) ages. The relation is plotted as a function of the effective diffusion coefficient of ⁸¹Kr in the aquitard (D_{eff}), for an underground production of between 0–10% modern and for two piston flow model age ranges. It is thereby assumed that the aquifer is 100 m thick and lies between two layers of indefinite aquitards (Sudicky and Frind (1981) [299]). The supposed porosities of the aquifer and the aquitards are 0.2 and 0.3, respectively. Flow velocity is 1 m/a.

in the decay law piston flow age calculation (the aquitards act as an additional sink for ⁸¹Kr). Relative deviations between groundwater and ⁸¹Kr tracer ages are shown in Fig. 5.17 and provide a realistic range of diffusion coefficients, subsurface secular equilibrium activities and measured ⁸¹Kr/Kr ratios (Lehmann and Purtschert (1997) [298]; Sanford (1997) [207]; Sudicky and Frind (1981) [299]). Underground production causes a positive shift in ⁸¹Kr/Kr ratios, whereas aquitard diffusion results in a negative shift. The assumed aquifer geometry and porosity are comparable to values typical for the investigated part of the Great Artesian Basin. The resulting maximal age difference is in the range ±20% and thus not much larger than the current analytical error. Additionally, for a groundwater sample with an age of 400 ka, the effect due to 5% underground production is compensated by diffusion with an effective diffusion coefficient of ~5 × 10⁻¹² m²/s. For the following discussion, ⁸¹Kr model ages based on radioactive decay only are used.

5.5.4. Comparison with helium data

Calculated ⁸¹Kr model ages now allow for an assessment of the concentration of radiogenic ⁴He, which increases with increasing groundwater age (Fig. 5.18). Two samples (DH, WC) showed a high accumulation rate of 9×10^{-10} cm³_{STP} · cm⁻³_{water} · a⁻¹, whereas RC and OD accumulated ⁴He at a much lower rate of 0.2×10^{-10} cm³_{STP} · cm⁻³_{water} · a⁻¹. However, the in situ ⁴He accumulation rate in the J-K sandstone is only 6.9×10^{-12} cm³_{STP} · cm⁻³_{water} · a⁻¹ (dotted line in Fig. 5.18) as calculated from the known U and Th concentrations and an average sandstone porosity of 20% (Lehmann et al. (2003) [256]). In accordance with observations at other locations in the Great Artesian Basin, the dominant source of helium is apparently external to the aquifer. By comparing the measured ³He and ⁴He concentrations



FIG. 5.18. Helium-4 accumulation as a function of 81 Kr model ages (left panel) and 3 He/4He signatures compared with calculated values in the sandstone and the Bulldog Shale (right panel). The dotted line indicates the increase of helium due to in situ U and Th decay within the aquifer.

in four groundwater samples to the calculated in situ ³He/⁴He production ratio (Fig. 5.18, right), it appears at least plausible that the source of the excess helium is located in the rocks and pore waters of the Bulldog Shale. This He exchange between the sandstone and the shale seems to be more effective at the end of the northern transect where DH and WC are located than for the locations of the other two wells, OD and RC.

5.5.5. Comparison with chlorine-36 data

The chloride and ³⁶Cl data along the two sampled transects are shown in Fig. 5.19. In the confined part (solid symbols) of the aquifer for the ⁸¹Kr study, both ³⁶Cl and ³⁶Cl/Cl decrease with decreasing hydraulic head (and distance), indicating increasing ages along the flow path. Chloride concentrations are relatively high and range from 600 to 3000 mg/L. The Cl decrease along the southern transect is likely the result of lower rates of evapotranspiration in the past (Love et al. (2000) [292]). This was also demonstrated by a good correlation between Cl concentrations and δ^{18} O values for the southern transect (not shown here). Concentrations of Cl along the northern transect are lower and show less variability, indicating that the input conditions were more humid and more constant in the recharge area of those samples. This observation is in line with other studies that also indicate spatially variable recharge and input conditions in this part of the Great Artesian Basin (Torgersen et al. (1991) [300]). In this study area, ³⁶Cl dating is apparently complicated by the unfortunate situation that both evaporative Cl enrichment during recharge (C_i) and varying subsurface Cl sources (C_a) occur simultaneously and with varying (and a priori unknown) strengths. The hypothesis of a spatially and temporally varying contribution of subsurface Cl is further strengthened by the weak correlation between δ^{18} O and the Cl concentration along the northern transect (Love et al. (2000) [292]). This implies once more that processes other than evaporation control Cl concentration. Neither dating by the ³⁶Cl/Cl ratio (insensitive to evaporation) nor by the ³⁶Cl concentration (rather insensitive to the addition of ³⁶Cl-'dead' chloride) offers an evident solution to this problem.

In light of the calculated ⁸¹Kr model ages, it is possible to demonstrate how such an ambiguity can be reduced by means of a multitracer comparison. As a starting point, the temporal evolution of the different ³⁶Cl components in a groundwater sample and their corresponding initial parameters (expressed as isotope ratios $R = {}^{36}$ Cl/Cl multiplied with the Cl concentrations *C*) are reconsidered (Bentley et al. (1986) [301]):



FIG. 5.19. Chloride and ³⁶Cl versus distance for south-western Great Basin groundwaters (from Love et al. (2000) [292]).

$$\underbrace{\underbrace{RC}}_{A} = \underbrace{\underbrace{R_i C_i \exp(-\lambda_{36}t)}_{B} + \underbrace{\underbrace{R_{se} C_i (1 - \exp(-\lambda_{36}t))}_{C} + \underbrace{(C - C_i) R_{ex}}_{D}}_{D}$$
(5.9)

where

A is measured ³⁶Cl concentration (atoms/L water);

- B is decay of the initial ³⁶Cl concentration in recharge water;
- *C* is the in-growth of a secular subsurface equilibrium ³⁶Cl concentration within the aquifer (R_{se});
- *D* is ³⁶Cl accumulation due to the addition of Cl from subsurface sources with a ³⁶Cl/Cl ratio of R_{ex} .

	RC	OD	DH	WC
⁸¹ Kr age t (ka)	230 ± 40	350 ± 50	290 ± 40	400 ± 50
C (mg/L)	1260	680	850	1040
$C_{\rm i}$ (mg/L)	1050	620	120	210
$C_{\rm a} = C - C_{\rm i} ({\rm mg/L})$	210	60	730	830
$\mathbf{K} = C_{\mathbf{a}}/t \;(\mathbf{mg} \cdot \mathbf{ka}^{-1} \cdot \mathbf{L}^{-1})$	0.95	0.15	2.54	2.07

TABLE 5.3. RECONSTRUCTED CONTRIBUTIONS OF METEORIC (C_1) AND SUBSURFACE (C_A) CI SOURCES IN THE SOUTH-WESTERN GREAT ARTESIAN BASIN



FIG. 5.20. Variations in ³⁶Cl/Cl and ³⁶Cl concentrations down two transects of the south-western Great Artesian Basin. Triangles indicate ⁸¹Kr dated locations (sampling date: \blacktriangle 1995 \triangle 1998). Lines represent the evolution for (a) decay, (b) a temporally linear Cl accumulation rate k of 0.5 mg \cdot ka⁻¹ \cdot L⁻¹ and (c) k = 1.6 mg/L ka starting with Cl concentrations of 200 mg/L and 800 mg/L, respectively. A ³⁶Cl/Cl ratio of 20 \times 10⁻¹⁵ for the accumulated Cl was assumed for cases b and c.

Apart from the groundwater age *t*, which is the target parameter for dating, it is necessary to estimate the meteoric ³⁶Cl/Cl initial ratio R_i , the recharge of Cl concentrations C_i , the secular equilibrium ratio R_{se} within the aquifer, and the ratio R_{ex} of any admixed or dissolved Cl. For this area of the Great Artesian Basin, a R_i of 125 × 10⁻¹⁵ was estimated based on relatively young samples in the recharge area which are ³H free and, therefore, not affected by thermonuclear ³⁶Cl (Love et al. (2000) [292]; Torgersen et al. (1991) [300]). It was further assumed that higher frequency variations of the ³⁶Cl fallout (Plummer et al. (1997) [248]) were smoothed out due to hydrodynamic dispersion (see Section 5.6).

A secular equilibrium ratio R_{Se} of 6.5×10^{-15} for J-K aquifer sandstone was calculated based on the measured elemental composition of several rock samples from the aquifer (Lehmann et al. (2003) [256]). Similarly, a ratio R_{ex} of 20×10^{-15} was obtained for the adjacent Bulldog Shale formation. The only residual free parameter is the chloride concentration that represents a recharge value (C_i), and that depends on the climatic conditions during recharge. It is known that several glacial cycles occurred over the timescales of the ³⁶Cl method dating range. The four well case study (C_i) can now be calculated because the second unknown t in Eq. (5.5) can be independently determined using ⁸¹Kr dating. In other words, the C_i value for each sample was determined by inserting the ⁸¹Kr age $t = t_{81}$ into Eq. (5.9) and solving for C_i . The subsurface input (C_a) corresponds to the difference between measured (C) and the initial Cl concentration (C_i). Finally, the Cl accumulation rate $k = C_a/t = t_{81}$ can be calculated (Table 5.3).

Reconstructed input concentrations C_i vary over almost one order of magnitude between 120 mg/L (DH) and 1050 mg/L (RC). The subsurface Cl accumulation rate k is small for two of the samples (<1 mg · ka⁻¹ · L⁻¹ for RC, OD) but more significant for DH and WC (2–3 mg · ka⁻¹ · L⁻¹). In Fig. 5.20, ³⁶Cl/Cl ratios are plotted as a function of the ³⁶Cl concentrations. Straight lines (a, a') indicate the theoretical evolution for decay and an underground secular equilibrium ratio of 20×10^{-15} but without any addition of subsurface Cl (terms *B* and *C* in Eq. (5.9)). The curved lines (b, b', c, c') represent cases for different Cl accumulation rates (term *D* in Eq. (5.9)). It is thereby assumed that Cl concentration increases linearly with time, starting with initial C_i concentrations of 200 mg/L (b, c) and 800 mg/L (b', c'), respectively. The large scatter of measured values on both transects is one more indication that evaporative enrichment and the accumulation of subsurface Cl accumulation rate in the subsurface. Samples low in ³⁶Cl (DH and WC) can either be the result of a high input concentration C_i (~800 mg/L) and a low accumulation rate (scenario a') or a low Cl input (200 mg/L) and a higher accumulation rate of ~1–2 mg · ka⁻¹ · L⁻¹ (scenario c).

The best estimate setting has either to be identified by a clear trend along a flowline (e.g. in Fig. 5.20) or by means of supplementary data such as ⁸¹Kr in this case. The results provided in Table 5.3 point to scenario c for DH and WC and scenarios a'-c' for RC and OD.



FIG. 5.21. ³⁶*Cl/Cl ratios versus Cl concentration of* ⁸¹*Kr dated samples (dashed red lines: pure mixing; blue solid lines: mixing + decay). Initial Cl concentrations as well as the quantification of* ³⁶*Cl/Cl reduction due to ageing are based on* ⁸¹*Kr data (Table 5.3).*

The impact of the different scenarios on 36 Cl dating results becomes more evident upon looking at the relation between the Cl concentration and the 36 Cl/Cl ratio (Fig. 5.21). The dashed lines represent pure mixing lines of the initial chloride with chloride in secular equilibrium with the Bulldog Shale (no radioactive decay). The solid lines include radioactive decay as quantified by 81 Kr measurements. The same initial 36 Cl/Cl ratio of 125×10^{-15} was assumed for all of the samples. For samples DH and WC, 93% and 89% of the 36 Cl/Cl ratio decrease is caused by the addition of subsurface chloride. Only the remaining 10% drop of the 36 Cl/Cl ratio is attributed to radioactive decay and, thus, to ageing. For OD and RC, on the other hand, the situation is quite different. The decrease in 36 Cl/Cl is dominated by the decay of atmospheric input. Chlorine-36 dating for these samples, therefore, seems to be straightforward. The identification and quantification of relative amounts of meteoric and subsurface Cl has to be based on additional tracers such as 81 Kr, as deduced in Section 6.6.3.

5.5.6. Additional evidence for the correctness of krypton-81 ages

Sparse experience with ⁸¹Kr dating can raise questions about the conclusions discussed above. Fundamentally, it poses the question of whether ⁸¹Kr ages are correct. Is it possible that processes other than admixture of Cl from the underlying shale are responsible for the disagreement of ⁸¹Kr and ³⁶Cl model ages for two of the samples? Again, the answer to these questions can only be obtained with additional evidence from other tracer measurements. The importance of multitracer approaches is once more emphasized (this is true for any groundwater investigation, not only for old groundwater).

The evaporative enrichment of initial Cl concentration C_i as a function of recharge temperature T is found using:

$$C_i(T) = \frac{C_p \cdot P}{R(T)}$$
(5.10)

where

- R(T) is the recharge rate (mm/a) as a function of the evaporation rate that is closely related to the recharge temperature $T(^{\circ}C)$;
- $C_{\rm p}$ is the Cl concentrations in precipitation (mg/L);
- *P* is the mean annual precipitation rate (mm/a).

From this simple chloride mass balance, a positive correlation is expected between recharge temperature T and the initial chloride concentration (warmer temperatures lead to a higher Cl enrichment in the recharge). Recharge temperatures can be reconstructed based on concentrations of dissolved noble gases (Aeschbach-Hertig et al. (1999) [302]; Mazor (1972) [303]). Noble gas recharge temperatures (NGRT) of the four wells are compared with reconstructed Cl input concentrations C_i in Fig. 5.22(a) (Lehmann et al. (2003) [256]). The reasonable correlation provides supporting evidence for the plausibility of estimated initial Cl concentrations (and derived ⁸¹Kr ages) because the parameters C_i and NGRT are analytically completely independent.

The second line of evidence comes from the comparison between accumulated radiogenic helium and accumulated Cl concentrations (C_a). Model calculations have shown that downward diffusion from the Bulldog Shale aquitard is most likely the process by which variable amounts of subsurface Cl are added (Love et al. (2000) [292]). Measured δ^{37} Cl values in rocks and groundwater support that the Bulldog Shale is the main source of Cl in the aquifer (see Zhang et al. (2007) [304] and Section 6.4.2). Moreover, the Bulldog Shale has already been identified to be the probable source for most of the accumulated He in the aquifer based on ³He/⁴He ratios (Fig. 5.18). It is an intriguing further piece of evidence that subsurface chloride accumulation (C_a) reconstructed on the basis of the ⁸¹Kr ages correlates well with the amount of accumulated ⁴He (Fig. 5.22(b)). It should be noted that the ⁴He concentration and noble gas temperatures are again completely independent parameters. A correlation



FIG. 5.22. (a) ⁸¹Kr derived initial chloride concentrations C_i versus calculated NGRT; (b) chloride of subsurface origin (C_a) versus concentration of radiogenic ⁴He_{rad}.

between ⁴He and Cl concentrations was also observed in other deep aquifer systems (Lehmann et al. (1996) [305]).

Despite the small number of samples, the conclusion has been drawn that the consistency of a whole set of different independent isotope tracers (⁸¹Kr, ^{36,37}Cl, ^{3,4}He, NGRT) points to:

- (a) The validity of ⁸¹Kr model ages in the range of 200–450 ka, which seem not to be significantly affected by secondary processes such as underground production, diffusion or variations in input concentration;
- (b) Distinct Cl accumulation histories with lower input concentrations and high Cl accumulation for two samples (DH, WC) and higher input concentrations and low subsurface accumulation for the other samples (RC, OD);
- (c) External sources of helium and chloride that are at least correlated.

5.5.7. Summary

The ten currently (2010) available ⁸¹Kr measurements in old groundwater³ certainly do not yet permit a comprehensive evaluation of the ⁸¹Kr method. Despite the sparse amount of data, some important conclusions can be drawn with regard to the analytical procedure of the ⁸¹Kr method and the applicability of ⁸¹Kr for dating old groundwater. An assessment of a novel technique is not meaningful without a comparison with more established methods. Owing to the comparable half-lives and dating ranges of ³⁶Cl and ⁸¹Kr, the focus is on the relationship between these two methods.

5.5.7.1. Krypton-81 methodology

In the past 15 years, significant progress has been made in the development of instruments for analysing ⁸¹Kr at natural concentration levels. The required amount of water has been reduced from about 17 t to about 1 t (2010) and is likely to be reduced further in the near future to approximately a few tens of litres (Lu and Mueller (2010) [287]). Sampling via gas extraction in the field has been proven to be practical and reliable. The gas processing and Kr separation procedure can be done using standard methods and will be further facilitated in the future with a probable decrease in sample volume.

³

Milk-River: 1 sample; GAB: 4 samples; Nubian aquifer (see Chapter 14): 6 samples.



FIG. 5.23. ³⁶Cl/Cl ratios as a function of ⁸¹Kr model ages (left plot) and Cl concentrations (right plot). Green triangles: samples from the Nubian aquifer; blue circles: samples from the Great Artesian Basin; solid circles: ³⁶Cl/Cl evolution dominated by decay; open circles: ³⁶Cl/Cl evolution dominated by the accumulation of Cl from subsurface sources. The lines indicate different calculated temporal ³⁶Cl/Cl evolutions (see text. D: Pure decay starting from ³⁶Cl/Cl = 120 × 10⁻¹⁵, R: Considering a subsurface secular equilibrium $R_{se} = 10 \times 10^{-15}A$: Considering a subsurface Cl accumulation at a rate of (2 mg \cdot ka⁻¹ \cdot L⁻¹)

5.5.7.2. Krypton-81 application

So far, nine out of ten ⁸¹Kr analyses from groundwater were significantly depleted compared with modern atmospheric krypton, with the lowest activity of 5% modern found in the Nubian aquifer (Sturchio et al. (2004) [5]). The proof-of-principle test of the 81 Kr method is, therefore, fulfilled. The initial results confirm — within remaining uncertainties — the expected advantageous characteristics of the ⁸¹Kr method, namely a constant input concentration and negligible underground production. This can be concluded from a comparison of ³⁶Cl/Cl data and ⁸¹Kr model ages from all currently available data pairs (Fig. 5.23, left). The lines in the plot indicate the calculated and expected relationship assuming different scenarios for the ³⁶Cl evolution. The first two scenarios represent pure decay (D) and decay with a subsurface ³⁶Cl/Cl equilibrium ratio of 10×10^{-15} (D + R). The scenario (D + R + A) assumes, in addition, a subsurface Cl accumulation with a 36 Cl/Cl ratio of 10×10^{-15} at a rate of 2 mg \cdot ka⁻¹ \cdot L⁻¹. All samples from the Nubian aquifer and two samples from the Great Artesian Basin agree with uncertainties within the range of the above mentioned ³⁶Cl accumulation scenarios. Without going into details of the local hydrology, this is already an encouraging coincidence, indicating the validity of the basic assumption for ⁸¹Kr model ages. It is also a demonstration of the applicability of the ³⁶Cl dating method despite some factors that could potentially affect the age interpretation of this isotope. However, for two of the Great Artesian Basin samples, ⁸¹Kr and ³⁶Cl ages disagree. The possible reasons are numerous and could originate from both tracers, but a look at Cl concentrations (right panel in Fig. 5.23) makes simplified ³⁶Cl interpretation more doubtful. In the Nubian aquifer, chlorinity is low and rather constant over time, representing ideal conditions for ³⁶Cl dating. In comparison, Cl concentrations in the Great Artesian Basin case study are much higher and more variable. This is just another element of the unfavourable ³⁶Cl dating conditions prevailing in this part of the Great Artesian Basin. However, if the fraction of subsurface Cl addition can be estimated using other means, it is nevertheless possible to calculate realistic tracer ages within the age of <1 Ma, even if a large fraction of Cl is of subsurface origin (Phillips (2000) [306]). The problem associated with DH and WC samples (open symbols) is that a high subsurface Cl accumulation rate goes together with a reduced meteoric



FIG. 5.24. Attenuation of a periodic climate signal as a function of groundwater age for different signal periods and Pe numbers (solid lines: Pe = 10; broken lines: Pe = 100).



FIG. 5.25. Temperature variations reconstructed from the Dome C ice core record (Luethi et al. (2008) [308]) compared with noble gas temperatures of four Great Artesian Basin wells.

input concentration. Future studies and more data are required for the verification of this hypothesis, which is based on the results of only four wells.

5.6. ADDENDUM: SIGNAL ATTENUATION DUE TO HYDRODYNAMIC DISPERSION

Fluctuations of initial recharge conditions and climate signal variations are propagated into the aquifer by advection and dispersion. These input signals are attenuated and phase shifted due to hydrodynamic dispersion. Attenuation factor A defined as the ratio of the remaining amplitude to

the initial amplitude of the signal as a function of the period (*T*) of the initial (climate) signal, the flow time *t* in the aquifer and the strength of the hydrodynamic dispersion which can be expressed by means of the dimensionless Peclet number Pe = vx/D (Roberts and Valochi (1981) [307]) is:

$$A = \exp(-\alpha) \text{ with } \alpha = \frac{Pe}{2} \left(\sqrt{0.5 + 0.5\sqrt{1 + \left(\frac{8 \cdot \pi \cdot t}{T \cdot Pe}\right)^2}} - 1 \right)$$
(5.11)

For example, an attenuation factor A of 0.7 corresponds to a reduction of the initial periodic (sinusoidal) signal by 30%. In Fig. 5.24, A is plotted as a function of groundwater age (assuming a flow velocity of 1 m/a) for different periods of the initial signal and for two different Peclet numbers, 10 and 100.

The remaining amplitude of a signal with a period of 10 ka after a flow time of 10 ka is 16% for a Pe number of 10 and 68% for a Pe number of 100 (Fig. 5.24). An aquifer system acts consequently as a low pass filter. Only long term low frequency input variations are recorded in old groundwater systems. An example are the noble gas temperatures (NGTs) of the four wells of the present Great Artesian Basin study compared in Fig. 5.25 with estimated temperature variations as recorded in δ^{18} O values from the Antarctic Dome C ice core (Luethi et al. (2008) [308]). The δ^{18} O/T relation was arbitrarily adjusted to local climate conditions. Despite the relatively large uncertainties in ⁸¹Kr ages and the NGTs, it can be concluded that small amplitudes of the observed variations are roughly in accord with the model calculations for a reasonable range of Peclet numbers between 10 and 100 (Gelhar et al. (1992) [297]). Larger temporal variations cannot be expected or are, if present, possibly the result of different recharge areas with distinct recharge conditions.

Chapter 6

CHLORINE-36 DATING OF OLD GROUNDWATER

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6.1. BASIC PRINCIPLES OF CHLORINE-36

Chlorine-36 has been widely used for dating old groundwater. The ³⁶Cl used for this purpose is produced in the atmosphere through the interaction of cosmic rays with argon atoms. The ³⁶Cl then mixes with ordinary atmospheric chloride (mostly derived from the ocean). The mixture is deposited on the land surface dissolved in rain or snow or as dry aerosols. Groundwater recharge carries the ³⁶Cl into the subsurface where the radiometric 'clock' is set. Chloride is conservative in the subsurface and, thus, the ³⁶Cl is rarely retarded with respect to the water velocity by adsorption or geochemical reactions. Groundwater age can be estimated using the radiometric decay equation and the decrease in ³⁶Cl from the amount in the recharge water. The main complication is variations in the Cl concentration of groundwater. This can potentially be due to variable evapotranspiration during recharge or to the addition of Cl in the aquifer. If the cause of Cl concentration variations is understood, the age calculation can be corrected to account for the process. Chlorine-36 dating is generally applicable to water in the age range 100 ka–1 Ma.

6.1.1. Chlorine-36 in the hydrological cycle

The principal application of ³⁶Cl to the dating of old groundwater is defining age through measuring the decay of atmospheric ³⁶Cl. Chlorine-36 is produced in the atmosphere by cosmic ray spallation of ⁴⁰Ar (Lal and Peters (1967) [309]). It decays to ³⁶Ar with a half-life of 301 000 \pm 4000 a (Bentley et al. (1986) [310]). The average global production rate lies between 20 and 30 atoms m²/s (Phillips (2000) [306]). This meteoric ³⁶Cl then mixes with stable oceanic Cl in the atmosphere, resulting in relatively low ratios of ³⁶Cl to stable Cl (³⁶Cl/Cl) near coastlines, but these ratios increase to high values near the centres of continents owing to the decrease in the atmospheric concentration of stable chloride (Davis et al. (2003) [311]; Keywood et al. (1997) [312]; Moysey et al. (2003) [313]).

The mixture of ³⁶Cl and stable chloride is deposited on the land surface dissolved in precipitation and as dry aerosols. Groundwater recharge transports the chlorine isotopes to the water table where they begin to be advected along with the flowing groundwater. As groundwater age increases, ³⁶Cl decays. In an ideal system (i.e. one with no subsurface sources of either ³⁶Cl or stable Cl and no sinks except radiodecay), calculating the ³⁶Cl model age is a simple matter of entering the initial and measured ³⁶Cl concentrations (or ³⁶Cl/Cl ratios) into the radioactive decay equation and solving for time.

In actual aquifers, although anomalous loss of either ³⁶Cl or stable Cl is seldom a problem, both species are often introduced in the subsurface. Concentrations of Cl and ³⁶Cl can also vary due to temporal or spatial changes in evapotranspiration in the aquifer recharge area. The challenge of ³⁶Cl dating of old groundwater is, thus, separating the changes in ³⁶Cl due to radioactive decay from these other processes (Phillips (2000) [306]). A representative schematic of ³⁶Cl in the hydrological cycle is shown in Fig. 6.1. The grey lines in the graphs on the bottom part of the figure show the simple exponential evolution of the ³⁶Cl/Cl ratio and ³⁶Cl concentration as a function of distance when no Cl



FIG. 6.1. Schematic of ³⁶Cl in the hydrological cycle. Numerical values are only representative. At the right hand side, marine Cl containing very little ³⁶Cl is lofted into the troposphere and over the continents. As it is advected inland, it mixes with ³⁶Cl produced by cosmic ray reaction with argon in the upper atmosphere. This mixture is deposited on the recharge area of an aquifer and the ³⁶Cl decays during groundwater flow.

is added in the subsurface. When Cl is added from bounding formations (which is common), the black lines show the evolution with distance. For the purposes of illustration, the assumed Cl concentration and 36 Cl/Cl ratio (which is shown by 36 Cl/Cl_{se} in the right hand graph) are unusually high. The 36 Cl/Cl ratio varies only moderately from the exponential case, but the 36 Cl concentration actually increases (due to the high equilibrium concentration in the bounding formation).

6.1.1.1. Historical summary

Application of ³⁶Cl to geochronology was first suggested by Davis and Schaeffer (1955) [314]. Although they did perform a few successful measurements on rocks and water containing fallout from nuclear weapons testing, the screen-wall beta counter technology of the time was incapable of quantifying ³⁶Cl in typical groundwater. This problem was partially solved with the development of liquid scintillation counting (Ronzani and Tamers (1966) [315]; Tamers et al. (1969) [316]). This method could measure ³⁶Cl at, and below, the levels typical of groundwater recharge, but suffered from the limitation that several grams of Cl were required. Inasmuch as groundwater recharge with high values of ³⁶Cl/Cl is typically fairly dilute, and subsurface water with high concentrations of Cl

typically shows fairly low ³⁶Cl/Cl, this analytical advance was limited to only a small number of practical applications.

The real breakthrough in the application of ³⁶Cl was the development of accelerator mass spectometry (AMS) as an analytical tool (Elmore et al. (1979) [317]). This technique was capable of measuring down to background levels of ³⁶Cl/Cl on milligram-sized samples and, thus, enabled analysis of nearly any groundwater sample (Davis et al. (1983) [318]). The first successful applications to old groundwater were in the Great Artesian Basin (Australia) and the Milk River aquifer (Canada) (Bentley et al. (1986) [310]; Phillips et al. (1986) [319]). These studies both illustrated the feasibility of ³⁶Cl as a method for dating old groundwater and pointed out the complications that result from variable evapotranspiration combined with subsurface sources of Cl and ³⁶Cl. Since the mid-1980s, the technique has been widely applied around the world (see Phillips (2000) [306], and Phillips and Castro (2003) [77] for a summary of studies).

6.2. SAMPLING TECHNIQUES FOR CHLORINE-36

Ease of sampling is one of the advantages of 36 Cl. Sampling is normally done by collecting sufficient water to contain at least ~10 mg of Cl in a clean container and precipitating the Cl as AgCl by adding excess AgNO₃ solution. Acidification is helpful in promoting the precipitation and flocculation of the AgCl.

The only case in which significant difficulty is likely to be encountered is if the water to be sampled contains very low Cl concentrations ($\sim 5 \text{ mg/L}$). In this case, a large water sample (5–10 L) must be collected. Flocculation for such dilute solutions is typically poor and isolation of the AgCl precipitate may be difficult or impossible. This problem can be addressed in two ways. The first is the use of an anion exchange resin column. Typically, the exchange resin is loaded with nitrate, which is displaced by Cl⁻ as the water sample flows through the column. However, anion exchange resins, as sold, typically have significant amounts of Cl⁻ adsorbed and great care must be taken to ensure that all of this Cl⁻ is flushed before the column is used for sampling. As the water being sampled is dilute, even small amounts of Cl⁻ contamination may be a serious problem. This method has been described in detail (Jannik (1989) [320]).

An alternative approach to dealing with low Cl concentrations is the addition of carrier. The carrier can either be ³⁶Cl-free ordinary Cl or one in which either ³⁵Cl or ³⁷Cl has been enriched. If an isotopically enriched carrier is used, the Cl concentration of the sample can be determined by means of isotope dilution mass spectrometry (IDMS) (Desilets et al. (2006) [321]) during AMS analysis. This offers a very significant advantage over separate measurement of the Cl concentration due to the difficulties involved in conventional measurement of Cl at low concentrations. Disadvantages of this approach are that if both the Cl concentration and the ³⁶Cl/Cl ratio are low, dilution of the ratio by addition of a carrier may significantly increase the uncertainty of the AMS measurement, and that carrier addition must be performed with great precision, which can be difficult under field conditions. For this reason, unless practical problems prevent shipment of the water sample to the laboratory, it is preferable to add the spike and precipitate the sample in the laboratory where the spike can be precisely weighed out. There is no single reliable source of isotopically enriched Cl and researchers are encouraged to contact the AMS laboratory that will provide their analyses for recommendations.

6.3. CHLORINE-36 SAMPLE PREPARATION AND MEASUREMENT

Chlorine-36 measurements in natural waters are almost entirely performed using AMS (Elmore et al. (1979) [317]; Elmore and Phillips (1987) [322]). This technique employs a tandem van de Graaff particle accelerator, originally designed for particle physics research, as a high energy mass spectrometer. One advantage of this instrument is that when the charge of the ion beam is reversed

in the high voltage terminal by passing through a thin foil (the 'tandem' aspect of the accelerator), all molecular species are broken up, eliminating molecular interference that would otherwise overwhelm the ³⁶Cl detector. A second advantage is that the very high energies imparted to the ion beam allow the use of a rate of energy loss detector that separates ³⁶Cl from its isobar ³⁶S, based on their differences in proton number. The history of AMS and recent advances have been surveyed (Elmore and Phillips (1987) [322]; Gove (1992) [323]; Muzikar et al. (2003) [324]; Suter (2004) [325]).

One recent advance that is now becoming frequently used for analysis of ³⁶Cl in environmental water samples is IDMS (Desilets et al. (2006) [321]). In this approach, an isotopically enriched spike of Cl (usually enriched in ³⁵Cl) is added to the sample before the Cl is precipitated as AgCl. Knowing the isotope ratio of the Cl spike and the masses of spike and sample, the Cl concentration of the sample (and, thus, also the ³⁶Cl concentration) can be calculated from the ³⁵Cl/³⁷Cl ratio that is measured during the AMS analysis. $R_{36,sample}$, the actual sample ³⁶Cl/Cl ratio (atoms ³⁶Cl · (atoms ³⁵Cl + ³⁷Cl)⁻¹), is calculated from the following formula, given $R_{36,meas}$, the ³⁶Cl/Cl ratio measured by the AMS; SS, the atomic ³⁵Cl/³⁷Cl ratio measured by the AMS; $R_{35,n}$, the atomic ³⁵Cl/⁽³⁵Cl + ³⁷Cl)) of natural Cl (0.7573); and $R_{35,sp}$, the ³⁵Cl/Cl ratio of the isotopically labelled spike:

$$R_{36,\text{sample}} = R_{36,\text{meas}} \left[1 + \frac{(1 - R_{35,\text{n}})SS - R_{35,\text{n}}}{R_{35,\text{sp}} - SS\left(1 - R_{35,\text{sp}}\right)} \right]$$
(6.1)

The Cl concentration of the sample ($C_{Cl,sample}$) in mg Cl/kg solution is correspondingly shown by:

$$C_{\text{Cl,sample}} = \frac{(1000)C_{\text{Cl,soln}}M_{\text{soln}}A_{n}\left(R_{35,\text{sp}} - SS\left(1 - R_{35,\text{sp}}\right)\right)}{M_{\text{water}}\left[\left(R_{35,\text{sp}}A_{35} + \left(1 - R_{35,\text{sp}}\right)A_{37}\right)\left(SS\left(1 - R_{35,\text{n}}\right) - R_{35,\text{n}}\right)\right]}$$
(6.2)

where

 $C_{\text{Cl,soln}}$ is the Cl concentration of the spike solution (mg Cl/g solution); M_{soln} is the mass of spike solution added to the sample (g); A_{n} is the atomic mass of natural Cl (35.4527 g/mol); M_{water} is the mass of the aqueous sample (g); A_{35} is the atomic mass of 35 Cl (34.9688 g/mol); A_{37} is the atomic mass of 37 Cl (36.9659 g/mol).

This methodology takes advantage of the high precision and accuracy of isotope ratio mass spectrometry to obtain a very reliable value for the Cl concentration of the sample. It is especially valuable for samples with low Cl concentration, where it not only provides a superior measurement of the Cl concentration, but also increases the Cl content of the water sample, thus facilitating precipitation and isolation of the AgCl and reducing the volume of water that must be collected.

As described above, Cl for ³⁶Cl analysis is collected through precipitation of AgCl. Fortunately, AgCl can be used as the target in the ion source of an AMS system. However, the sample must first be purified of S. Although the rate of energy loss detector is highly efficient at separating ³⁶Cl from ³⁶S, concentrations of S greater than a few milligrams per litre in the AgCl can still produce enough ³⁶S counts to seriously degrade the precision of the ³⁶Cl analysis, especially if the ³⁶Cl/Cl ratio is low. The sample preparation procedure, therefore, focuses on reducing the S concentration to make it as low as possible.

The standard ³⁶Cl preparation procedure was originally developed by H.W. Bentley (Bentley et al. (1986) [310]; Bentley et al. (1986) [301]; Phillips et al. (1986) [319]). The procedure consists of first dissolving the AgCl precipitate in NH_4OH , reprecipitating it through the addition of HNO₃, redissolving it and then adding BaNO₃ solution. The Ba²⁺ precipitates sulphur as BaSO₄. The solution is then separated from the BaSO₄ precipitate and the AgCl reprecipitated through the addition of HNO₃. The repeated dissolution/reprecipitation steps also lower the S content of the AgCl by partitioning the S

Average coefficient of variation (%)				Analytical bias relative to average (%)			
	Analytical	Sample	Sample	Sample	Lab A	Lab B	Lab C
	Both treatments	Both treatments	Uniform preparation	Laboratory preparation			
All data	46	37	30	38	0	6	21
$^{36}Cl/Cl > 10 \times 10^{-15}$	10	14	12	16	3	-1	-3

TABLE 6.1. STATISTICAL EVALUATION OF INTERLABORATORY COMPARISON DATA (from Mahara et al. (2004) [327])

into the solution with each precipitation. Depending on the sulphur concentration of the water sampled, this procedure may be repeated two or three times.

The main disadvantages of this procedure are that it may require one to several days, depending on the number of $BaNO_3$ steps, and that a small amount of Cl is lost with each cycle. An alternative procedure has recently been developed (Jiang et al. (2004) [326]). This procedure employs ion exchange columns to concentrate the Cl and reduce S contamination. The authors claim that Cl recovery is >90% and that the procedure takes less than one day, however, it has not yet been widely tested.

After drying, the AgCl can be packed into a holder and placed in the ion source of an accelerator mass spectrometer. The machine measures the ³⁶Cl/Cl ratio and the ³⁵Cl/³⁷Cl ratio (assuming an isotopically enriched spike has been added) of the AgCl. This analysis typically uses between 15 min and 1 h of beam time. The analyses are standardized by normalization to recognized international standards (unlike ¹⁴C, these standards are arbitrary and do not reflect any natural material). From these ratios and associated information on sample volume and the mass of the sample spike ³⁶Cl/Cl ratio, the Cl concentration and ³⁶Cl concentration can be calculated. If IDMS has not been employed, the Cl concentration must be analysed using an independent method. Ion chromatography is generally the preferred method.

Assuming the sample has been spiked with 35 Cl or 37 Cl, the AMS laboratory will report back either the 36 Cl/(35 Cl + 37 Cl) ratio or the 36 Cl/(35 Cl + 37 Cl) ratio or the 36 Cl/(35 Cl ratio. The user must combine this with data on the sample mass, the spike isotope ratio, and the mass of spike added in Eqs (6.1, 6.2), to obtain the sample 36 Cl/Cl and Cl concentration.

Until recently, any systematic comparisons of ³⁶Cl analyses' reliability have been very limited in scope. However, Mahara et al. (2004) [327] have recently published a very thorough interlaboratory comparison. They sent 15 natural water samples to three AMS laboratories around the world (the laboratories were not identified by name). Each of the 15 samples was subjected to two treatments: the first aliquot was processed in Mahara's laboratory using a uniform processing procedure, while the second aliquot was sent to the AMS laboratory as an untreated water sample and processed there by whatever procedure was standard in that laboratory. This constituted a total sample of 90 AMS analyses, which is a sufficient basis for statistical evaluation. The chloride concentrations of the samples ranged from 9 to 17 900 mg/L and the mean ³⁶Cl/Cl ratios ranged from 0.5 to 410×10^{-15} , a typical range for deep groundwater samples.

The outcome of this comparison is summarized in Table 6.1 and shown graphically in Fig. 6.2. The results are divided into 'all samples' (a total of either 90 or 45 analyses, depending on whether both treatments or only one are being considered) and ' 36 Cl/Cl > 10 × 10⁻¹⁵', which constituted 9 of the 15 samples. The 'analytical standard deviation' is the mean of the 1 σ standard deviations for each analysis, converted to a coefficient of variation using the mean of the six replicate analyses. The next three columns provide the coefficients of variation for both treatments combined and each


FIG. 6.2. Reproducibility of AMS ³⁶Cl/Cl measurements on water samples as a function of the ³⁶Cl/Cl ratio of the sample, based on data from Mahara et al. (2004) [327]. 'Uniform preparation' refers to samples prepared in Mahara's laboratory, 'Lab preparation' to samples prepared at several AMS laboratories, and 'All data' to the two data sets combined.

separately. Finally, the last three columns summarize the analytical bias (relative to the mean of all six replicates) for the three AMS laboratories. Figure 6.2 shows that for samples with ³⁶Cl/Cl less than $\sim 20 \times 10^{-15}$, the coefficients of variation are reasonably small, but that they in some cases rise to values over 100% as the ³⁶Cl/Cl ratio approaches zero. The reported analytical standard deviations appear to predict the actual measured standard deviations reasonably well. For samples with ³⁶Cl/Cl greater than 10×10^{-15} , having the sample preparation performed in three separate laboratories, as opposed to a single laboratory, increased the coefficient of variation from 12% to 16%. This difference of 4% would appear to be a reasonable estimate of the magnitude of variability that might be expected as a result of differing laboratory preparation procedures. The bias evaluation indicates that samples can be expected to be reproducible between laboratories to \sim 3%, which is quite adequate for the purposes of groundwater dating.

6.4. CHLORINE-36 RESEARCH GROUPS AND LABORATORIES

Owing to the size and expense of accelerator mass spectrometers, the number of laboratories around the world that are capable of ³⁶Cl analysis on typical deep groundwater samples is limited. However, because such major laboratories are almost always operated as shared facilities, they are accessible to outside investigators, and as a result there are many research groups employing ³⁶Cl in groundwater studies.

The institution that performed the original ³⁶Cl AMS analyses was the tandem accelerator laboratory at the University of Rochester (New York, USA), but this facility has since been closed down. Analyses were taken over by the Center for Accelerator Mass Spectrometry at Lawrence Livermore National Laboratory (Livermore, CA, USA) (Roberts et al. (1996) [328]), the Purdue Rare Isotope

Measurement Laboratory (West Lafayette, IN, USA; 'PRIME Lab') (Elmore et al. (1996) [329]), the AMS laboratory at the Paul Scherrer Institute (Zurich, Switzerland) (Synal et al. (1994) [330]), the Research Group and Laboratory of the Technical University of Munich (Garching, Germany), and the laboratory at Australia National University (Canberra, Australia) (Fifield (2000) [331]). For many years, these facilities have performed the bulk of ³⁶Cl analyses around the world, but they have recently been joined by several laboratories that have more recently developed the ³⁶Cl capability. These include the Scottish Universities Environmental Research Centre (East Kilbride, United Kingdom) (Freeman et al. (2004) [332]), the China Institute of Atomic Energy (Jiang et al. (2004) [326]), the University of Tokyo (Tokyo, Japan) (Aze et al. (2007) [333]), the University of Tsukuba (Tsukuba, Ibaraki, Japan) (Sasa et al. (2007) [334]), the University of Uppsala (Uppsala, Sweden) (Alfimov et al. (2007) [335], and Oak Ridge National Laboratory (Oak Ridge, TN, USA) (Galindo-Uribarri et al. (2007) [336]).

6.5. SPECIFICS OF THE ³⁶Cl METHOD

Unlike many groundwater tracers and dating agents that may undergo complex chemical reactions in the subsurface (such as ¹⁴C or uranium isotopes), ³⁶Cl is virtually inert. This greatly simplifies the interpretation of its behaviour. In spite of this relative simplicity, the interpretation is often not straightforward. The major complications in using ³⁶Cl to estimate groundwater age are the introduction of subsurface chloride, subsurface production of ³⁶Cl, and variation in the input of ³⁶Cl due to changes in evapotranspirative concentration or changes in cosmogenic production. High chloride concentrations arising from connate waters, evaporite dissolution, or possibly rock-water interaction are common in sedimentary basins and deep crystalline rocks. These may either diffuse upward or be advected into aquifers by cross-formational flow. In general, this subsurface-source chloride is not ³⁶Cl free, because ³⁶Cl is produced at low levels (compared with meteoric chloride) in the subsurface by absorption by ³⁵Cl of thermal neutrons produced by U and Th series decay and U fission (Fabryka-Martin et al. (1988) [337]; Lehmann et al. (1993) [250]; Phillips (2000) [306]). In addition to subsurface addition of Cl isotopes, the production of ³⁶Cl in the atmosphere and, thus, the input at the recharge area may also change with time as a result of fluctuations in the intensity of the terrestrial and solar magnetic fields (Plummer et al. (1997) [248]; Wagner et al. (2001) [338]). Finally, changes in climate can affect both the distance from the ocean shore (Bentley et al. (1986) [310]; Purdy et al. (1996) [339]) and, thus, the accession of stable marine chloride to the recharge area, and the amount of evapotranspiration of the recharge water (Love et al. (2000) [292]; Zhu et al. (2003) [340]), which concentrates Cl and ³⁶Cl equally.

As a general working principle, ³⁶Cl dating of old groundwater is most straightforward and least ambiguous in situations where the meteoric ³⁶Cl/Cl ratio at the aquifer recharge area is high relative to the steady state subsurface ratios and where subsurface input of chloride is minimal. Subsurface equilibrium ratios typically vary from about 5×10^{-15} to 50×10^{-15} . The ratios at the higher end of this range are most commonly found in acidic plutonic or volcanic formations and the large sedimentary aquifers in which ³⁶Cl is commonly employed usually have subsurface equilibrium ratios of less than 20×10^{-15} . Meteoric ³⁶Cl/Cl in aquifer recharge may be below this ratio close to the ocean, but rises to values of $100-1000 \times 10^{-15}$ in continental interior settings. Thus, the 'cleanest' applications of the method are likely to be found in large sedimentary basin aquifers with recharge in the continental interior and permeabilities high enough to flush most connate solutes. Recent studies in the Australian interior at Palm Valley (Wischusen et al. (2004) [341]), the Amadeus Basin (Cresswell et al. (1999) [342]; Kulongoski et al. (2008) [343]), the Coonamble embayment in the Great Artesian Basin (Mahara et al. (2007) [344]), and, in North Africa, the Nubian aquifer (Patterson et al. (2005) [43]; Sturchio et al. (2004) [5]) provide good examples of this favourable situation.

6.5.1. Meteoric sources of ³⁶Cl

In most cases, as described above, the fundamental basis for ³⁶Cl dating of groundwater is the radiodecay, during subsurface residence, of relatively high concentrations of ³⁶Cl introduced to aquifers, along with recharging groundwater. Successful dating, thus, requires knowledge of ³⁶Cl in atmospheric deposition.

The ultimate source of ³⁶Cl in the atmosphere is the interaction of high energy cosmic rays (principally protons and neutrons) with the nucleus of ⁴⁰Ar atoms (see Phillips (2000) [306] for more information on the nuclear reactions). This production is highest near the geomagnetic poles and lowest near the geomagnetic equator because the magnetic field of the earth deflects primary cosmic ray protons where the field lines are quasi-horizontal near the equator, but allows the cosmic ray particles to reach the atmosphere following the near-vertical field lines at the poles (Desilets and Zreda (2003) [345]; Lal and Peters (1967) [309]; Powell (1955) [346]; Simpson and Uretz (1953) [347]). Chlorine-36 deposition on the land surface, however, does not peak at the geomagnetic poles. Most of the ³⁶Cl production takes place in the stratosphere because the cosmic ray flux is higher there than in the troposphere, and it is the position of ³⁶Cl in the troposphere. This mixing is greatest at ~40° latitude, during the spring season. This produces the characteristic maximum in deposition at this latitude, decreasing towards both the pole and equator as deposition removes ³⁶Cl from the atmosphere during turbulent transport northward and southward (Fig. 6.3) (Bentley et al. (1986) [310]; Phillips (2000) [306]).

Were the tropospheric ³⁶Cl concentration is directly proportional to ³⁶Cl deposition on the land surface, ³⁶Cl in groundwater recharge would be straightforward to predict. In reality, the processes involved in ³⁶Cl deposition are considerably more complex. Chlorine-36, along with stable Cl, adheres to atmospheric aerosols. Depending on their size, these aerosols are deposited at differing rates (Buseck and Schwartz (2003) [348]). They may serve as nuclei for the condensation of water droplets or be engulfed by droplets after they have formed. Depending on the degree of water saturation of the atmosphere, the droplets may grow rapidly and precipitate to the land surface or may simply persist in the atmosphere. As a result of these interactions, ³⁶Cl may have both varying residence times and varying deposition rates in different parts of the troposphere.



FIG. 6.3. Estimated latitudinal distribution of ³⁶Cl deposition. Empirical data are compared to calculations by Parrat et al. (1996) [349], and Lal and Peters (1967) [309]. (Figure modified from Phillips (2000) [306].)

The most detailed time series of ³⁶Cl in precipitation was produced by Knies (1994) [350], who measured over 350 samples from West Lafayette, Indiana, USA, between June 1992 and June 1993. Concentrations in individual samples (multiple samples were collected during storms) varied from 10⁵ to 10⁷ atoms/L and the range of concentrations in an individual event sometimes spanned an order of magnitude. Averaged over a large number of storm events, ³⁶Cl concentrations and deposition rates do form spatially coherent patterns, but a very high degree of short term variability shows that the controls on deposition are very sensitive to environmental conditions.

The average monthly ³⁶Cl deposition rate of the samples from Knies' data set exhibited a strong correlation to average monthly precipitation (0.052 ± 0.006 atoms ³⁶Cl \cdot m⁻² \cdot s⁻¹ \cdot (mm/a)⁻¹ converted to annual units; $r^2 = 0.85$) (Phillips (2000) [306]). This suggests that some of the variability in ³⁶Cl deposition can be explained by variations in precipitation. Phillips (2000) [306] used this correlation to normalize ³⁶Cl deposition measurements spanning the globe, obtaining a global average value of ~30 atoms \cdot m⁻² \cdot s⁻¹. He also used it, in concert with an estimate of the latitudinal distribution of ³⁶Cl deposition and the geographic distribution of precipitation and stable chloride deposition, to calculate the distribution of the ³⁶Cl/Cl ratio over the USA. However, other data sets bearing on this relation have not showed as strong a correlation (Hainsworth et al. (1994) [351]; Moysey et al. (2003) [313]). A large set of data on ³⁶Cl in groundwater collected yielded a slope for the ³⁶Cl deposition relation that was about half that of the Knies data (Davis et al. (2003) [311]; Moysey et al. (2003) [313]).

This observation may help to reconcile previous estimates of 36 Cl deposition and the distribution of the 36 Cl/Cl ratio. If the slope from the Moysey/Davis data (~0.025 atoms 36 Cl · m⁻² · s⁻¹ · (mm/a)⁻¹) is used in the Phillips (2000) [306] equation for calculating global average 36 Cl deposition, a value of ~25 atoms · m⁻² · s⁻¹ is obtained, which is closer to that calculated by Moysey et al. (2003) [313] and several other authors. The empirical map of 36 Cl/Cl ratios over the USA produced by Davis et al. (2003) [311] and Moysey et al. (2003) [313] (Fig. 6.4) showed a pattern similar to that predicted by Phillips (2000) [306], but in general lower values. If both the lower slope from Moysey et al. (2003) [313] and the lower global deposition value calculated above are substituted in the algorithm from Phillips (2000) [306] for the distribution of the 36 Cl/Cl ratio, the match is markedly improved. However, 36 Cl/Cl ratios in the south-eastern USA are still lower than calculated. The most likely explanation for this



FIG. 6.4. The distribution of meteoric ³⁶Cl/Cl ratios over the USA estimated by Davis et al. (2003) [311], based on empirical data.

systematic deviation is that much of the Cl deposited over the south-eastern region originates from the lower latitudes of the north Atlantic Ocean, where ³⁶Cl atmospheric concentration is less than in the area where the ³⁶Cl is eventually deposited on the land surface.

The strongest correlation that Moysey et al. (2003) [311] found for the ³⁶Cl/Cl ratio was an inverse one with stable Cl deposition. This is encouraging, suggesting that the deposition of ³⁶Cl is fairly uniform, with dependence on amount of precipitation as a second order effect, and that the geographical variation of the ³⁶Cl/Cl ratio can be explained mostly by the amount of dilution from stable Cl deposition. For the remainder of the globe that has been studied for ³⁶Cl deposition less intensively than the USA, this indicates that with current knowledge of the latitudinal variation of ³⁶Cl deposition, precipitation and stable Cl deposition (which is much easier to measure than ³⁶Cl deposition), ratios of ³⁶Cl/Cl in groundwater recharge might be satisfactorily estimated.

6.5.2. Secular variation in the atmospheric deposition of ³⁶Cl

As described above, the penetration of the primary cosmic radiation into the atmosphere of the earth is modulated by the strength of the terrestrial magnetic field (Elsasser et al. (1956) [352]). Large fluctuations in both the intensity of the dipole magnetic field and in the position, configuration and intensity of the non-dipole field have been well documented (Korte and Constable (2006) [353]; Valet et al. (2005) [354]). Cosmogenic production of ³⁶Cl has, therefore, varied with time. This inference has been verified by measurement of ³⁶Cl in the meteoric proxy archives of ice cores (Baumgartner et al. (1998) [355]; Wagner et al. (2001) [338]) and fossil rat urine (Plummer (1996) [356]) (Fig. 6.5). The magnitude of variation in both of these records was about a factor of two. The extent to which these fluctuations in atmospheric production are reflected in the initial ³⁶Cl content of old groundwater samples has not been determined. Over the long timescales usually considered (>100 ka), dispersion and mixing may average out the input variations. In one of the few continental archives over this timescale, a very deep vadose zone profile from the Mojave Desert, these variations in production were not readily apparent, although the deep chloride did have higher ³⁶Cl/Cl ratios than expected based on modern samples (Tyler et al. (1996) [357]).

In addition to the atmospheric production variation, the ³⁶Cl/Cl ratio of atmospheric deposition can vary as a result of changes in the stable Cl deposition. Such changes could be produced by variation in the distance between the aquifer recharge area and the ocean, driven by sea level changes. Trends in the ³⁶Cl/Cl ratio down flowlines in the Carrizo aquifer (Texas, USA) (Bentley et al. (1986) [310]) and the Aquia aquifer (Maryland, USA) (Purdy et al. (1996) [339]) have been attributed to this mechanism.

6.5.3. Chlorine-36 from nuclear weapons fallout

The USA tested numerous thermonuclear weapons in the Pacific Ocean during the 1950s and 1960s. Thirty-five of these, between 1954 and 1958, were conducted with devices placed on barges in the ocean (Zerle et al. (1997) [358]). The resultant thermal neutron activation of ³⁵Cl in sea water and dispersion in the stratosphere produced a global pulse of ³⁶Cl fallout between 1954 and 1965. This peaked at deposition rates approximately two orders of magnitude greater than natural atmospheric ³⁶Cl production. Phillips (2000) [306] has presented a global reconstruction of the latitudinal distribution of the fallout pulse.

Owing to the magnitude and duration of this pulse, it presents a potential complication to the ³⁶Cl dating of old groundwater. Contamination of old groundwater samples by relatively small proportions of bomb era recharge could markedly increase the apparent ³⁶Cl concentration of old groundwater. For this reason, it is common to analyse samples for ³⁶Cl, for ³H or for ³H/³He in order to provide assurance that such contamination is negligible.



FIG. 6.5. (a) Chlorine-36 deposition variations in a Greenland ice core (Wagner et al. (2001) [338]) (a) variation in the virtual axial dipole moment of the earth over the past 75 ka, (b) ³⁶Cl concentration in the ice. It should be noted that ³⁶Cl concentration varies as a function of ice deposition rate as well as production. (b) ³⁶Cl/Cl in fossilized rat urine from the south-western USA over the past 40 ka (from Plummer et al. (1997) [248]).

The bomb ³⁶Cl pulse can also complicate the estimation of the initial ³⁶Cl ratio or concentration by contamination of young samples collected to assess the initial condition. Samples of post-bomb recharge (as established by CFC or ³H/³He dating) could potentially be used for this purpose, but this is complicated by retention of bomb ³⁶Cl in vegetation and subsequent soil/plant recycling (see Section 6.5.4.2).

Scheffel et al. (1999) [359] have reported ³⁶Cl deposition rates several times the expected natural ones for post-bomb precipitation samples. They attributed this to recycling of bomb ³⁶Cl. If this attribution is correct, then precipitation samples should also not be used to establish the initial ³⁶Cl for groundwater dating. However, the Cl concentration data in precipitation reported by Scheffel et

al. (1999) [359] also appear to be unreasonably high (cf. values reported in Berner and Berner (1987) [360]). This process, rather than bomb ³⁶Cl recycling, may explain anomalous ³⁶Cl deposition rates.

6.5.4. Processes affecting ³⁶Cl during recharge

During deposition on the land surface and infiltration through the vadose zone, ³⁶Cl concentrations and ratios can potentially be affected by several processes. The most prominent of these are evaporation, transpiration, biological uptake, differential transport through fast and slow flow paths, and weathering release of ³⁶Cl from minerals.

6.5.4.1. Effects of evapotranspiration

Virtually all recharge water is concentrated to some extent by evapotranspiration (Lerner et al. (1990) [361]). In arid regions, Cl⁻ in recharge water can be enriched over precipitation by up to 500-fold (Scanlon et al. (2006) [362]; Tyler et al. (1996) [357]). Climate variations at the glacial/interglacial timescale can produce large changes in the evapotranspirative concentration of recharge (Walvoord et al. (2002) [44]). Trends in Cl concentration down flow paths that were produced by this mechanism have been noted in the Great Artesian Basin (Airey et al. (1983) [363]) and other aquifers. This phenomenon can produce significant problems in attempts to date such groundwater using changes in ³⁶Cl concentration. Use of the ³⁶Cl/Cl ratio is generally preferable in this case, since ³⁶Cl and Cl are concentrated equally by evapotranspiration.

6.5.4.2. Effects of plant uptake of Cl and ³⁶Cl

Chlorine is an essential nutrient for plants and is, thus, taken up by their roots and utilized in plant tissues and fluids (Sheppard et al. (1999) [364]). Scarce nutrients such as NO_3^- and P exhibit concentration profiles through the root zone that decrease with depth; this is an indication that they are being semi-quantitatively retained in the soil via biological recycling. In contrast, Cl⁻ typically shows concentration profiles that increase with depth, reflecting predominant control by evapotranspirative concentration (Jobbagy and Jackson (2001) [365]). In general, the effect of plant uptake is most prominent when Cl⁻ concentrations in soil water are low.

The Cl⁻ taken up by plant roots is incorporated into organic compounds within the plant. The concentration of Cl in plant tissue (dry mass basis) is typically ten times that of the Cl⁻ in the soil water from which the plants grew, and in some plants may be 150 times the soil water concentration (Kashparov et al. (2007) [366]; Sheppard et al. (1999) [364]). Most of this Cl is released back to the soil by decomposition, either after leaves are shed or after the plant dies, but some fraction may be incorporated in volatile organic molecules such as chloroform, tetrachloromethane and 1,1,1-trichloroethane (Laturnus and Matucha (2008) [367]). Chlorine-36 in these compounds may then be volatilized to the atmosphere, although the fraction lost this way is probably generally small.

Some of the Cl incorporated in plant tissues is directly released to the soil water as Cl⁻ during decomposition, but a significant fraction can be retained in relatively refractory humic and fulvic acids in the soil (Myneni (2002) [368]). These, and similar, compounds in soil can then adsorb additional Cl⁻ from the soil water (Lee et al. (2001) [369]). A small fraction of the Cl⁻ deposited on the soil surface may be immobilized over geological time in these refractory compounds, but a strong trend towards increasing concentration with depth (Jobbagy and Jackson (2001) [365]) shows that most Cl⁻ eventually passes through the soil column. The effect of vegetation uptake and chemical transformation is, thus, to retard and homogenize Cl⁻ deposited from the atmosphere.

This retardation (relative to the flux of associated water) is clearly evidenced by the slowness in passing through the hydrological system of the pulse of ³⁶Cl released by nuclear weapons testing in

the late 1950s (Elmore et al. (1982) [370]; Zerle et al. (1997) [358]). Numerous studies have noted that in situations where consideration of hydrological fluxes indicate that surface water or soil water should have been flushed of the bomb pulse, fallout ³⁶Cl is still found at high levels in the system (Alvarado et al. (2005) [371]; Hogan et al. (2007) [372]; Milton et al. (1997) [373]; Van Valkenburgh (1996) [374]). Measurements of ³⁶Cl in various species of conifers in Canada have verified that twenty or more years after the bomb fallout peak, the vegetation retained ³⁶Cl/Cl ratios similar to that of the peak (Milton et al. (1997) [375]). Cornett et al. (1997) [376] estimated a mean residence time of ~40 a for Cl in vegetation and soil under relatively humid, heavily vegetated conditions in Ontario, Canada. Given the subsequent discovery of Cl sequestration in relatively refractory organo-chlorine compounds (Myneni (2002) [368]), the residence time distribution is undoubtedly skewed, with a tail of quite long residences.

The net effect of biological uptake of ³⁶Cl is to provide a low pass filter at the front end of the groundwater system. Residence times in the organic reservoir (plants plus soil) are almost certainly quite short compared with the residence time in aquifers being considered for ³⁶Cl dating, but the retention helps to smooth short term fluctuations in ³⁶Cl and Cl deposition.

6.5.4.3. Effects of transport through the vadose zone

Transport through the vadose zone is a necessary step prior to atmospherically deposited ³⁶Cl becoming a groundwater solute. In most cases, this constitutes a geologically instantaneous transfer and has little influence on ³⁶Cl dating of old groundwater. However, Cl⁻ residence times in the vadose zone can vary widely depending on climate and vadose zone thickness, varying from a few days to >10⁵ a. In arid regions with thick vadose zones, the residence time of Cl⁻ may be significant in comparison to subsurface residence times of interest. For example, Tyler et al. (1996) [357] has shown that ³⁶Cl is retained in deep (>200 m) vadose zones of the Mojave Desert for over 120 000 a. Modelling of this system by Walvoord et al. (2002) [44] indicates that plausible climate change events are capable of flushing this accumulated Cl⁻ into underlying aquifers in a matter of a few thousand years.

Large contrasts in the hydraulic properties of vadose zones can produce similar effects without the necessity for a very arid climate. For example, Foster and Smith-Carrington (1980) [377] have shown that diffusion into low permeability matrix blocks has retarded the arrival of agricultural nitrate by decades during transport through a fractured chalk vadose zone in England. Conversely, at least small amounts of bomb ³⁶Cl are apparently bypassing large amounts of Cl⁻ that entered the vadose zone at Yucca Mountain, Nevada, during the Pleistocene and are now entering a tunnel at hundreds of metres depth (Campbell et al. (2003) [378]; Cizdziel et al. (2008) [379]). Dual media vadose zones (usually high permeability fractures in a low permeability but high porosity matrix) can have the apparently paradoxical property of retaining large reservoirs of solutes while permitting the rapid transmission of water. If aquifer recharge areas intended for ³⁶Cl dating have dual media characteristics, the effect on the recharge value for the ³⁶Cl should be carefully evaluated.

6.5.4.4. Effects of weathering release of cosmogenic in situ ³⁶Cl

In addition to the effects of the vegetation–soil–vadose zone on 36 Cl transport, this zone can also be a source of the nuclide. Nuclear reactions provoked by the actions of cosmic radiation on the nuclei of atoms making up soil and rock can produce 36 Cl within the mineral phases (Gosse and Phillips (2001) [380]). The production rate of 36 Cl increases quasi-exponentially with altitude. Phillips (2000) [306] has described the production reactions in some detail and evaluated their importance for groundwater dating. Given normal weathering rates, these in situ reactions are of negligible importance for most rock types at sea level. However, at elevations >3 km, this source can increase the flux of 36 Cl to the water table by more than 50%, especially at tropical latitudes where atmospheric deposition rates are low. Limestone is of particular importance in this regard because it has both a high concentration of the target element calcium and it weathers unusually rapidly. Even at sea level at mid-latitudes, weathering of ³⁶Cl from limestone can contribute ~10% of the atmospheric flux, whereas at high elevations near the equator it can release ³⁶Cl amounting to >200% of the atmospheric flux. The release of this 'epigene' ³⁶Cl (Bentley et al. (1986) [310]) should always be considered in evaluating the accession rate of ³⁶Cl to the aquifer if the recharge area is above a ~2 km elevation.

6.5.5. Subsurface processes influencing ³⁶Cl concentrations and ³⁶Cl/Cl

6.5.5.1. Hypogene production of ³⁶Cl

Chlorine-36 is unusual (although not unique) among nuclides used for groundwater tracing in that it can be produced by a thermal neutron absorption reaction, in this case ${}^{35}Cl(n, \gamma){}^{36}Cl$ (Davis and Schaeffer (1955) [314]). This means that any water that contains Cl⁻, which is virtually ubiquitous, and undergoes a neutron flux will produce ${}^{36}Cl$. Neutrons are released in the subsurface below the reach of cosmic radiation by nuclear reactions, principally neutrons directly emitted from the nuclei of uranium atoms undergoing spontaneous fission and as a secondary result of α particles released during the decay of uranium series nuclides and absorbed by light nuclei that then eject a neutron (Feige et al. (1968) [381]). These neutrons are rapidly slowed to thermal energies and may then be absorbed by ${}^{35}Cl$. The reaction ${}^{39}K(\alpha, n){}^{36}Cl$ can also produce ${}^{36}Cl$ in the subsurface, but it is generally insignificant in comparison to the neutron absorption reaction on Cl (Lehmann et al. (1993) [250]).

The production of neutrons as a result of spontaneous fission emission is simply a function of the concentration of U in the rock:

$$P_{\rm nsf} = 0.429 C_{\rm U} \tag{6.3}$$

where

 $P_{n,sf}$ is the production rate in neutrons \cdot (g rock)⁻¹ \cdot a⁻¹; C_U is the concentration of U in parts per million (Fabryka-Martin (1988) [382]).

The production by alpha-n reactions is shown by:

$$P_{n,\alpha} = \frac{\sum_{i} S_{i}C_{i}Y_{n}^{U} + \sum_{i} S_{i}C_{i}Y_{n}^{Th}}{\sum_{i} S_{i}C_{i}}$$
(6.4)

where

 $P_{n,\alpha}$ is the production rate in neutrons $\cdot (g \operatorname{rock})^{-1} \cdot a^{-1}$; S_i is the mass stopping power of element *i* for α particles of a given energy in MeV $\cdot \operatorname{cm}^2 \cdot g^{-1}$; C_i is the concentration of element *i* in parts per million; Y_n^{U} and Y_n^{Th} are the neutron yields of element *i* per parts per million of U or Th in secular equilibrium with their daughters (Fabryka-Martin (1988) [382]; Feige et al. (1968) [381]).

Values for these constants are given in Table 6.2.

When neutrons are emitted by the reactions described above, they are at energies well above the thermal level dictated by the ambient temperature (<0.5 eV). They are slowed and lose energy principally by collision with light atomic nuclei. During this energy moderation process, some of the neutrons may be absorbed by nuclei they encounter. The equilibrium neutron flux (neutrons \cdot cm⁻² \cdot a⁻¹) is provided by a balance between the neutron production rate and the rates of absorption in the thermal energy range and the epithermal energy range just above the thermal level:

	$S_{ m i}$	Y_n^U	$Y_{\mathrm{n}}{}^{\mathrm{Th}}$	$\sigma_{ m th,i}$	$I_{\mathrm{a,i}}$	$\sigma_{ m sc,i}$	$A_{\rm i}$	$\xi_{ m i}$
Element	Mass stop- ping power $(MeV \cdot cm^2 \cdot g^{-1})$	Neutron yield (n per ppm U)	Neutron yield (n per ppm Th)	Thermal n abs. cross-section $(10^{-24} \text{ cm}^2/\text{ atom})$	Dilute resonance integral (10 ⁻²⁴ cm ² / atom)	Neutron scattering cross-section (10 ⁻²⁴ cm ² / atom)	Atomic weight (g/mol)	Energy loss per collision (unitless)
Н	1542			0.33	0	20.5	1.0	1.000
Li	548	21.1	9.6	70.5	0	0.95	6.9	0.264
Be	529	265	91.2					
В	527	62.3	19.2	767	343	4.27	10.8	0.174
С	573	0.45	0.18	0.0034	0.0016	4.74	12.0	0.158
0	527	0.23	0.079	0.0002	0.0002	3.76	16.0	0.12
F	472	30.8	11.8					
Na	456	14.5	6.8	0.53	0.311	3.025	23.0	0.084
Mg	461	5.8	2.6	0.063	0.038	3.42	24.3	0.08
Al	444	5.1	2.6	0.23	0.17	1.41	27.0	0.072
Si	454	0.69	0.335	0.17	0.082	2.04	28.1	0.07
Cl	420			33.5	13.7	15.8	35.45	0.055
Р	433	0	0	0.165	0.079	3.13	31.0	0.063
S	439	0	0					
Κ	414	0.45	0.305	2.15	1.00	2.04	39.1	0.05
Ca	428	0	0	0.43	0.235	2.93	40.1	0.049
Ti	375	0	0	6.1	3.1	4.09	47.9	0.041
Cr				3.1	1.6	3.38	52.0	0.038
Mn	353			13.3	13.4	2.20	54.9	0.036
Fe	351	0.19	0.205	2.56	1.39	11.35	55.8	0.035
Sm				9640	1400	38	150.4	0.013
Gd				41 560	390	172	157.3	0.013
UO ₂	74.7	0.077	0.027					

TABLE 6.2. VALUES FOR PARAMETERS USED IN CALCULATING ³⁶Cl PRODUCTION BY NEUTRON FLUX IN THE SUBSURFACE (from Fabryka-Martin (1988) [382])

$$\Phi_{n} = \frac{p(E_{th})}{\sigma_{m}} P_{n,total} + \frac{\left(1 - p(E_{th})\right)}{I_{eff}} P_{n,total}$$
(6.5)

where

$P_{n,total}$	is equal to the sum of $P_{n,sf}$ and $P_{n,\alpha}$;
$p(E_{\rm th})$	is the probability that a neutron will escape the epithermal energy range without being
	absorbed, called the resonance escape probability (unitless);
$\sigma_{ m m}$	is the macroscopic thermal neutron absorption cross-section (cm ² /g);
$I_{\rm eff}$	is the effective dilute resonance integral (cm ² /g) (Fabryka-Martin (1988) [382]).

The first term on the right hand side of Eq. (6.5) is the thermal neutron flux and the second term is the epithermal neutron flux. The macroscopic thermal neutron absorption cross-section and the effective dilute resonance integrals are equivalent to the total absorption cross-sections of all of the elements in the rock and pore fluid in the thermal and epithermal energy ranges, respectively, and are shown by:

$$\sigma_{\rm m} = \sum_{i} N_i \sigma_{\rm th,i} \tag{6.6}$$

$$I_{\rm eff} = \sum_{i} N_i I_{\rm a,i}$$
(6.7)

where

 N_i is the concentration of element *i* in atoms⁻¹; $\sigma_{\text{th},i}$ is the thermal neutron absorption cross-section of element *i* (cm²); $I_{a,i}$ is the dilute resonance integral for element *i*.

The elemental concentrations are referenced per gram of rock plus pore fluid and the summations should include concentrations in the pore fluid as well as rock.

The resonance escape probability is found by:

$$p(E_{\rm th}) = \exp \frac{-I_{\rm eff}}{\sum_{i} \xi_i N_i \sigma_{\rm sc,i}}$$
(6.8)

where

 $\sigma_{\text{sc},i}$ is the neutron scattering cross-section for element *i*;

is the average log decrement of energy loss per collision with an atom of element *i*.

For hydrogen, ξ_i is equal to 1.0 and for heavier elements it is a function of the atomic number, A:

$$\xi_i = \frac{2}{A_i + 0.667} \tag{6.9}$$

Values for $\sigma_{\text{th},i}$, $\sigma_{\text{sc},i}$, $I_{\text{a},i}$, A_i and ξ_i are provided in Table 6.2.

Given the fluxes as calculated above, the production rate for ${}^{36}Cl$ in the pore water (atoms ${}^{36}Cl$ in pore water \cdot (g aquifer)⁻¹ \cdot a⁻¹) is then simply the product of the neutron fluxes at the two energy levels and the cross-sections for the reactions yielding ${}^{36}Cl$ at those energies:

$$P_{36,pw} = \frac{N_{35,pw}\sigma_{35}}{\sigma_{m}} p(E_{th})P_{n,total} + \frac{N_{35,pw}I_{a,35}}{I_{eff}} (1 - p(E_{th}))P_{n,total}$$
(6.10)

where

 $N_{35,pw}$ is the concentration of ³⁵Cl in the pore water (atoms ³⁵Cl in pore water \cdot (g aquifer)⁻¹);

- σ_{35} is the cross-section for the reaction ${}^{35}Cl(n, \gamma){}^{36}Cl$ in the thermal energy range, equal to $(43.6 \pm 0.4) \times 10^{-24} \text{ cm}^2/\text{atom};$
- $I_{a,35}$ is the dilute resonance integral for the same reaction in the epithermal energy range, equal to $(18 \pm 2) \times 10^{-24} \text{ cm}^2/\text{atom}$ (Fabryka-Martin (1988) [382]).

For the purpose of estimating the age of old groundwater, the quantities of interest are usually the secular equilibrium ³⁶Cl concentration (atoms ³⁶Cl \cdot (L pore water)⁻¹) and the secular equilibrium ³⁶Cl/Cl ratio in the pore water (unitless):

$$C_{36,\text{se}} = \frac{P_{36,\text{pw}}}{\lambda_{36}} \left(\frac{\rho_{\text{B}} + n_{\text{e}} \rho_{\text{sol}}}{n_{\text{e}}} \right) 10^3$$
(6.11)

$$R_{36,se} = \frac{P_{36,pw} A_{n,Cl}}{C_{Cl} \lambda_{36} A_{v}} \left(\frac{\rho_{\rm B} + n_{\rm e} \rho_{\rm sol}}{n_{\rm e}}\right) 10^{6}$$
(6.12)

where

 $\begin{array}{ll} \lambda_{36} & \text{is the decay constant of } {}^{36}\text{Cl} (2.303 \times 10^{-6}\text{/a}); \\ \rho_{b} & \text{is the dry bulk density of the aquifer (g/cm^{3}); } \\ C_{C1} & \text{is the concentration of Cl}^{-} \text{ in the pore water (mg/L); } \\ \rho_{pw} & \text{is the density of the pore water solution (g/cm}^{3}); \\ n_{e} & \text{is the effective porosity (unitless); } \\ A_{n,Cl} & \text{is the atomic mass of natural Cl} (35.4527 \text{ g/mol}); \\ A_{v} & \text{is Avogadro's number (6.023 \times 10^{23} \text{ atoms/mol}). } \end{array}$

It should be noted that, strictly, the 'secular equilibrium' concentration or ratio refers to the theoretical value of these quantities for a chloride solution in contact with a specific rock over a very long period (>2 Ma). Actual groundwater may move through formations of varying chemistry or porosity, or change Cl concentration with time, and thus not achieve true equilibrium with the rock.

Typical values for $R_{36,se}$ range from $<1 \times 10^{-15}$ in ultramafic rocks to $\sim 50 \times 10^{-15}$ in granites or rhyolites (Bentley et al. (1986) [310]; Fabryka-Martin (1988) [382]; Lehmann et al. (1993) [250]; Phillips (2000) [306]). Lithologies having exceptionally high concentrations of U and Th can support ratios as large as 10^{-10} , but these are rarely encountered (Fabryka-Martin (1988) [382]). Phillips (2000) [306] compared ³⁶Cl secular equilibrium ratios measured on 56 water samples with the ratios calculated (by the authors of the papers) from chemical analyses of the host rocks. The average bias of the calculated ratios relative to the measured ones was <3% and the average absolute error was 33%. This constitutes an acceptable level of accuracy and precision for most hydrological purposes.

6.5.5.2. Subsurface systematics of ³⁶Cl

As described above, the simplest and most straightforward applications of ³⁶Cl dating are to aquifers recharging in the continental interior and permeable enough that subsurface sources of Cl-have been flushed away. In this case, ³⁶Cl model age as a function of flow distance can be obtained by application of the radioactive decay equation to the measured distribution of ³⁶Cl/Cl ratios. Figure 6.6 shows an example of this simple type of behaviour from the Nubian sandstone aquifer of north Africa (Patterson et al. (2005) [43]). Here, one set of samples (in blue) follows a clearly defined decay line between the initial recharge value and the subsurface secular equilibrium value. A second set (in red) has a more complicated history, evidently originating from a more evaporated recharge source and in some cases showing evidence of subsurface Cl⁻ addition. Nevertheless, both sets can be at least approximately dated by their positions down their respective decay lines.



FIG. 6.6. Variation in ³⁶Cl/Cl and the ³⁶Cl concentration down two flow paths in the Nubian sandstone aquifer of north Africa (Patterson et al. (2005) [43]).

In many cases, however, significant increases or fluctuations in Cl concentration, often accompanied by corresponding variations in the ³⁶Cl concentration or ratio are encountered. The most important processes affecting ³⁶Cl in the subsurface are radioactive decay, hypogene production (discussed above), mixing with other subsurface water, and the addition of Cl⁻ from evaporite dissolution. The basic equations for evaluating these systematics were laid out by Bentley et al. (1986) [301] and Phillips et al. (1986) [319] (see also Michelot (1988) [383]). They are based on the simultaneous interpretation of the ³⁶Cl concentration, the ³⁶Cl/Cl ratio and the Cl concentration. If the systematics of Cl variation can be reliably inferred, the simple mixing/decay equations from these sources can be employed to calculate ³⁶Cl model ages. Even if unambiguous arguments for one mechanism cannot be asserted, it is often possible to calculate ³⁶Cl model ages based on alternative hypotheses and, thus, provide useful bounds on the possible range of groundwater ages (Phillips (2000) [306]). Although more sophisticated numerical models can yield a detailed understanding of ³⁶Cl systematics in specific situations (e.g. Park et al. (2002) [90]), these fundamental equations still provide a sound basis at least for initial interpretations.

A mass balance of ³⁶Cl in the subsurface can be expressed as follows:

$$C_{36} = R_{\text{meas}}C_{\text{meas}} = R_{36,\text{re}}C_{\text{re}}\exp(-\lambda_{36}t) + \left((1-f)R_{36,\text{se1}} + fR_{36,\text{se2}}\right)C_{\text{re}}\left(1-\exp(-\lambda_{36}t)\right) + R_{36,\text{se2}}\left(C_{\text{meas}} - C_{\text{re}}\right) \quad (6.13)$$

where

 C_{36} is the ${}^{36}Cl$ concentration (atoms ${}^{36}Cl/L$); $R_{36,re}$ is the recharge ${}^{36}Cl/Cl$ ratio; C_{re} is the recharge Cl⁻ concentration (atoms Cl⁻/L); $R_{36,se1}$ is the secular equilibrium ${}^{36}Cl/Cl$ ratio in the aquifer; $R_{36,se2}$ is the secular equilibrium ${}^{36}Cl/Cl$ ratio in some source of Cl⁻ (such as a brine, an evaporite, diffusion out of an aquitard) being added to the system; C_{meas} is the measured Cl⁻ concentration of the sample (atoms/L);Ris the measured ${}^{36}Cl/Cl$ ratio of the sample and $f = (dC/dt)(\partial C_{-})$ is a term that accounts for

 R_{meas} is the measured ³⁶Cl/Cl ratio of the sample and $f = (dC/dt)(\lambda C_{\text{re}})$ is a term that accounts for the rate of addition of aquifer external subsurface Cl to the sample.

 $R_{36,se2}$ may or may not be the same as $R_{36,se1}$. If $R_{36,se1}$ is the same as $R_{36,se2}$, the solution of Eq. (6.13) is:

$$t = \frac{-1}{\lambda_{36}} \ln \frac{C_{\text{meas}} \left(R_{36,\text{meas}} - R_{36,\text{se}} \right)}{C_{\text{re}} \left(R_{36,\text{re}} - R_{36,\text{se}} \right)}$$
(6.14)

There are several circumstances that allow simplification of this formulation. One is that the Clbeing added originates from dissolution of bedded halite. In this case, R_{se} equals zero (Fabryka-Martin et al. (1987) [384]; Phillips (2000) [306]), no additional ³⁶Cl is added, and Eq. (6.14) reduces to:

$$t = \frac{-1}{\lambda_{36}} \ln \frac{C_{\text{meas}} R_{36,\text{meas}}}{C_{\text{re}} R_{36,\text{re}}}$$
(6.15)

Alternatively, variations in the concentration of ³⁶Cl and Cl⁻ down the flow path may arise from temporal variations in the amount of evapotranspiration during recharge, or from subsurface enrichment due to ion filtration. In either case, the ³⁶Cl and Cl⁻ are concentrated equally, the ³⁶Cl/Cl ratio does not change and Eq. (6.13) becomes:

$$t = \frac{-1}{\lambda_{36}} \ln \frac{R_{36,\text{meas}} - R_{36,\text{se}}}{R_{36,\text{re}} - R_{36,\text{se}}}$$
(6.16)

Equation (6.16) also applies when there is no change in the Cl⁻ concentration. Finally, there is the case where the Cl⁻ concentration increases due to diffusion of, or mixing with, brine that has a secular equilibrium ³⁶Cl/Cl different from that of the aquifer itself (i.e. $R_{36,se1} \neq R_{36,se2}$). In this case, the solution is:

$$t = \frac{-1}{\lambda_{36}} \ln \frac{C_{\rm re} \left(R_{36,\rm se2} - R_{36,\rm se1} \right) + C_{\rm meas} \left(R_{36,\rm meas} - R_{36,\rm se2} \right)}{C_{\rm re} \left(R_{36,\rm re} - R_{36,\rm se1} \right)}$$
(6.17)



FIG. 6.7. Hypothetical evolution of ³⁶Cl and Cl⁻ down four flow paths having a common initial composition, which is Cl⁻ = 50 mg/L, ³⁶Cl/Cl = 500 × 10⁻¹⁵ and ³⁶Cl concentration = 4.25×10^8 atoms/L. The aquifer is assumed to have a secular equilibrium of ³⁶Cl/Cl of 10 × 10⁻¹⁵. Arrows indicate the direction of the evolution. For all flow paths except B, the symbols are spaced at 50 ka intervals. Case A is simple decay towards R_{36,se}. Case B is dilution by 'dead' Cl without ageing. Case C is variable evapotranspiration during recharge. Case D is the addition of Cl due to diffusion out of an aquitard having R_{36,se} of 50 × 10⁻¹⁵. Colour keyed translucent arrows show the corresponding evolution paths in the two dimensional bounding planes.

Figure 6.7 illustrates four different evolutionary paths for water having a common initial composition, which is Cl⁻ = 50 mg/L, 36 Cl/Cl = 500 × 10⁻¹⁵ and 36 Cl concentration = 4.25 × 10⁸ atoms/L (this is equivalent to the closest vertex of the cube formed by the three coordinates in Fig. 6.7). The aquifer is assumed to have a secular equilibrium 36 Cl/Cl of 10×10^{-15} . Case A is simply constant recharge conditions and radiodecay down the flow path. The evolution is modelled over 2 Ma and the points are at 50 ka intervals (this is the same for all cases except B). Case A shows the linear correlation of $C_{36,\text{meas}}$ and $R_{36,\text{meas}}$, together with invariant Cl⁻, that is characteristic of simple decay in a closed system. Case B illustrates a situation in which the flow is so fast that ³⁶Cl decay is negligible but Cl⁻ progressively increases due to dissolution of halite ($R_{36.se} = 0$). The decrease in the ³⁶Cl/Cl ratio down the flow path may give the appearance of decay, but the invariant ³⁶Cl concentration and linear relation with inverse Cl⁻ identifies this path as merely dilution by 'dead' Cl⁻. Case C features variable Cl⁻ concentrations, ranging between 50 and 100 mg/L, and observed down the flow path due to climate driven changes in evapotranspirative concentration in the recharge area. The characteristic signature of this process is correlated changes in Cl⁻ and ³⁶Cl concentration (the snaky path followed by the dots in the figure), but a relatively smooth decrease in ³⁶Cl/Cl with flow distance. Instead of following Case B in a linear pattern to the right (low inverse Cl⁻), the data points lie in the same plane as Cases A and D. Finally, Case D is similar to Case A, except that Cl⁻ concentration increases steadily down the flow path to 150 mg/L due to the diffusion of Cl⁻ having a 36 Cl/Cl of 50 \times 10⁻¹⁵ out of a bounding shale. Here, instead of the linear pattern produced by simple decay, the various measures of concentration show a pronounced curvature 'hooking' to the right (i.e. towards low inverse Cl⁻). Figure 6.7 illustrates how differing histories produce characteristic and distinctive patterns that can be used to diagnose the appropriate approach to estimating groundwater age.

6.5.5.3. Examples of subsurface systematics

Three examples of ³⁶Cl systematics are provided in Fig. 6.8. The first (Fig. 6.8(a)) is from the Nubian sandstone aquifer (Patterson et al. (2005) [43]). As noted above, the ³⁶Cl systematics of this aquifer are very simple, having a relatively high meteoric input and simple decay without significant subsurface addition of Cl or ³⁶Cl. In Fig. 6.8, the ³⁶Cl evolution exhibits a linear trend sloping diagonally downwards towards low ³⁶Cl concentration and low ³⁶Cl/Cl. This is similar to the trend of line 'A' in Fig. 6.7, for simple ³⁶Cl decay.

The data points from the Milk River aquifer (Nolte et al. (1991) [291]; Phillips et al. (1986) [319]) differ from the Nubian sandstone in that they start at a lower inverse Cl concentration and form a trend that curves towards higher 1/Cl as the ³⁶Cl concentration and ³⁶Cl/Cl ratio decrease. Figure 6.8(b) is expanded from Fig. 6.8(a) in order to illustrate this trend in more detail for the distal flow path, but it leaves out the samples from the proximal portion of the flow path. This curved trajectory is similar to that of line 'D' in Fig. 6.7. Line 'D' modelled an increase of Cl concentration in the aquifer due to diffusion of Cl out of bounding aquitards. The same mechanism is believed to be operative in the Milk River aquifer (Fabryka-Martin et al. (1991) [385]; Nolte et al. (1991) [291]).

The third data set in Fig. 6.8(a) is from the Tokachi Basin in Japan (Mahara et al. (2007) [344]). This trend first shows a decrease in ³⁶Cl/Cl accompanied by an increase in Cl (decrease in 1/Cl), but without a significant decrease in the ³⁶Cl concentration. After the samples reach an inverse Cl <0.05 L/mg (Cl concentration >20 mg/L), they 'turn the corner' and the ³⁶Cl concentration increases along with Cl concentration, but the ³⁶Cl/Cl remains relatively constant. This pattern is unusual. The trend in the first part of the flow path is indicative of decay of meteoric ³⁶Cl/Cl accompanied by increasing Cl. Once the ³⁶Cl/Cl approaches secular equilibrium, it stabilizes but the Cl and ³⁶Cl increase. The stable ³⁶Cl/Cl is maintained by the Cl and ³⁶Cl increasing at the same rate. Mahara et al. (2007) [344] attribute this pattern to progressive solute concentration increase driven by ion filtration (reverse osmosis) and the trend shown in Fig. 6.8 is consistent with this explanation. However, the trend also resembles that of case 'D' in Fig. 6.7 (subsurface Cl addition) with an extended 'tail'. Inferences drawn from



FIG. 6.8. Examples of ³⁶Cl systematics. (a) Trends of ³⁶Cl/Cl, ³⁶Cl concentration and inverse Cl concentration in the Nubian sandstone aquifer (blue points; Patterson et al. (2005) [43]), the 'eastern flow path' on the Milk River aquifer (grey points; Nolte et al. (1991) [291]; Phillips et al. (1986) [319]), and the Tokachi Basin of Japan (red points; Mahara et al. (2007) [344]). The ³⁶Cl concentration and ³⁶Cl/Cl data have been normalized by dividing by the highest values in each data set in order to facilitate plotting on a single graph. (b) Expansion of (a) to more clearly illustrate trends in the Milk River aquifer. The dashed line shows the trend projected onto the ³⁶Cl concentration–inverse Cl plane.

additional environmental tracers might be useful to distinguish these possibilities, and this topic is discussed below.

A fourth example of subsurface ³⁶Cl systematics may be adduced from the south-western portion of the Great Artesian Basin aquifer in Australia. This aquifer, originally studied by Love et al. (2000) [292], has been reassessed in detail by R. Purtschert in Section 5.5 of this book. The figures and discussion will, therefore, not be reproduced here. The data from this study area are particularly informative because, as in the Nubian sandstone aquifer system, results from the independent ⁸¹Kr method are also available for comparison. This comparison reveals considerable complications in the subsurface systematics of the ³⁶Cl.

One notable characteristic of this aquifer is the very high chloride concentrations, ranging from >500 to 3000 mg/L. These are vastly above the Cl concentrations in precipitation, indicating that recharge water is evapotranspiratively concentrated by two to three orders of magnitude (Love et al. (2000) [292]). The aquifer is also bounded by a unit, the Bulldog Shale, that contains relatively large concentrations of Cl (up to 18 000 mg/L) and sufficient concentrations of radioactive elements to raise the subsurface equilibrium ratio to about 20×10^{-15} , four times that in the aquifer. In spite of these complications, the distribution of the ³⁶Cl/Cl ratio in the aquifer is a relatively regular function of flow distance (Figs 5.19 and 5.20), and, thus, creates the possibility that ³⁶Cl might produce useful groundwater age estimates.

The comparison with the ⁸¹Kr results given in Chapter 5 shows that the relatively smooth decline of ³⁶Cl/Cl ratios may be fortuitous. The measured Cl concentrations and ³⁶Cl/Cl appear to be a result of markedly varying contributions by evapotranspirative concentration during recharge and diffusive input from the Bulldog Shale during flow, rendering very difficult the calculation of a useful ³⁶Cl tracer age without independent quantification of at least one of these processes.

The results from the ⁸¹Kr comparison bear out the concerns of Love et al. (2000) [292], who warned that "The preceding discussion emphasizes that estimates of 'absolute' groundwater age using ³⁶Cl data are subject to large uncertainties because of problems of estimating the initial concentration of ³⁶Cl... and correcting for sources or sinks of chloride...". As emphasized above in this chapter, ³⁶Cl dating is most likely to yield useful results when the Cl and ³⁶Cl systematics are simple and the subsurface ³⁶Cl is dominated by meteoric input. The south-western Great Artesian Basin offers strong support for this caution. The combination of extreme (and, therefore, potentially highly variable) evapotranspirative concentration and large subsurface sources of Cl and ³⁶Cl warns of complications that are too large for reliable dating corrections. Potential users of the method should carefully evaluate their study areas for similar problems.

6.5.6. Use of other environmental tracers to interpret chloride systematics

As illustrated above, although the end member cases illustrated in Fig. 6.6 are clearly distinguishable, in some real world cases there may be multiple processes influencing ³⁶Cl and Cl patterns, or there may be insufficient data to distinguish fully between alternative hypotheses. The past 20 years have seen a major advance in the development of additional tracers that can be examined in conjunction with the ³⁶Cl and Cl patterns and that can provide independent constraints on chloride systematics.

Probably the simplest and most cost effective of these is measurement of the concentration of Br along with Cl⁻ (Davis et al. (1998) [296]; Davis et al. (2004) [386]; Whittemore (1995) [387]). Most meteoric waters over the continents have a Cl/Br (mass:mass) value lower than that of sea water, which is 290. This is because during the formation of marine aerosols, Br is preferentially fractionated into the smaller particles which persist longer in the atmosphere and are, thus, more readily transported towards the continental interiors (Davis et al. (2004) [386]). Cl/Br ratios between 50 and 150 are characteristic of continental interiors.

In contrast, solutions originating from dissolution of marine evaporites or from connate fluids tend to have ratios of between 300 and 1000 (Whittemore (1995) [387]). Such solutions start at the marine



FIG. 6.9. The evolution of the ³⁶Cl concentration and the Cl/Br ratio for the same hypothetical cases as in Fig. 6.7.



FIG. 6.10. (a) Relation between $\delta^{37}Cl$ and the Cl concentration in groundwater from the Great Artesian Basin of Australia (Zhang et al. (2007) [304]); (b) relation between $\delta^{37}Cl$ and 1/Cl in the Nubian aquifer of north Africa (Patterson et al. (2005) [43]).

ratio of 290 and, inasmuch as Br is excluded during the precipitation of halite, can have ratios of up to several thousand. These characteristics are convenient for the differentiation of Cl sources, since recharge water will generally possess a low Cl/Br value and subsurface sources of Cl will have high Cl/Br values. Figure 6.9 illustrates the use of Cl/Br to distinguish sources of Cl in the scenarios illustrated in Fig. 6.6. The recharge water is assumed to have a Cl/Br ratio of 100 and the subsurface source a ratio of 1000. The cases in which subsurface Cl is added show an evolution to the right of the graph whereas those where changes in Cl are not subsurface related only evolve in the vertical.

The stable isotope composition of the Cl is another environmental tracer that is integral to the halides and can help elucidate the origins of Cl within aquifer systems (Rao et al. (2005) [388]; Stewart and Spivack (2004) [389]; Whittemore (1995) [387]). The δ^{37} Cl of the ocean and of marine evaporites has apparently been within ±0.5‰ of 0‰ throughout the Phanerozoic (Eastoe et al. (2007) [390]). However, the δ^{37} Cl of Cl⁻ in pore fluids of shales seems to range between -1 and -2‰ (Zhang et al. (2007) [304]) and addition of Cl from this source is probably responsible for the generally negative

(~0 to -2%) values often found in sedimentary basin waters (Weaver (2000) [391]). In contrast, marine aerosols usually have positive δ^{37} Cl, varying between +0.5 and +2.5‰ (Volpe and Spivack (1994) [392]). This difference in atmospheric and subsurface isotopic signatures can help to fingerprint the origin of Cl⁻ in water being dated with ³⁶Cl.

Figure 6.10 relates Cl⁻ and δ^{37} Cl in two systems: the Great Artesian Basin (Zhang et al. (2007) [304]) and the Nubian aquifer (Patterson et al. (2005) [43]). The Great Artesian Basin data show a clear trend of decreasing δ^{37} Cl with increasing Cl⁻ concentration. Direct measurement of Cl⁻ in pore water from bounding shale units confirmed that diffusion of Cl⁻ out of the shale was the likely source of the increased Cl⁻ with flow distance in this aquifer. However, three samples show increased Cl⁻ with relatively constant δ^{37} Cl. These are from a distinct portion of the basin and the likelihood that this Cl⁻ increase is due to recharge area evaporation is supported by independent evidence.

The data from the Nubian aquifer (Patterson et al. (2005) [43]) exhibit a more complex pattern. The spacing of wells in the Western Desert of Egypt is irregular and does not permit as comprehensive a view of the spatial distribution of water quality. However, the δ^{37} Cl clearly aids in distinguishing different groups of waters characterized by differing Cl⁻ concentrations and, thus, aids in interpreting ³⁶Cl data.

In summary, even though Cl has unusually simple geochemistry, the evolution of the ³⁶Cl concentration and the ³⁶Cl/Cl ratio down flow paths can still exhibit considerable complexity that reflects the heterogeneity of water sources and transport mechanisms in the subsurface. These trends have generally been thought of as requiring 'correction' of the calculated ³⁶Cl model ages, but are perhaps better considered as hallmarks of the water history. For example, diffusion of low ³⁶Cl/Cl chloride out of an aquitard into an aquifer is also indicative of diffusion of 'old' water molecules out of the aquitard, and correspondingly, diffusion of 'young' aquifer water into the aquitard. Variable ³⁶Cl ratios due to variable evapotranspiration during recharge probably also indicate variations in the recharge rate, and hence groundwater velocity. As noted in Chapter 1, the interpretation of age tracer data is most valuable when it is comprehensive, in other words, when a large number of different tracers can be interpreted within a reasonably well defined hydrogeological framework and be reconciled with a single, coherent history and set of processes. This chapter has focused on the calculation of single valued ³⁶Cl tracer ages, but integrating the ³⁶Cl patterns into a more comprehensive data set may permit estimation of actual frequency distribution of groundwater age.

A significant amount of recent research has explored the use of additional environmental tracers to yield information on halide systematics. Examples include ¹²⁹I (Fabryka-Martin et al. (1991) [385]; Snyder and Fabryka-Martin (2007) [393]), the Cl/Br ratio (Davis et al. (2000) [394]; Hurwitz et al. (2005) [395]; Metcalfe et al. (2007) [396]; Rao et al. (2005) [388]), δ^{37} Cl (Lehmann et al. (2003) [256]; Zhang et al. (2007) [304]) and ⁴He (Kulongoski et al. (2008) [343]; Mahara et al. (2007) [344]; Patterson et al. (2005) [43]). The application of one or several of these tracers, all associated with the systematics of Cl or ³⁶Cl in some way, can greatly help to constrain sources of Cl and ³⁶Cl or to explain variations in their distributions.

6.6. COMPARISON OF ³⁶Cl WITH OTHER METHODS OF DATING

As discussed in the introduction to this book, interpretation of age dating tracers is most informative when multiple methods can be compared. In this section, the patterns of ³⁶Cl are compared with those of other tracers in several aquifer systems.

6.6.1. Comparison with radiocarbon

Unfortunately, the useful range of ³⁶Cl in groundwater does not overlap with that of radiocarbon. The decay of ³⁶Cl is still small when ¹⁴C has decayed beyond the limit of practical application. This is



FIG. 6.11. Variation of ¹⁴C activity and ³⁶Cl/Cl with flow distance in the Ojo Alamo and Nacimiento aquifers of the San Juan Basin, south-western USA. Data are from Phillips (2000) [306], Plummer (1996) [356] and Stute et al. (1995) [213]. The open squares are ³⁶Cl/Cl corrected for radioactive decay using the inferred ¹⁴C model age.

illustrated in Fig. 6.11, where radiocarbon and ³⁶Cl are compared in the Ojo Alamo and Nacimiento aquifers of the San Juan Basin, south-western USA (Phillips (2000) [306]; Plummer (1996) [356]; Stute et al. (1995) [213]). The ¹⁴C activity exhibits a quasi-exponential decrease with flow distance, as expected. By ~30 km, the activity is too low to yield useful groundwater age estimates. As predicted, the ³⁶Cl/Cl is approximately constant over this interval. The open squares in Fig. 6.11 show the ³⁶Cl/Cl corrected for decay using the radiocarbon model age. Given the observed variability in the ³⁶Cl/Cl, this decay is too small to be useful for groundwater age estimation. The pattern of lower Holocene ³⁶Cl/Cl compared with the late Pleistocene is due to secular variation of the ³⁶Cl production, modulated by the dipole geomagnetic field strength.

6.6.2. Comparison with ⁴He

Only a few age tracers significantly overlap with ³⁶Cl. One of the best is ⁴He accumulation. Figure 6.12 compares ⁴He accumulation, ³⁶Cl and ¹⁴C along the 'eastern flow path' in the Milk River aquifer (Drimmie et al. (1991) [168]; Nolte et al. (1991) [291]; Phillips et al. (1986) [319]). The ¹⁴C adds little information, but is consistent with the other tracers. The first sample on the flow path contains about 10 pmc and the rest negligible ¹⁴C.

The ³⁶Cl shows a quasi-exponential decay with flow distance. In Fig. 6.12, this profile has been fitted using the following equation:

$$R_{36}\left(x\right) = R_{0,36} \exp\left(-\lambda_{36} \frac{x}{q_s}\right)$$
(6.18)

where

 $R_{36}(x)$ is the ³⁶Cl/Cl ratio as a function of flow distance;

 $R_{0,36}$ is the initial ³⁶Cl/Cl ratio;

 $q_{\rm s}$ is the seepage velocity of the groundwater.



FIG. 6.12. Trends of 36 Cl/Cl, 4 He and 14 C with flow distance down the Milk River aquifer. Data are taken from Drimmie et al. (1991) [168], Nolte et al. (1991) [291] and Phillips et al. (1986) [319]. The red line illustrates the fit of an exponential decay model (Eq. (6.18)) to the 36 Cl/Cl data and the blue line the fit of a linear accumulation model to the 4 He model. Details are discussed in the text.

The fit illustrated employed $R_{0,36} = 700 \times 10^{-15}$ and $q_s = 5$ cm/a. This simplistic dating approach neglects subsurface addition of Cl and ³⁶Cl, which is undoubtedly significant in this case (Nolte et al. (1991) [291]; Phillips (2000) [306]), but gives a first order idea of the behaviour of the system.

The good fit to this simple equation (Eq. (6.18)) indicates that flow velocity is approximately constant. If this is the case, and if ⁴He is introduced to the aquifer at a constant rate, then ⁴He should accumulate linearly with distance. Figure 6.12 shows that there is indeed a linear accumulation, with ⁴He increasing at the rate of 1.3×10^{-6} cm³ STP \cdot cm⁻³_{H2O} \cdot km⁻¹. Assuming a seepage velocity of 5 cm/a, this is equivalent to a helium influx of 6×10^{-11} cm³ STP \cdot cm⁻³_{H2O} \cdot a⁻¹. The calculated contribution rate of ⁴He from the rock matrix is approximately one order less than this value, if all the ⁴He produced is assumed to diffuse into the pore water (Andrews et al. (1991) [397]). If the ⁴He is instead assumed mostly to access the aquifer water by upward diffusion from the crust beneath, the ⁴He flux would be approximately 5×10^{-4} cm³ STP \cdot m⁻² \cdot a⁻¹. This is not an especially large flux. In any case, the exponential dependence of the ³⁶Cl/Cl ratio with distance and the linear dependence of the ⁴He confirm that the trends are consistent with the basic conceptual models for both isotopes that have been presented in this volume.

6.6.3. Comparison with ⁸¹Kr

Another dating method that overlaps very well with ³⁶Cl is ⁸¹Kr, with a half-life of 229 000 a. Although the technology for ⁸¹Kr measurement is relatively new and has, therefore, only been studied in relatively few localities, both nuclides have been measured in the Nubian sandstone aquifer system (Sturchio et al. (2004) [5]). Figure 6.13 shows the ³⁶Cl/Cl ratio as a function of the model ⁸¹Kr age. If the two dating methods are consistent, ³⁶Cl/Cl should fall along a trend determined by the following equation:

$${}^{36}\text{Cl/Cl}_{\text{meas}} = \left[{}^{36}\text{Cl/Cl}_{\text{o}} - {}^{36}\text{Cl/Cl}_{\text{se}} \right] \exp(-\lambda_{36}t_{81}) + {}^{36}\text{Cl/Cl}_{\text{se}}$$
(6.19)



FIG. 6.13. ³⁶Cl/Cl ratios measured in the Nubian sandstone aquifer of Egypt as a function of groundwater age calculated using measured ⁸¹Kr/Kr ratios, from Sturchio et al. (2004) [5]. The blue line is the ³⁶Cl/Cl ratio calculated from the ⁸¹Kr model age using Eq. (6.19).

where ${}^{36}\text{Cl/Cl}_{o}$ is the recharge ratio; ${}^{36}\text{Cl/Cl}_{se}$ is the secular equilibrium ratio; t_{81} is the model ${}^{81}\text{Kr}$ age.

In Fig. 6.12, the data have been fitted to Eq. (6.19) with ${}^{36}\text{Cl/Cl}_{o} = 131 \times 10^{-15}$ and ${}^{36}\text{Cl/Cl}_{se} = 8 \times 10^{-15}$. An initial ${}^{81}\text{Kr/Kr}$ ratio of $1.10(\pm 0.05) \times 10^{-12}$ was used in calculating the simple exponential decay ${}^{81}\text{Kr}$ model age. The agreement between the calculated and measured ${}^{36}\text{Cl/Cl}$ ratios is generally good, especially considering that no effort was made to correct the model ${}^{36}\text{Cl}$ ages for subsurface additions of Cl and ${}^{36}\text{Cl}$.

6.6.4. Comparison without a well defined flow path

In some cases, general concordance between ³⁶Cl trends and those of independent tracers can be established even if a clear-cut flow path cannot be distinguished. This is illustrated in Fig. 6.14, where ³⁶Cl and ⁴He data from the Tokachi Basin in Japan are plotted (Mahara et al. (2007) [344]). Here, the data are too scattered and irregular to allow evaluation of a flow path. However, the relation between the temporal patterns of accumulation of ³⁶Cl and ⁴He can still be evaluated. A simplistic model for the dependence of ³⁶Cl/Cl on time is shown by:

$${}^{36}\text{Cl/Cl}(t) = {}^{36}\text{Cl/Cl}_{0}\exp(-\lambda_{36}t) + {}^{36}\text{Cl/Cl}_{se}\left[1 - \exp(-\lambda_{36}t)\right]$$
(6.20)

where ${}^{36}Cl/Cl_o$ is the recharge ${}^{36}Cl/Cl$ ratio and ${}^{36}Cl/Cl_{se}$ the secular equilibrium ratio. The ${}^{4}He$ accumulation is equally simplistically given by:



FIG. 6.14. ${}^{36}Cl/Cl$ ratio as a function of ${}^{4}He$ content in groundwater from the Tokachi Basin, Japan. Data are from Mahara et al. (2007) [344]. The blue line is ${}^{36}Cl/Cl$ as a function of ${}^{4}He$ accumulation, calculated from Eq. (6.22).

$${}^{4}\text{He}(t) = A_{4\text{He}}t \tag{6.21}$$

where A_{4He} is the accumulation rate of ⁴He. Equation (6.21) can be substituted into Eq. (6.22) to yield:

$${}^{36}\text{Cl/Cl}(t) = {}^{36}\text{Cl/Cl}_{o}\exp\left(-\lambda_{36}\frac{{}^{4}\text{He}}{A_{4\text{He}}}\right) + {}^{36}\text{Cl/Cl}_{se}\left[1 - \exp\left(-\lambda_{36}\frac{{}^{4}\text{He}}{A_{4\text{He}}}\right)\right]$$
(6.22)

In Fig. 6.14, the solution of equation 6.22 is shown for ${}^{36}\text{Cl/Cl}_{o} = 60 \times 10^{-15}$, ${}^{36}\text{Cl/Cl}_{se} = 10 \times 10^{-15}$, and $A_{4\text{He}} = 9 \times 10^{-7} \text{ cm}^3 \text{ STP} \cdot \text{cm}^{-3} \cdot \text{a}^{-1}$. This calculated curve matches the data well, confirming that both ${}^{36}\text{Cl}$ and ${}^{4}\text{He}$ are following the expected conceptual models and allowing the ${}^{4}\text{He}$ accumulation rate to be estimated. As for the Milk River aquifer, the original authors offer a more nuanced interpretation.

6.6.5. Summary

Chlorine-36 has been used to estimate groundwater ages in numerous old groundwater systems over the past 20 years. The systematics are well understood, with ³⁶Cl principally produced in the atmosphere and entering the aquifer along with groundwater recharge. Once in the subsurface, ³⁶Cl acts quite conservatively, leaving radiodecay as the only significant sink. The main complication for ³⁶Cl dating of old groundwater is the subsurface introduction of chloride, with accompanying ³⁶Cl. However, straightforward corrections for this mixing are possible if the nature of the subsurface processes is evaluated. Results from ³⁶Cl dating of old groundwater can now be compared with those from a variety of other methods of dating. These comparisons are generally internally consistent and support the widespread use of ³⁶Cl for dating old groundwater.

Chapter 7

DATING OF OLD GROUNDWATER USING URANIUM ISOTOPES — PRINCIPLES AND APPLICATIONS

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7.1. INTRODUCTION

This chapter provides background on the behaviour of uranium isotopes in groundwater and shows that uranium isotope disequilibrium presents a method that has the potential to play an important role within the concerted application of techniques to date old groundwater. Depending on the geochemistry of the aquifer system, the potential dating range extends from about 10 ka up to 1 Ma, which overlaps the ¹⁴C and the ³⁶Cl/⁸¹Kr dating ranges. Uranium isotopes can provide independent information relevant to groundwater age that complements other dating approaches and may help resolve ambiguities in data interpretation. Moreover, uranium isotopes in groundwater have the potential for quantifying geochemical parameters of the water–rock interaction and represent natural analogues for radioactive waste. Any multitracer application to date old groundwater should integrate uranium isotope measurements, which can easily be afforded by the use of modern mass spectrometric techniques.

Among the natural decay series radionuclides, the uranium isotopes ²³⁴U and ²³⁸U and the ratio of activity of these isotopes (²³⁴U/²³⁸U) provide the greatest potential to trace natural water and to date old groundwater. Moreover, they are very useful as natural analogues in assessing the behaviour of radionuclides in nuclear waste disposal sites.

7.1.1. History

In 1955, V.V. Cherdyntsev and P.I. Chalov discovered that in secondary minerals and natural water, ²³⁴U and ²³⁸U predominantly occur in radioactive disequilibrium, i.e. the activity ratio ²³⁴U/²³⁸U is different from unity (Cherdyntsev et al. (1955) [398]). Subsequent studies have shown that this disequilibrium is a consequence of the energetic alpha decay of ²³⁸U that causes recoil fractionation between ²³⁴U and ²³⁸U due to differential release of ²³⁴U and ²³⁸U from the rock into the surrounding water (Chalov and Merkulova (1966) [399]; Cherdyntsev (1969) [400]; Osmond and Cowart (1976) [401]; Osmond and Cowart (1982) [402]). This disequilibrium found wide application in surface and groundwater studies.

In aerobic aqueous systems, measurements of uranium and ²³⁴U/²³⁸U have been used to trace the flow of river water and groundwater (Plater et al. (1992) [403]; Porcelli and Swarzenski (2003) [404]; Sarin et al. (1990) [405]; Tuzova (1986) [406]; Tuzova and Novikov (1991) [407]), establish timescales of weathering processes (Andersen et al. (2009) [408]; Dosseto et al. (2008) [409]; Vigier et al. (2006) [410]), quantify mixing of surface and groundwater (Briel (1976) [411]), and identify groundwater inflow into surface water (Durand et al. (2005) [412]).

The suitability of uranium isotope disequilibrium as a tracer and timer of groundwater was first demonstrated by Osmond et al. (1968) [413] and later by Chalov et al. (1979) [414], Osmond and Cowart (1976) [401], and Osmond et al. (1983) [415]. Given the long half-life of 234 U (2.45 × 10⁵ a), many attempts have been made to apply 234 U/ 238 U and/or the 234 U excess (difference in the activity concentration of 234 U and 238 U) to date old groundwater up to hundreds of thousands of years (Andrews et al. (1982) [416]; Andrews and Kay (1983) [417]; Barr et al. (1979) [418]; Cowart and Osmond (1974) [419]; Eshova (1981) [420]; Fröhlich et al. (1984) [421]; Ivanovich et al. (1991) [422]; Kigoshi (1973)

[423]; Kronfeld and Adams (1974) [424]; Pearson et al. (1983) [425]). Cowart and Osmond (1974) [419] noted that groundwater age derived from the decay of ²³⁴U excess may represent the migration time of the uranium tracer rather than the travel time of the groundwater. Consequently, any attempt to use the uranium isotope disequilibrium for groundwater studies requires a thorough knowledge of the sorption behaviour of these isotopes in the aquifer system (Fröhlich and Gellermann (1987) [426]).

The past two decades have seen a rapid expansion in the use of uranium series disequilibrium in a variety of disciplines such as geochronology, geochemistry and hydrology. Among others, applications of uranium isotopes to groundwater studies are reported by Bonotto (2000) [427], Bonotto (2006) [428], Deschamps et al. (2004) [429], Luo et al. (2000) [430], Rogojin et al. (1998) [431] and Tricca et al. (2001) [432]. Many recent studies take advantage of new analytical techniques, which began in the late 1980s with the use of thermal ionization mass spectrometry for the measurement of uranium isotopes and other radionuclides of the natural decay series (Chen et al. (1986) [433]). The application of multicollector inductively coupled plasma mass spectrometry (MC-ICP-MS) especially allowed measurement of much smaller water samples with greater accuracy and a significant increase in the measuring capacity in comparison to alpha spectrometry (Goldstein and Stirling (2003) [434]). The MC-ICP-MS technique enables high precision measurements of previously undetectable variations in many elements, including isotopic fractionation between ²³⁵U and ²³⁸U in water (Rademacher et al. (2003) [435]). Achievements have also been made in quantifying the effects of preferential release of ²³⁴U in weathering and erosion studies both by laboratory and field experiments (Andersen et al. (2009) [408]). In conclusion, the advent of mass spectrometric analysis of uranium isotopes, which is quicker and more precise, may enable broader application of this method and its practical application.

7.1.2. Scope and objective

This review is focused on the uranium isotope disequilibrium in groundwater and its relevance to dating of old groundwater. First, the natural abundance of uranium isotopes and their geochemical behaviour in groundwater will briefly be discussed. Second, a critical review of the models used to derive information from uranium isotope measurements on groundwater age will be given. Special emphasis is placed on a conceptual model incorporating water–rock interaction that has been used for dating old groundwater. Finally, some case studies will be discussed which demonstrate the strengths and limitations of the uranium isotope groundwater dating technique and its integration into multitracer approaches to date old groundwater. Developments in the use of uranium and ²³⁴U/²³⁸U have been reviewed by Cherdyntsev (1971) [436], Osmond (1980) [437], Osmond and Cowart (1976) [401], Osmond and Cowart (1992) [438], and Osmond and Cowart (2000) [439]. Monographs on this subject have been published by Ivanovich and Harmon (1982) [440], Ivanovich and Harmon (1992) [441] and, more recently, by Bourdon et al. (2003) [442].

7.2. NATURAL ABUNDANCE OF URANIUM ISOTOPES

Naturally occurring uranium consists of three alpha active isotopes: ²³⁸U, ²³⁵U and ²³⁴U. The first two isotopes are initial members of the corresponding natural radioactive decay series and the latter one is a decay product of ²³⁸U (Fig. 7.1). The ²³⁵U activity in natural uranium is less than 5% of the ²³⁸U activity and, thus, has not been used for hydrological applications. Given the relatively short half-life of ²³⁴U (2.455 × 10⁵ a) compared with ²³⁸U (4.468 × 10⁹ a), these two uranium isotopes are expected to be globally in secular radioactive equilibrium, i.e. ²³⁴U/²³⁸U = 1. It was, therefore, a surprise when Cherdyntsev et al. (1955) [398] reported that in some geological objects, radioactive equilibrium is disturbed. In groundwater, the ²³⁴U/²³⁸U ratio is usually >1, while in weathered rock, for instance, this ratio can be distinctly <1.

TI	238	²³⁸ U				2	³⁴ U
	4.468×10 ⁹ a					2.455×10 ⁵ a	
Da		a		²³⁴ Pa	1	β	
1 a		, u		1.17 m			α
ть	²³⁴ Th		β			23	⁰ Th
1 11	24.1 d					75.38×10 ³ a	
Ac							α
Ra						22 10	⁶ Ra 502 a
Fr							α
Dn						22	² Rn
						3.	824 d

FIG. 7.1. Part of the ²³⁸U decay series (from ²³⁸U to ²²²Rn).

The quantities used to express uranium abundance and measuring results include the following:

- Uranium activity concentration = uranium activity (Bq or mBq) divided by volume of water (L) in which uranium is dissolved.
- Uranium concentration = mass of uranium (mg or μg) divided by volume of water (L) in which uranium is dissolved.
- Specific activity of uranium = uranium activity (Bq or mBq) divided by mass of substance (kg) containing the uranium.
- (Relative) uranium content = mass of uranium divided by mass of substance containing the uranium (g/g, ppm = 1 mg U/1 kg of substance, or 1 ppb = 1 μ g U/1 kg of substance).
- Uranium activity ratio = activity of 234 U divided by activity of 238 U in a given sample.

It should be noted that 1 ppm uranium corresponds to a specific activity of 12.4 Bq/kg.

In ocean water, related to a salinity of 35‰, uranium concentration ranges from 3.162 to 3.281 µg/L (Chen et al. (1986) [433]) and the activity ratio is 1.147 ± 0.001 (Andersen et al. (2007) [443]; Robinson et al. (2004) [444]) (Table 7.1). In continental surface water, the uranium content varies between 10^{-3} and 10^{3} ppb, and the activity ratio ranges from 1 to 2 (Osmond and Cowart (1976) [401]). Most of the 234 U/ 238 U values of lakes and rivers are between 1.1 and 1.4 (Chabaux et al. (2003) [445]; Ferronsky and Polyakov (1982) [446]).

Groundwater shows the largest variation both of uranium concentration and the activity ratio. An evaluation of nearly 800 measurements published at the beginning of the 1980s (Gellermann and Fröhlich (1984) [447]) uncovered a logarithmic normal distribution of uranium concentration with an average value of 1 ppb and a range from 10^{-3} to 10^4 ppb. The lower end of this distribution corresponds to the analytical detection limit by alpha spectrometric measurements of uranium made in 1984; in reality, uranium concentrations may be even lower. The activity ratios in groundwater ranged from 0.5 to about 30; values >5 were mainly associated with low uranium concentrations. None of the published activity ratio values were below 0.5; this appears to be in agreement with theoretical considerations of Bondarenko (1981) [448]. The frequency distribution of the $^{234}U/^{238}U$ activity ratio is generally asymmetric and strongly depends on the type of water-bearing rocks. In an extensive study of groundwater from Kazakhstan, Syromyatnikov (1961) [449] found characteristic frequency distributions of $^{234}U/^{238}U$ for various rock types (Fig. 7.2).

Object	Uranium content (ppm)	²³⁴ U/ ²³⁸ U	
Sedimentary rocks			
carbonates	0.6 ± 0.5	0.92 ± 0.01	
clays	2 ± 1	0.9 ± 0.1	
phosphorites	100	1.0-1.15	
Igneous rocks			
mafic	0.9	(1.0)	
diorites	2	(1.0)	
granodiorites	2.6	(1.0)	
silicic volcaneous	5	(1.0)	
Magma (basalt)	0.078	(1.0)	
Ocean water	$3.3 imes 10^{-3}$	1.147 ± 0.001	
Groundwater	1×10^{-3} (1-10 ⁻⁶)	1.5 (0.5–30)	

TABLE 7.1. URANIUM CONTENT AND ²³⁴U/²³⁸U IN ROCKS AND NATURAL WATERS



FIG. 7.2. Histograms of ${}^{234}U/{}^{238}U$ distribution in the groundwater of igneous rocks (a), sedimentary and metamorphic rocks (b) and uranium ores (c) (from Ferronsky and Polyakov (1982) [446]).

7.3. URANIUM GEOCHEMISTRY

In natural waters, the prevailing valence states of uranium are +4 and +6. During weathering, uranium is oxidized to the hexavalent uranyl ion $UO_{2^+}^2$ which forms soluble complexes with $CO_{3^-}^2$ and $PO_{4^-}^3$ under near-neutral conditions, and with $SO_{4^-}^2$, F⁻ and Cl⁻ at lower pH values (Langmuir (1978) [450]). The presence of these complexing ions inhibits adsorption and, hence, is mainly responsible for the mobility of uranium observed in natural waters (Rose and Wright (1980) [451]). Under oxidizing conditions, typical uranium concentrations in water are close to 1 ppb (Osmond and Cowart (1992) [438]). Under reducing conditions, uranium occurs in the tetravalent state and is stable as U(OH)₄; the maximum uranium concentration is at about 0.06 ppb, which corresponds to the solubility limit of uraninite (UO₂) (Gascoyne (1992) [452]).

Adsorption and precipitation processes are important in controlling the uranium isotope migration in groundwater. Dissolved UO_2^{2+} is susceptible to adsorption, especially by organic matter such as humic acids (Lenhart and Honeyman (1999) [453]), iron oxyhydroxides and micas (Ames et al. (1983) [454]; Arnold et al. (1998) [455]; Duff et al. (2002) [456]; Hsi and Langmuir (1985) [457]; Liger et al. (1999) [458]). The retention of adsorbed uranium, and thus also of ²³⁴U excess, depends on the pH of the solution. Silicate mineral surfaces generally have high uranium retention at a pH of 5–10, while at pH < 4 the uranium retention is low (Krawczyk-Barsch et al. (2004) [459]). During crystallization of Fe minerals, uranium that has been exchangeably adsorbed by the originally amorphous Fe hydroxides can irreversibly be incorporated into more stable sites (Ohnuki et al. (1997) [460]; Payne et al. (1994) [461]). This long term precipitation of Fe minerals can transfer a significant fraction of adsorbed uranium onto surface coatings. Uranium sorption on goethite was found to be initially reversible, but after some months a portion of this uranium removal is of the order of, or higher than, the decay constant of ²³⁴U, it may be difficult to disentangle the effects of the two processes on uranium evolution over greater distances.

Studies of the uranium isotopic composition along the groundwater flow from the outcrop to confined deeper regions of aquifers revealed the existence of three zones (Fig. 7.3) with different ²³⁴U/²³⁸U ratios and uranium contents (Andrews and Kay (1983) [417]; Andrews and Kay (1982) [463]; Osmond and Cowart (1982) [402]): (i) an oxidizing zone (often coinciding with the vadose zone where weathering takes place) characterized by high uranium content and a moderate ²³⁴U/²³⁸U ratio; (ii) a redox front with decreasing uranium concentration due to reduction of hexavalent uranium to rather insoluble tetravalent uranium and with a high ²³⁴U/²³⁸U ratio due to enhanced recoil of ²³⁴U from precipitated phases; and (iii) a reduced zone with low uranium content and varying ²³⁴U/²³⁸U.

There are three effects that give rise to the observed disequilibrium between ²³⁴U and ²³⁸U: (i) preferential release of more loosely bound ²³⁴U from damaged mineral lattice sites; (ii) release of ²³⁴U excess adsorbed on mineral grain surfaces in contact with the aqueous phase; and (iii) direct recoil of ²³⁴Th (the immediate short lived daughter of ²³⁸U) from near mineral surface boundaries into the surrounding aqueous phase. The first effect is a consequence of the nuclear recoil by the energetic alpha decay of ²³⁸U and ²³⁴Th. This recoil induces bond breaks and lattice damage and displaces decay products into weakly bound interstitial (surficial) sites of the mineral grains (Chalov and Merkulova (1966) [399]; Cherdyntsev (1971) [436]; Fleischer (1980) [464]; Fleischer (1982) [465]; Hussain and Lal (1986) [466]; Rosholt et al. (1963) [467]; Zielinski et al. (1981) [468]). A further cause for the disequilibrium is the ionization of ²³⁴U from a 4⁺ to 6⁺ valence state by stripping two of its electrons



FIG. 7.3. Schematic of uranium isotope evolution along a confined aquifer; preferential leaching under oxidizing conditions, precipitation in the redox zone and recoil ejection and radioactive decay of ²³⁴U.

during the decay sequence ${}^{238}U(4^+) \rightarrow {}^{234}Th(4^+) \rightarrow {}^{234}Pa(5^+) \rightarrow {}^{234}U(6^+)$ (Dooley et al. (1966) [469]). An alternative explanation of the ${}^{234}U$ oxidation has been found by computer simulations of the recoil process (Adloff and Roessler (1991) [470]). These simulations suggest that recoiling ${}^{234}Th$ atoms push the oxygen atoms of the mineral in front of it so that the final resting location of ${}^{234}Th$ becomes enriched in oxidizing species. These species subsequently oxidize ${}^{234}U$ after decay of ${}^{234}Th$.

The various mineral phases of a given rock type do not only have different susceptibility to lattice damage induced by alpha decay, but also differring ability to anneal (recover from) this damage. In general, lattice defect recovery is a slow process at normal groundwater temperatures and, thus, some silicate minerals are comparatively susceptible to preferential release of ²³⁴U from damaged lattice sites (Andersen et al. (2009) [408]; Eyal and Fleischer (1985) [471]). In contrast, minerals such as monazite and apatite show a rapid recovery (Chaumont et al. (2002) [472]; Eyal and Olander (1990) [473]; Hendriks and Redfield (2005) [474]).

Kigoshi (1971) [475] found that ${}^{234}U/{}^{238}U$ ratios >3 cannot be explained by this preferential ${}^{234}U$ release alone, but require a combination with an additional fractionation mechanism based on direct alpha recoil ejection of ²³⁴Th from the solid into the aqueous phase (see also Hussain and Krishnaswami (1980) [476], and Rama and Moore (1984) [477]). At the transition from oxic to anoxic conditions, high groundwater ²³⁴U/²³⁸U ratios are produced due to recoil effects and preserved by the anoxic water. Thus, uranium is concentrated on secondary phases by precipitation. As a consequence, uranium concentrations strongly decrease and ²³⁴U/²³⁸U ratios increase due to recoil from these phases (Osmond and Cowart (1992) [438]). The recoil effect depends on the uranium concentration in the mineral, the grain size of the mineral, the recoil range of ²³⁴Th (about 20 nm) and the time (DePaolo et al. (2006) [478]; Kigoshi (1971) [475]). Provided the ²³⁴Th residence time in the aqueous phase is long enough compared with its half-life, ²³⁴U is produced directly within the aqueous phase by the decay of recoil ejected ²³⁴Th. If, however, ²³⁴Th is quickly adsorbed by mineral surfaces (Langmuir and Herman (1980) [479]), then ²³⁴U is produced at these surface sites from which it can easily enter the surrounding groundwater. Note that over long timescales (of the order of 100 ka) in slow moving groundwater and at low leaching (weathering) rates ($<10^{-6}/a$), direct recoil may overcompensate radioactive decay of ²³⁴U and, thus, cause an increase of ²³⁴U/²³⁸U along the groundwater flow (Andersen et al. (2009) [408]).

7.4. URANIUM ISOTOPE MEASUREMENTS

The uranium isotopes ²³⁸U and ²³⁴U are alpha emitters and thus, until recently, have been measured by alpha spectrometry combined with isotope dilution methods using ²³²U or ²³⁶U as analytical tracers (Lally (1992) [480]). This technique is still cost effective and well suited for applications where higher detection limits and lower precision and longer measuring (counting) times (several days per sample) are acceptable. Alpha spectrometry laboratories often simultaneously operate dozens of solid state alpha detectors and small vacuum chambers. In the late 1980s and early 1990s, mass spectrometry became an alternative to decay counting techniques (Chen et al. (1992) [481]). Although much more expensive, it facilitates more accurate measurements in a shorter time and with much smaller samples (Table 7.2).

For alpha spectrometry of uranium isotopes, at least 10 L of water is necessary. When using mass spectrometry, water samples of the order of 10 mL are sufficient for analysis. If water samples contain particulate matter, filtering (usually with 0.45 μ m membranes) is required. Adsorption of uranium onto the container walls or suspended matter can be avoided by adding, as soon as feasible during sampling, enough nitric acid to lower the pH of the water to approximately 1. (If other U–Th series nuclides are to be measured also, a more sophisticated sampling procedure is necessary, which, for example, is described by Tricca et al. (2001) [432]).

In the laboratory, a weighed amount of spike solution (usually with the shorter lived ²³²U for alpha spectrometry and the longer lived ²³³U or ²³⁶U for mass spectrometry) has to be added to the water sample. For alpha spectrometric analysis, the water volume must be reduced by evaporation or through co-precipitation of uranium with, for example, ferric hydroxide as carrier. The precipitate is re-dissolved

		Alpha spectrometry	Thermal ionization mass spectrometry	Multiple- collector thermal ionization mass spectrometry	Inductive coupled plasma mass spectrometry	Multiple-collector inductive coupled plasma mass spectrometry
Sample size (µg)	Uranium	1-100	0.1–2	0.01-1	0.01-0.45	0.01-0.45
Precision	²³⁸ U	2-10	0.1	0.1	0.1–5	<0.1
(2σ) (%)	²³⁴ U/ ²³⁸ U	2-10	0.5	0.1-0.2	0.1–10	0.05-0.2
Meas. time	Uranium	1–28 d	4 h	1–2 h	1–10 min	15–30 min

TABLE 7.2	. COMPARISON	OF ANALYTICAI	L METHODS FOR	R URANIUM IS	OTOPE ANALYS	SIS (Goldstein
and Stirling	(2003) [434])					

in an acid medium and then passed through an anion exchange column to isolate uranium from other nuclides that might cause interference during counting. Finally, the uranium is deposited on a suitable substrate (e.g. electrodeposition on polished stainless steel planchets) for alpha spectrometric analysis. More details of this laboratory procedure can be found in Lally (1992) [480]. For mass spectrometric measurements, the following procedure is used: addition of a spike (²³³U or ²³⁶U), drying, anion exchange and loading onto filaments for analysis.

Table 7.2 compiles parameters that allow comparison of the various methods currently available for the measurement of ²³⁴U and ²³⁸U in natural water samples (Goldstein and Stirling (2003) [434]). There are several suitable mass spectrometric methods which basically differ regarding the type of ion source, ionization method and ion collector system. The first mass spectrometric measurements of uranium and thorium isotopes were performed with thermal ionization mass spectrometers (TIMS) (Chen et al. (1986) [433]; Edwards et al. (1987) [482]; Goldstein et al. (1989) [483]). Sample size, measuring precision and time of analysis have improved at least one order of magnitude since that time. Since the 1990s, inductive coupled plasma mass spectrometry (ICPMS) has become more commonly used as an alternative to TIMS with comparable or even better precision. ICPMS facilitates a fast and easy acquisition of data. Analysis times are typically less than 10 min (Goldstein and Stirling (2003) [434]). Since the end of the 1990s, MC-ICPMS (multiple-collector-ICPMS) is increasingly being used. It facilitates an even better precision than conventional ICPMS. The cost per sample analysis is presently about US \$25.

7.5. URANIUM ISOTOPE DATING METHOD

7.5.1. Introduction

A straightforward dating of old groundwater by uranium isotope disequilibrium would be possible if: (i) the initial state of disequilibrium were known and (ii) the concentrations of both isotopes had not changed by chemical and physical processes other than radioactive decay. The initial state of disequilibrium can be estimated empirically by extrapolation of measured values along the groundwater flow direction. However, the second requirement is difficult to satisfy because of the various geochemical processes (including dissolution, precipitation, sorption/desorption) involved in the water–rock interaction that affect the evolution of uranium in groundwater. A range of attempts have been made by various authors to interpret uranium isotope measurements in terms of groundwater age. In the following, a model is described that allows a critical review of such approaches and helps better define potential and limitations of the groundwater dating using uranium isotope disequilibrium. The model is based on the approach published by Fröhlich et al. (1984) [421] and, in its present version, has been used by Ivanovich et al. (1991) [422] to evaluate the uranium isotope data of the Milk River aquifer. A similar model was used by Pearson et al. (1983) [425] for the numerical evaluation of ¹⁴C and uranium isotope data of the Carrizo aquifer. Furthermore, a detailed description of radionuclide transport models has been given by Ku et al. (1992) [484]. More recently, Porcelli and Swarzenski (2003) [404] reviewed the general principles and evaluated the controlling processes incorporated in the models.

7.5.2. Mathematical formulation of the model

The basic model (Fröhlich et al. (1984) [421]) describes the radionuclide evolution in a one dimensional groundwater flow of constant velocity. The following notation is used:

$N_{\rm m}, N_{\rm im}, N_{\rm a}$	number of radionuclide atoms in the mobile (m), immobile (im) and adsorbed (a) phase
N	total number of radionuclide atoms in the mobile immobile and adsorbed phase.
11	$N = N_{\rm m} + N_{\rm m} + N_{\rm r}$
N _r	number of radionuclide atoms in the solid (rock) phase
$V_{\rm m}, V_{\rm im}, V_{\rm r}$	volume of the mobile, immobile and rock phase
V	total (unit) volume: $V = V_m + V_{im} + V_r$
п	flow (effective) porosity: $n = V_m/V$
<i>n</i> _{im}	matrix porosity: $n_{\rm im} = V_{\rm im}/V$
n _t	total porosity: $n_{\rm t} = (V_{\rm m} + V_{\rm im})/V = n + n_{\rm im}$
<i>m</i> _r	mass of rock: $m_r = \rho \times V_r$
x	distance along flow path
t	time
$v_{ m f}$	Darcy velocity
ν	flow velocity: $v = v_f/n$
D	dispersion/diffusion coefficient
λ	radioactive decay constant
р	precipitation rate constant
e	dissolution (leaching) rate constant
γ	recoil efficiency
-1	subscript denoting the radioactive parent nuclide. Given the short half-life of ²³⁴ Th and
	its short lifetime in the liquid phase, the parent nuclide of 234 U is assumed to be 238 U
∂N	time derivative of the amount of the given radionuclide in the liquid and adsorbed
dt	phases of the unit volume
$D \frac{\partial^2 N_m}{\partial x^2}$	change of the dispersive/diffusive flux, assuming that D is constant
$v \frac{\partial N_m}{\partial x}$	change of the advective flux, assuming v is constant
$ \begin{split} \lambda N \\ \lambda_{-1} & N_{-1} \\ p(N_{\rm m} + N_{\rm im}) \\ e N_{\rm r} \\ \gamma \lambda_{-1} & N_{-1{\rm r}} \end{split} $	radioactive decay in liquid and adsorbed phase radioactive decay of parent nuclide in liquid and adsorbed phases irreversible precipitation from liquid to rock phase dissolution from rock phase recoil ejection from rock phase



FIG. 7.4. Schematic diagram of a unit volume (V) of an aquifer and of the processes controlling the temporal change of the radionuclide content in the liquid (mobile and immobile) phase (see text).

Figure 7.4 schematically represents a unit volume of the aquifer with the physicochemical processes controlling the radionuclide evolution. The processes considered in the model include dispersive/diffusive transport through and advective transport in the liquid phase, sorption/desorption and precipitation/dissolution across the solid–liquid interface, radioactive decay and ingrowth (due to radioactive decay of the precursor) in the liquid phase, and alpha recoil input. It is assumed that dissolution and precipitation of solids occur irreversibly and that sorption/desorption are reversible processes following a linear adsorption isotherm which is characterized by a constant equilibrium distribution coefficient (K_d). This K_d value is defined as the ratio of the specific activity of the given radionuclide in the adsorbed phase and the activity concentration of the radionuclide in the liquid phase:

$$K_{\rm d} = \frac{N_{\rm a}/m_{\rm r}}{N_{\rm m}/V_{\rm m}}$$
(7.1)

It should be noted that this approach is appropriate as long as the decay rate of the given radionuclide is considerably smaller than the rate constants of reversible sorption and desorption (Fröhlich et al. (1995) [485]). Alpha decay induced recoil ejection is assumed to be proportional to the activity of the parent nuclide in the rock matrix.

The liquid phase (groundwater) is divided into a mobile and an immobile component and, thus, the total porosity of the rock n_t is the sum of flow (effective) porosity n and matrix porosity $n_{im}/n_t = n + n_{im}$. It should be noted that in porous rock aquifers the matrix porosity is usually negligible $(n_{im} \ll n \text{ or } n_t \approx n)$, while in fractured rocks the effective (fracture) porosity is generally small in comparison with the matrix porosity $n \ll n_{im}$. It is further assumed that the given radionuclide is able to penetrate fully into the immobile groundwater, i.e. mobile and immobile groundwater are assumed to have the same radionuclide concentration:

$$\frac{N_{\rm m}}{V_{\rm m}} = \frac{N_{\rm im}}{V_{\rm im}} \tag{7.2}$$

The mathematical formulation of the model is based on the mass balance equation of the radionuclide in the unit volume of the aquifer (Fig. 7.4). The temporal change of the amount of

the radionuclide is given by the difference between the input and output of the radionuclide as well as by its production and decay. The mass balance includes both the liquid and adsorbed phases in the unit volume:

$$\frac{\partial N}{\partial t} = D \frac{\partial^2 N_{\rm m}}{\partial x^2} - v \frac{\partial N_{\rm m}}{\partial x} - \lambda N + \lambda_{-1} N_{-1} - p \left(N_{\rm m} + N_{\rm im} \right) + e N_{\rm r} + \gamma \lambda_{-1} N_{-1\rm r}$$
(7.3)

The various terms of Eq. (7.3) are schematically shown in Fig. 7.4 and are explained in the above notation. Considering that:

$$N = N_{\rm m} + N_{\rm im} + N_{\rm a}$$

taking into account Eqs (7.1, 7.2) and the definitions of the various porosities, it can be shown that:

$$N = R \times N_{\rm m}$$

where *R* is the retardation factor:

$$R = \frac{n_{\rm t}}{n} + \frac{1 - n_{\rm t}}{n} \rho K_{\rm d} \tag{7.4}$$

Similarly, it can be shown that $N_{\rm m} + N_{\rm im}$ of the precipitation term in Eq. (7.3) can be replaced by $\frac{n_{\rm t}}{n}N_{\rm m}$. Thus, with Eq. (7.3), it follows that:

$$R\frac{\partial N_{\rm m}}{\partial t} = D\frac{\partial^2 N_{\rm m}}{\partial x^2} - v\frac{\partial N_{\rm m}}{\partial x} - (R\lambda + \frac{n_t}{n}p)N_{\rm m} + R_{\rm -1}\lambda_{\rm -1}N_{\rm -1m} + eN_{\rm r} + \gamma\lambda_{\rm -1}N_{\rm -1r}$$
(7.5)

Finally, replacing the number of radionuclide atoms in Eq. (7.5) by the corresponding activity

concentration $a = \frac{\lambda N_{\rm m}}{V_{\rm m}}$, $a_{-1} = \frac{\lambda_{-1}N_{-1m}}{V_{\rm m}}$, $a_{\rm r} = \frac{\lambda N_{\rm r}}{V}$ and $a_{-1r} = \frac{\lambda_{-1}N_{-1r}}{V}$, and multiplying both sides by $\frac{V_{\rm m}}{\lambda}$ leads to:

$$R\frac{\partial a}{\partial t} = D\frac{\partial^2 a}{\partial x^2} - v\frac{\partial a}{\partial x} - \left(R\lambda + \frac{n_t}{n}p\right)a + R_{-1}\lambda a_{-1} + ea_r/n + \gamma\lambda a_{-1r}/n$$
(7.6)

This equation describes the evolution of any radionuclide of the natural decay series (Fröhlich et al. (1995) [485]). For the determination of ${}^{234}\text{U}/{}^{238}\text{U}$ disequilibrium, Eq. (7.6) represents a system of three partial differential equations that has to be solved for the three members of the decay sequence ${}^{238}\text{U} \rightarrow {}^{234}\text{Th} \rightarrow {}^{234}\text{U}$. The following simplifying assumptions allow a straightforward analytical solution of these equations. In aquifer systems with old groundwater, the radionuclide distributions are supposed to be in steady state ($\frac{\partial a}{\partial t} = 0$). Thus, the partial differential equations change to ordinary differential equations. The ${}^{234}\text{Th}$ activity concentration in groundwater is, in general, very low or even negligible, which reduces the system to two equations. Furthermore, it is assumed that the parameters characterizing the water–rock interaction (R, p, n_v , n) and the activity concentrations in the rock phase (a_r and a_{-1r}) are constant along the considered groundwater flow path. Consequently, the system of Eq. (7.6) reduces to two ordinary linear differential equations of second order with constant coefficients, for which the following solutions for the ${}^{238}\text{U}$ and ${}^{234}\text{U}$ activity concentrations can easily be obtained:

$$a_{8}(\tau) = a_{8s} + (a_{80} - a_{8s}) \exp(\kappa_{8}\tau)$$
(7.7)

$$a_4(\tau) = a_{4s} + (a_{40} - a_{4s}) \exp(\kappa_4 \tau)$$
(7.8)

TABLE 7.3. COMPILATION OF EARLIER ATTEMPTS TO DATE OLD GROUNDWATER USING URANIUMISOTOPES (from Fröhlich and Gellermann (1987) [426])

Authors	Study area; aquifer rock type	Dating formula(s)	Results	
Kronfeld (1971) [486], Kronfeld and Adams (1974) [424]	Hosston aquifer (Texas, USA); sandstone	$AR = AR_0 exp(-\lambda_4 \tau)^*$ (water rock interaction neglected)	Flow velocity 0.2–1.0 m/a derived	
Cowart and Osmond (1974) [419], Cowart and Osmond (1977) [487]	Carrizo aquifer (Texas, USA); sandstone	Carrizo aquifer $X = X_s + (X_0 - X_s) \exp(-\lambda_4 \tau)^{**}$ Texas, USA);(retardation, precipitation, leaching neglected)		
Pearson et al. (1983) [425]	Carrizo aquifer (Texas, USA); sandstone	Groundwater and radionuclide transport equation incorporating water rock exchange	¹⁴ C data (uncorrected) used to validate numerical solution of the transport equation; uranium retardation factor in reducing zone about 30	
Barr et al. (1979) [418]	Delaware Basin (New Mexico–Texas, USA); evaporite, limestone	$AR = AR_{s} + (AR_{0} - AR_{s})$ exp($-\lambda_{4}\tau$) (retardation, precipitation, leaching neglected)	$AR_s = 1$ assumed and AR_0 estimated; calculated ages between 0.3 and 1.1 Ma	
Eshova (1981) [420]	Bachardensky aquifer (Turkmenistan)	$AR = 1 + (AR_0 - 1)exp(-\lambda_4 \tau)$ (retardation, precipitation, leaching neglected)	Estimated groundwater age 60 ka	
Fritz et al. (1980) [488]	Strina test site	$AR = 1 + (AR_0 - 1)exp(-\lambda_4 \tau)$	Vertical age differences of 0.14 Ma estimated: model	
Andrews et al. (1982) [416]	(Sweden); granite	AR = 1 + (AR ₀ - 1)exp($-\lambda_4 \tau$) + β_A [1 - exp($-\lambda_4 \tau$)], where $\beta_A \approx a_{8r}/a_8$	assumptions not supported by chemical data	
Andrews and Kay (1983) [417], Andrews et al. (1984) [489]	East Midlands aquifer (United Kingdom); sandstone	AR = 1 + (AR ₀ - 1)exp($-\lambda_4 \tau$) + β_A [1 - exp($-\lambda_4 \tau$)], where $\beta_A \approx a_{8r}/a_8$	U isotopes are related to the hydrochemistry and difficult to relate to groundwater age	
Fröhlich et al. (1984) [421]	Triassic aquifer (Germany); sandstone	Groundwater and radionuclide transport equation incorporating water–rock exchange	Combined meaurements of ¹⁴ C and uranium isotopes; for reducing zone, the uranium retardation factor is between 30 and 80	
Ivanovich et al. (1991) [422]	Milk River sandstone aquifer, Canada	Groundwater and radionuclide transport equation incorporating water–rock exchange	²³⁴ U (²³⁸ U) age in good agreement with results obtained by hydraulic and ³⁶ Cl methods (see Table 7.4)	

The subscripts 8 and 4 indicate ²³⁸U and ²³⁴U, respectively, 0 and s indicate initial and stationary values, respectively, and τ is the groundwater age, or more precisely the time the groundwater parcel needs to travel along a distance *x* of the flow path:

$$\tau = x / v \tag{7.9}$$

The parameters included in Eqs (7.7, 7.8) are defined as follows:

$$\kappa_{i} = \frac{v^{2}}{2D} \left[1 - \left(1 + \frac{4DK_{i}}{v^{2}}\right)^{1/2} \right]$$
(7.10)

$$K_{\rm i} = R\lambda_{\rm i} + \left(\frac{n_{\rm t}}{n}\right)p \tag{7.11}$$

 $a_{8s} = e_8 a_{8r} / (nK_8) \tag{7.12}$

$$a_{4s} = (e_4 a_{4r} + \gamma \lambda_4 a_8 r) / (nK_4) \tag{7.13}$$

The dispersivity D/v in deep aquifer systems is assumed to be small, i.e. $D/v \ll v/4K_i$. Thus, expressing the square root in Eq. (7.10) by a Taylor series, the terms $\left(\frac{4DK_i}{v^2}\right)^v$ with v > 1 can be neglected, so that Eq. (7.10) reduces to:

$$\kappa_{\rm i} \approx -K_{\rm i} \tag{7.14}$$

A numerical example of the practical application of the above equations represents the evaluation of uranium isotope data of the Continental Intercalaire aquifer provided in Section 7.6.

Using Eqs (7.7, 7.8) (with the parameters defined by Eqs (7.9–7.14)), Fröhlich and Gellermann (1987) [426] reviewed earlier attempts of groundwater dating using uranium isotopes. They found that the dating equations used in most of these studies (Table 7.3) represent special cases of Eqs (7.7, 7.8) for which the uranium isotope exchange between water and rock were neglected. As can be seen in Table 7.3, the uranium isotope results are often expressed by the ${}^{234}U/{}^{238}U$ activity ratio (AR) and ${}^{234}U$ excess (X). With the notation used in Eqs (7.7, 7.8), it follows that:

$$AR = {}^{234}U/{}^{238}U = a_4/a_8$$

$$X = {}^{234}\text{U} - {}^{238}\text{U} = a_4 - a_8$$

It should be noted that, apart from analytical solutions of the radionuclide transport equation, numerical solution techniques have also been used (e.g. Pearson et al. (1983) [425]). Such numerical solutions have certain advantages over analytical solutions if spatial variations of the hydraulic and geochemical properties of the aquifer systems are significant. Moreover, in order to simulate real field problems, transport in two or even three dimensions must be evaluated; this can only be realized with numerical techniques.

7.5.3. Identification of model parameters

In the following, the properties (behaviour) and values of the geochemical parameters that are incorporated in the model, are discussed.

7.5.3.1. Generalized dating equation and dating range

Model Eqs (7.7–7.14) indicate that groundwater age can be derived from uranium isotope measurements provided that the parameters quantifying water–rock exchange processes are known for the given aquifer system. Combining Eqs (7.7, 7.8), it follows that:

$$\tau = \frac{1}{R\lambda_4} ln \left(\frac{a_8 - a_{8s}}{a_4 - a_{4s}} \times \frac{a_{40} - a_{4s}}{a_{80} - a_{8s}} \right)$$
(7.15)

This equation shows that groundwater dating with uranium isotopes requires knowledge (determination) of the uranium retardation factor and the initial and stationary activity concentrations of both isotopes. It should be noted that in deriving this relationship the precipitation rate has been eliminated, recognizing that precipitation is an element specific rather than isotope specific process. Figure 7.5 illustrates the dating range that can be covered under favourable conditions, in particular for those cases where the ²³⁸U activity concentration is found to be constant along the studied groundwater flow path (negligible precipitation).

For the sake of simplicity, Fig. 7.5 assumes that the stationary value of the ²³⁴U activity concentration is zero. Using the error propagation law, the relative error of the model age $\frac{d\tau}{\tau}$ has been calculated: re-arranging Eq. (7.8), replacing κ_4 by K_4 and neglecting p and a_s , it follows that:

$$\frac{d\tau}{\tau} = \frac{da_4 / a_{40}}{R\lambda_4 \tau} \sqrt{1 + \exp(2R\lambda_4 \tau)}$$

where da_4/a_{40} is the relative analytical error of the uranium isotope measurement.

Fig. 7.5 clearly shows that the dating range depends on the analytical accuracy and on the retardation factor. If the dating range is defined as the age range for which the relative error of the uranium isotope model age is lower than 25%, then Fig. 7.5 shows that for R = 1 the dating range is from about 50 to 1000 ka, while for R = 5 this range goes from about 10 to 200 ka. Therefore, Fig. 7.5 clearly demonstrates that the retardation factor is a key parameter that controls the dating range. If there



FIG. 7.5. Characterization of the uranium isotope dating range (see text). The red curves correspond to a retardarion factor of R = 1 and the blue curves R = 5. The curves have been calculated assuming a relative analytical error of the uranium isotope measurement da_4/a_{40} of 2% (lower red and blue curves) and 4% (upper red and blue curves), respectively.
is a retardation factor >1, the uranium isotope dating range may overlap the one of ¹⁴C dating and, in this way, fill the gap between the upper limit of ¹⁴C and the lower limit of ³⁶Cl and ⁸¹Kr dating. *7.5.3.2. Retardation factor*

First of all, it should be noted that the retardation factor R is relevant to all radiometric dating methods: conservative radionuclides (3H, 81Kr) can be subject to retardation in groundwater of fractured rocks because of the double porosity $(n_t/n \text{ in Eq. (7.4)})$; non-conservative radionulides (such as ¹⁴C, uranium and radium isotopes) are subject to sorption/desorption processes and, thus, to retardation in all rock types (Eq. (7.4)). Garnier (1985) [164] concluded from ¹⁴C field studies that "the interaction between ¹⁴C species (in the mobile and immobile phases) make ages obtained by ¹⁴C overestimated". The K_d value defining the effect of sorption processes on the radionuclide retardation (Eq. (7.4)) can be determined by laboratory experiments. However, deviations between laboratory and field results may occur due to differences between laboratory and field conditions. For example, Fjeld et al. (2001) [490] in laboratory experiments with aquifer rocks found a uranium retardation factor of 30. Porcelli and Swarzenski (2003) [404] noticed that this value was different from values derived from field study and attributed this difference to "difficulties of using laboratory data as an average for the larger scales of the aquifer or limitations of the mathematical model that was applied to the field data". Pearson et al. (1983) [425] estimated, from ¹⁴C and uranium isotope data of the Carrizo sandstone aquifer, a uranium retardation factor of 30. For a Permian-Triassic sandstone, Ivanovich et al. (1991) [422] found considerably higher values of $0.8-7 \times 10^3$. Given the variability of the retardation factor values, it is essential to determine this parameter for the groundwater formation of interest. In the following, examples of the determination of the retadation factor will be discussed; further practical aspects will be included under Section 7.6.

Constant ²³⁸U activity concentrations under reducing conditions suggest that leaching and precipitation are negligible and that any increase of ²³⁴U can be attributed to recoil ejection. A typical example is shown in Fig. 7.6, where at an almost constant ²³⁸U value along a flow path in the reducing part of a sandstone aquifer the ²³⁴U activity concentration increases remarkably with the ¹⁴C piston flow model age as suggested by Eq. (7.8). The ¹⁴C ages were determined without geochemical adjustment



FIG. 7.6. Activity concentration of $^{238}U(\bullet)$ and $^{234}U(\bullet)$ as a function of the ^{14}C model age in the reducing zone of a Triassic sandstone aquifer in Thuringia, Germany (from Fröhlich et al. (1984) [421]).

of the ¹⁴C initial concentration. Fitting the measured to the calculated data (Eq. (7.5)), K_4 has been determined: $K_4 = (1.1 - 2.4) \times 10^{-4}$ /a. Given that precipitation is negligible, from Eq. (7.11) it follows that the retardation factor is between about 40 and 80. This result is in rather good agreement with the one found by Pearson et al. (1983) [425] for the Carrizo sandstone aquifer, and it underlines that, under reducing conditions, the 'effective decay constant' K_4 can be about one order of magnitude higher than the radioactive decay constant, i.e. the 'effective life time' of ²³⁴U in the investigated groundwater can be accordingly shorter than the radioactive lifetime of 234 U of $1/\lambda_4 = 3.54 \times 10^5$ a.

7.5.3.3. Precipitation rate

Although the dating formula (Eq. (7.15)) does not explicitly include the precipitation rate, knowledge of this parameter is important. If its value is of the same order of magnitude or even higher than the radioactive decay rate of ²³⁴U, groundwater dating with uranium isotopes becomes a geochemical rather than a radiometric dating method (see Eq. (7.11)). An approach to determine the precipitation rate is demonstrated in Figs 7.7(a) and 7.7(b), where the relationship between ²³⁴U and ²³⁸U is shown; this has been calculated with Eqs (7.7, 7.8) for given ratios between stationary and initial concentrations of both uranium isotopes. It can be seen that with increasing removal rate r = $(n_t/n)p/R$, the curves come close to a straight line. Furthermore, a concave curve shape indicates an increase in uranium isotope concentrations along the flow path (Fig. 7.7(a)); when concentrations decrease, the shape is convex (Fig. 7.7(b)).

A practical example of the diagrams in Fig. 7.7 is provided by the ²³⁴U–²³⁸U diagrams in Fig. 7.8, where the uranium isotope data of the Hosston aquifer (Kronfeld (1971) [486]) are plotted together with trend lines calculated for different values of the parameter *r*. The data appear to fit trend lines with $r \ge 2\lambda_4$, i.e. precipitation may not be negligible in these aquifer sections. Overall, trend line analysis appears to be an important approach to constrain precipitation effects as well as initial and stationary uranium isotope concentration. Typical values of the parameter *r* derived from earlier uranium isotope



FIG. 7.7. Uranium isotope evolution along a flow path at given ratios between saturation and initial concentrations: $a_4/a_{40} = 20$; $a_{8s}/a_{80} = 10$ (a) and $a_{4s}/a_{40} = 0.4$; $a_{8s}/a_{80} = 0.1$ (b) (see text for a definition of r/λ_4).



FIG. 7.8. Uranium isotope evolution in the Hosston aquifer (Sections 1 and 2) and theoretical trend curves for selected values of the removal rate r. Full line: $r >> \lambda_4$; dot dashed line: $r = 2\lambda_4$; broken line: $r = \lambda_4$ (after Fröhlich and Gellermann (1987) [426]).

studies by this approach range from about 10⁻⁶ to 10⁻⁴ a⁻¹ (Fröhlich and Gellermann (1987) [426]). Thus, irreversible uranium precipitation cannot a priori be disregarded in uranium isotope groundwater dating.

7.5.3.4. Leaching and recoil ejection

Under oxidizing conditions, the recoil ejection of ²³⁴U appears to be negligible compared to leaching because of the very low ²³⁴U decay rate (Eq. (7.13)). Such conditions usually exist in the shallow unconfined part of an aquifer system in which the groundwater age is comparatively short, so that $K_4\tau \ll 1$ can be assumed. Thus, from Eqs (7.7, 7.8), it follows that the activity of ²³⁸U (²³⁴U) increases in proportion to groundwater age, where the proportional factor is the leaching terms e_8a_{8r}/n and e_4a4_{r}/n , respectively. In fact, combined ¹⁴C and uranium isotope measurements in the unconfined part of a Triassic sandstone aquifer in Thuringia, Germany, have shown a linear increase in the activity of both uranium isotopes with slopes $e_8a_{8r}/n = 0.1 \text{ mBq} \cdot \text{L}^{-1} \cdot \text{a}^{-1}$ and $e_4a_{4r}/n = 0.15 \text{ mBq} \cdot \text{L}^{-1} \cdot$ a^{-1} (Fröhlich et al. (1984) [421]). With typical values of $a_{8r}/n \approx a_{4r}/n$ for sandstone of this aquifer, the following values have been found: $e_8 \approx 0.2 \times 10^{-6}/\text{a}$ and $e_4 \approx 0.4 \times 10^{-6}/\text{a}$. The higher value for ²³⁴U is attributed to preferential leaching.

For the reducing part of this aquifer, the stationary value of ²³⁴U was estimated to be in the range of 30 to 50 mBq/L (Fig. 7.6), and for the 'effective decay rate' a value of $K_4 = (1.1-2.4) \times 10^{-4}/a$ was obtained (see also Section 7.5.3.2). Finally, with Eq. (7.13), it follows for the recoil ejection term that $\gamma \lambda_4 a_{\rm sr}/n \approx a_{\rm 4s} \times K_4 \approx (3-12) \times 10^{-3}$ mBq \cdot L⁻¹ \cdot a⁻¹. Thus, the recoil ejection rate for ²³⁴U appeared to be about one to two orders of magnitude lower than the leaching rate under oxidizing conditions.

7.5.3.5. Summary

The retardation effect is relevant to all radiometric dating methods. Retardation affects dating with conservative radionuclides (³H, ⁸¹Kr) in fractured rocks owing to double porosity (n_t/n in Eq. (7.4)) and affects non-conservative radionulides (¹⁴C, uranium and radium isotopes) in all aquifer rocks owing to reversible water–rock exchange.

Given the observed variability of the retardation factor, it is essential to determine the uranium retardation for each location of interest. Reliable values for the retardation factor of uranium should be derived from field (rather than laboratory) studies that include the use of other dating tools, for



FIG. 7.9. The study area in southern Texas. The Carrizo sandstone dips gently towards the south–southeast. A-A' is the line of the cross-section of Fig. 7.10. The projections of sample points onto this line are made parallel to the strike of the formation. An underlined sample number, such as 410, indicates that no uranium data are available for that location (from Cowart and Osmond (1974) [419]).

example, ¹⁴C dating of the upstream section of the aquifer flow, where the relatively young groundwater is amenable to ¹⁴C dating.

Analysis of uranium isotope trend lines can help constrain values of the precipitation rate. Using data from earlier uranium isotope dating attempts, it has been shown that the precipitation rate, p, can be remarkably higher than the 'apparent decay rate', $R\lambda_4$; i.e. under such conditions, uranium isotope dating would be a geochemical rather than a radiometric dating method (see Figs 7.7 and 7.8). More generally, it can be concluded that the study of trend lines (²³⁴U as a function of ²³⁸U or the ²³⁴U/²³⁸U ratio as a function of 1/²³⁸U (e.g. Osmond and Cowart (2000) [439])) are a prerequisite for any attempt to derive values of the groundwater age from uranium isotope measurements.

Oxidizing zones typically contain relatively young groundwater with ages below the dating range of uranium isotopes. However, measurements of uranium isotopes together with suitable dating tools, such as ¹⁴C, may be used to determine the leaching rates under field conditions, which may be relevant for other applications of uranium isotopes, in particular as natural analogues in connection with nuclear

waste disposal (IAEA (1989) [491]). Typical values of the leaching rate found for ²³⁸U and ²³⁴U are at about $0.2 \times 10^{-6}/a$ and $0.4 \times 10^{-6}/a$, respectively.

Under reducing conditions, a steady increase of ²³⁴U activity concentration at constant ²³⁸U activity concentration can be attributed to the effect of recoil ejection. Characteristic activities have been found to range from $3-12 \times 10^{-3}$ mBq \cdot L⁻¹ \cdot a⁻¹ (IAEA (1989) [491]), which is about one to two orders of magnitude lower than the leaching rate under oxidizing conditions.

7.6. CASE STUDIES

There are numerous studies on the use of the uranium isotope disequilibrium to date old groundwater. Early attempts are summarized in Table 7.3. Here, the uranium isotope dating results of the Carizzo aquifer, USA are discussed and evaluation is made of recently published uranium isotope data of the Continentale Intercalaire aquifer, in the north-western Sahara. The discussion is aimed at demonstrating the potential and limitations of uranium isotope dating in practical applications. The uranium isotope studies of groundwater from the Milk River aquifer, Canada, are discussed in Chapter 11.

7.6.1. Carrizo sandstone aquifer, South Texas, USA

One of the earliest uranium isotope studies of old groundwater was related to the Carrizo sandstone aquifer, South Texas, USA (Cowart and Osmond (1974) [419]). The Carrizo formation is Eocene coastal plain sandstone which crops out nearly parallel to the coast and dips towards the Gulf of Mexico (Fig. 7.9). The Carrizo is a well confined aquifer with little leakage in or out of the sand; it was hydrogeologically and hydraulically well studied and had many observation wells for sampling.



FIG. 7.10. Cross-section along A-A' of Fig. 7.7, showing the sample well locations relative to the dipping Carrizo aquifer (upper). The ²³⁴U/²³⁸U activity ratios (linear scale on left) and the U concentration values (logarithmic scale on right) as a function of corresponding well positions (lower) (from Cowart and Osmond (1974) [419]).

Moreover, earlier ¹⁴C data were used to determine flow velocity and age of the groundwater (Pearson and White (1967) [492]).

The water of the Carrizo is of meteoric origin and infiltrates in the outcrop area under oxidizing conditions. The aquifer consists mainly of quartz sand with a thickness varying from about 180 m near the outcrop to ca. 400 m at a distance downdip of some 90 km (Fig. 7.10, upper part). In the outcrop region, relatively high uranium concentrations associated with low ²³⁴U/²³⁸U ratios were found (Fig. 7.10, lower part), which is characteristic for oxidizing conditions. Somewhat downdip, a sharp decrease in the uranium concentration indicated a change to reducing conditions with strong uranium precipitation. Radioactive decay of the precipitated uranium at the grain surfaces associated with recoil ejection of the daughter nuclide ²³⁴Th were suggested to be the cause of increasing ²³⁴U excess and, thus, high activity ratios. The activity ratio reached a maximum of nine at about 33 km, and further downdip it decreased, while low ²³⁸U values remained comparatively constant. The boundary between low and high activity ratios was rather well defined.

Cowart and Osmond (1974) [419] ascribed this decrease in the activity ratio to radioactive decay of 234 U excess *X* according to the relationship:

$$X_{\rm P} = X_{\rm S} + (X_0 - X_{\rm S})\exp(-\lambda_4 \tau)$$
(7.16)

where

 $X_{\rm P}$ is the observed ²³⁴U excess at any point;

 X_S is the steady state (stationary) excess;

 X_0 is the initial excess;

 τ is the time elapsed between the initial condition (X_0) and the time of measurement (X_P);

 λ_4 is the radioactive decay rate of ²³⁴U.

Replacing time, τ , by the distance, x, down the flow direction $\tau = x/v$, v = flow velocity, Eq. (7.16) corresponds to a straight line in a semi-logarithmic plot of $(X_P - X_S)$ versus x, where the slope of the line is shown by λ_4/v . Figure 7.11 shows the plot of the measured data and the best fit line in



FIG. 7.11. Plot of ²³⁴U excess as a function of distance down the flow direction and in the direction of increasing water age. The dash dotted line has been drawn assuming a velocity of 150 cm/a and a radioactive decay of ²³⁴U excess from an initial value of 0.020 ppb (²³⁸U equivalents). The broken line is the best fit to the data points and corresponds to an 'apparent flow velocity' of about 8 cm/a (from Cowart and Osmond (1974) [419]).



FIG. 7.12. Measured and simulated ¹⁴C contents with distance down gradient from outcrop (from Pearson et al. (1983) [425]).

a semi-logarithmic diagram. The slope of this line corresponds to an apparent flow velocity (also called 'uranium migration velocity') of less than 8 cm/a. However, hydrological estimates (Alexander and White (1966) [493]) and ¹⁴C dating (Pearson and White (1967) [492]) indicated a value of at least 150 cm/a, which is about 20 times higher.

Pearson et al. (1983) [425] followed up the evaluation of these ¹⁴C and uranium isotope data, using a groundwater flow and radionuclide transport model that incorporates water–rock exchange similar to Eq. (7.6). The solute transport equation (conservation of mass for one dimensional groundwater flow) was solved by a numerical technique, validated using the ¹⁴C data (Fig. 7.12) and then applied to simulate ²³⁴U and ²³⁸U movement in the reducing part of the Carrizo. Calculating the ²³⁴U/²³⁸U ratio for several K_d values and comparing the simulated with the measured ratios, the authors were able to determine the best fit K_d value and, thus, the uranium retardation in the system.

Figure 7.13 demonstrates that uranium transport in the reducing zone down gradient of about 33 km in the Carrizo is best simulated using a K_d of 6.0. From Eq. (7.4), it follows with $n_t \approx n = 0.35$ and $\rho_r = 2.6$ g/cm³ (Pearson et al. (1983) [425]) that the retardation factor is 30, or that the uranium migration velocity in the Carrizo is only 1/30th of the flow velocity of groundwater movement. This result explains the disparity in the flow velocities of water and uranium found by Cowart and Osmond (1974) [419]. Their model (Eq. (7.16)) did not account for the reversible sorption of uranium in the Carrizo aquifer. However, it is interesting to note that the ratio between groundwater flow velocity derived from hydrological estimates and ¹⁴C determinations, and the velocity derived from the decrease of ²³⁴U excess was of the same order as the retardation factor obtained by Pearson et al. (1983) [425].

Overall, the Carrizo case study clearly demonstrates that, in sandstone aquifers, exchange between dissolved and adsorbed uranium may occur that retards the velocity of uranium movement relative to that of the water itself. Therefore, determination of the retardation factor through combined ¹⁴C and uranium isotope measurements in the upstream part of an aquifer (younger groundwater) can facilitate



FIG. 7.13. Measured and simulated uranium activity ratios with distance down gradient from outcrop (from Pearson et al. (1983) [425]).

the use of uranium isotope dating downstream where the age of the groundwater is beyond the ${}^{14}C$ dating range.

7.6.2. Continental Intercalaire aquifer, north-west Sahara

The Continental Intercalaire is one of the largest confined aquifer systems in the world. It is located in the north-western part of the Sahara and covers an area of some 600 000 km². It occupies the continental formations of the Lower Cretaceous (Neocomian, Barremian, Aptian, Albian) and extends from the Saharan Atlas in the north to the Tassili mountains of the Hoggar in the south, and from western Algeria in the west to the Libyan desert in the east (Fig. 7.14). The depth of the aquifer roof is approximately 1000 m below the surface in the lower Sahara in the south and reaches 2000 m in the north in the region of the saline lakes of Chott Melrhir (Algeria) and Chott Djerid (Tunisia). There are three groundwater flow paths which all converge towards a single discharge zone in Tunisia (Chott Djérid/Chott Fejej region and Gulf of Gabès). The main flow path comes from the Saharan Atlas and reaches up to the Chott Djérid and the Gulf of Gabès in Tunisia (see lower part of Fig. 7.14).

The groundwater of the Continental Intercalaire aquifer system was subject to various isotopic investigations over the past 50 years (Edmunds et al. (2003) [494]; Edmunds et al. (1997) [495]; Gonfiantini et al. (1974) [496]; UNESCO (1972) [497]). Using radiocarbon as a dating tool, it was found that, except near outcrops, the radiocarbon ages are at or below the dating limit. First attempts to date the old Continental Intercalaire groundwater by ³⁶Cl were published by Michelot et al. (1989) [498], followed in 1994 by additional sampling for ³⁶Cl. Guendouz and Michelot (2006) [499] published all of their data and their evaluation in terms of groundwater age; values of up to 1 Ma were obtained. The first uranium isotope measurements of Continental Intercalaire groundwater were carried out by Chkir et al. (2009) [500] to study the variability of these isotopes in the aquifer system.



FIG. 7.14. The Lower Cretaceous outcrops forming the Continental Intercalaire aquifer system and its piezometric surface leading to discharge in the area of the Chotts of Tunisia. The lower part shows the sites chosen by Edmunds et al. (2003)[494] for sampling along the cross-section from the Saharan Atlas (Algeria) to the Tunisian Chotts (main flow path) (from Edmunds et al. (2003) [494]).



FIG. 7.15. Distribution of ${}^{238}U$ and ${}^{234}U$ (a), and of ${}^{14}C$ and ${}^{36}Cl$ (b) along the main flow path of the Continental Intercalaire from its outcrop to its discharge area (about $2^{\circ}E$ to $10^{\circ}E$). It should be noted that in the given latitude region, a longitude difference of 1° corresponds to a distance of about 90 km.



FIG. 7.16. Exponential regression lines fitting the uranium isotope and ³⁶Cl data of the selected section along the main flow part: (a) ²³⁴U concentration and ²³⁴U excess concentration, (b) ³⁶Cl concentration and ³⁶Cl** concentration corrected for in situ production equivalent to a stationary ³⁶Cl/Cl ratio of 5×10^{-15} . It should be noted that x^* is the longitude (in °E) along the flow path. For the sake of simplicity, the curvature of the flow path (Fig. 7.14, lower part) has been ignored. Thus, a longitude difference of 1° is approximately equivalent to a flow path distance of 93 km.

In the following, the uranium isotope composition of groundwater from the Continental Intercalaire is examined to determine groundwater age. To this end, data available for the main flow path (region extending from 2°E to 10°E and 32°N to 34°N; see Fig. 7.14) were selected. The ¹⁴C and ³⁶Cl data of this region (Edmunds et al. (2003) [494]; Guendouz and Michelot (2006) [499]) are also examined in terms of groundwater age.

Figure 7.15(a) shows that the uranium concentration remains nearly constant from about 2.5°E to about 4.5°E from where it rapidly decreases to about 0 ppb. This abrupt decrease matches the sudden increase in the Fe concentration (Edmunds et al. (2003) [494]) which indicates that the groundwater becomes reducing. Therefore, the decrease of ²³⁴U at nearly constant ²³⁸U can be attributed to radioactive decay of ²³⁴U. Except near outcrop, where ¹⁴C indicates Holocene groundwater, ¹⁴C is virtually absent (Fig. 7.15(b)) and, thus, the groundwater age is beyond the ¹⁴C dating range. It should, however, be

TABLE 7.4. COMPILATION OF THE DATING RESULTS ESTIMATED ON THE BASIS OF URANIUM ISOTOPE AND ³⁶Cl MEASUREMENTS OF GROUNDWATER OF THE CONTINENTAL INTERCALAIRE

Dating method	<i>v/R</i> (m/a)	<i>v</i> (m/a)	age ^a (Ma)
²³⁴ U	0.53		0.94
²³⁴ U excess	0.39		1.3
³⁶ Cl		0.39	1.3
³⁶ Cl ^{**} (in situ production)		0.28	1.8

^a At a distance of 500 km from the outcrop.

noted that downstream of about 8°E the ¹⁴C values increase above the detection limit. This behaviour, also replicated by the uranium isotope concentrations, can be associated with the convergence of all Continental Intercalaire groundwater flowlines near the Tunisian Chotts between about 8°E and 9°E (Edmunds et al. (2003) [494]). In particular, the higher ¹⁴C values point to a second recharge area located in the Dahar uplands in southern Tunisia (Edmunds et al. (1997) [495]). Therefore, only uranium isotope and ³⁶Cl data from about 3°E to 7°E along the main flow path appear to be suitable for estimating the groundwater flow velocity (age).

Since uranium and ²³⁴U stationary values approach zero (Fig. 7.15(a), from about 5.5°E to 7.5°E), a simple exponential decrease can be assumed for ²³⁴U as well as ²³⁴U excess which, according to Eqs (7.7–7.14), should be proportional to $\exp(-R\lambda_4\tau)$, where $\tau = x/v$. In fact, Fig. 7.16(a) suggests that the data fit an exponential function reasonably well. Similarly, ³⁶Cl values can be fitted to an exponential function $\exp(-\lambda_{36}\tau)$. Apart from the directly measured ³⁶Cl values, the evaluation also includes ³⁶Cl values corrected for in situ production (³⁶Cl^{**}, Fig. 7.16(b)). A 'reasonable' value for the situ production was assumed that corresponded to a stationary ³⁶Cl/Cl ratio of 5 × 10⁻¹⁵. From the coefficients of the exponential functions given in Figs 7.16(a) and 7.16(b) and the decay constants of ²³⁴U and ³⁶Cl, groundwater flow velocity was estimated. The results compiled in Table 7.4 show that the flow velocity estimated by ³⁶Cl is lower than the one derived from ²³⁴U and ²³⁴U excess. Thus, the uranium retardation appears to be negligible (*R* = 1). Given the uncertainties inherent in the approach, it can be concluded that the estimated flow velocity and ages which are close to the ones derived from ³⁶Cl.

7.7. SUMMARY

Old groundwater typically occurs under reducing conditions in deep aquifer formations where, in addition to radioactive decay, processes of reversible sorption (retardation factor), irreversible precipitation (precipitation rate) and recoil ejection may affect the evolution of uranium isotopes. So far, attempts to date old groundwater using uranium isotopes have only been of limited success, mainly because of the inappropriate modelling that did not match the geochemical conditions in the studied aquifers. This chapter has provided evidence that any dating model must take full recognition of water–rock interaction processes controlling the behaviour of the uranium isotopes in groundwater.

Favourable conditions for groundwater dating exist where uranium (²³⁸U) concentration along a given section of the groundwater flow is constant (but \neq 0), so that irreversible precipitation of uranium can be assumed to be negligible. In these cases, the only remaining unknowns are retardation factor and the stationary value of ²³⁴U. The latter parameter can be determined by extrapolation of the ²³⁴U trend ('evolutionary trend') along the flow path. The retardation factor can be determined by combining uranium isotope dating with an independent dating method, for example, ¹⁴C dating of groundwater in the upstream region of the flow path (as in the case of the Carizzo aquifer) or ³⁶Cl dating (as in the case of the Continental Intercalaire aquifer). In this context, it should also be noted that determination of uranium isotope geochemical parameters such as precipitation rate and retardation factor are highly relevant for the use of uranium isotopes as natural analogues in assessment of nuclear waste disposals (IAEA (1989) [491]).

The discussion of the Carrizo case study has shown that in sandstone aquifers exchange between dissolved and adsorbed uranium may occur, retarding the movement of uranium relative to the water. This retardation causes a faster decrease of 234 U (see Eq. (7.11)) than expected from pure radioactive decay of 234 U and, thus, results in an accordingly older 234 U based age' than the age of the groundwater itself. Assuming that in the upstream part of the aquifer, which is amenable to 14 C dating, the flow velocity derived from 14 C data represents groundwater velocity, the retardation factor (ratio of groundwater velocity and uranium migration velocity) can be determined. In the case of the Carrizo aquifer, the estimated value was about 30 and, thus, considerably higher than that derived from the Continental Intercalaire aquifer where uranium retardation was found to be negligible (retardation factor = 1). For this aquifer, flow velocities derived from 36 Cl data and the one determined by uranium isotope data show fairly good agreement (Table 7.4).

Although the interpretation of uranium isotope data in terms of groundwater age is not an easy task, this method shows potential for playing an important role within the concerted application of techniques to date old groundwater. Depending on the geochemistry of the aquifer system, the potential dating range extends from about 10 ka up to 1 Ma, which overlaps the ¹⁴C and the ³⁶Cl/⁸¹Kr dating range. Uranium isotopes can provide independent information relevant to groundwater age that complements other dating approaches and may help to resolve ambiguities in data interpretation. Moreover, uranium isotopes in groundwater have the potential to quantify geochemical parameters of the water–rock interaction and represent natural analogues for radioactive waste. Any multitracer application to date old groundwater should integrate uranium isotope measurements which can easily be afforded by the use of modern mass spectrometric techniques.

Chapter 8

HELIUM (AND OTHER NOBLE GASES) AS A TOOL FOR UNDERSTANDING LONG TIMESCALE GROUNDWATER TRANSPORT

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8.1. INTRODUCTION

Helium-4 is the alpha decay product from the radioactive decay of U–Th series elements that occur naturally in the Earth. As both U and Th have long half-lives in comparison to typically anticipated groundwater ages, the accumulation of ⁴He along a groundwater flow path has long been explored and evaluated as a groundwater dating tool. A simple age, Δt , can be defined in the following way:

$$\Delta t = \frac{\Delta C}{\left[\sum I\right]} \tag{8.1}$$

where

 ΔC is the change in concentration of ⁴He with respect to an initial condition;

 ΣI is the sum of ⁴He inputs the groundwater parcel.

 Δt is usually called the ⁴He model age, which using certain assumptions under favourable conditions can be interpreted with respect to an idealized water age. It should then be possible to estimate, for example, flow velocities, provided there is some additional evidence that the suite of ⁴He samples is along a flowline. However, because ⁴He diffusion coefficients are higher than that of water, and because groundwater is an open system with regard to both locally produced ⁴He (which can accumulate or be lost) supplied on the grain scale as well as externally imposed sources and sinks for ⁴He which can exert influences on the kilometre scale, the methodology becomes considerably more complex. This paper presents the ⁴He methodology as a geochemical construct and then illustrates how such information can be interpreted and applied to problems of basin scale groundwater flow. The goal is to enable a valuable groundwater tracer (⁴He and other noble gases) to be understood from a practical standpoint and interpreted in a realistic environment.

8.2. THE GEOCHEMICAL CONSTRUCT FOR APPARENT ⁴He TRACER AGES

Helium-4 is present in the atmosphere at levels of 5.24 ppm and is sparingly soluble in water (Ozima and Podosek (2002) [251]). As water accumulates near the water table, it equilibrates with soil gas (idealized as air) and acquires an initial concentration of ⁴He. When the vertical recharge

velocity of the groundwater isolates the water parcel from the atmosphere (e.g. the recharge velocity moves the water parcel away from the groundwater table faster than diffusion-like exchange can re-equilibrate the water parcel with the soil gas; Peclet number $(v\Delta x/D > 1)$), the water is initialized to a concentration of ⁴He controlled by the partial pressure of He at the water table, temperature, salinity and the dissolution of soil air bubbles due to water table fluctuations ('excess air'). For systems such as ³⁶Cl, the assumption is that the water parcel then acts as a closed system and loses ³⁶Cl through radioactive decay without mixing with other water parcels. The comparable assumption for ⁴He would be that radioactive decay of dissolved U-Th series elements produces alpha particles (4He++) which then accumulate in the water parcel. However, for most systems, the contribution from dissolved phase U-Th series alpha decay is insignificant and the idealized geochemical construct must be altered to allow ⁴He sources from the solid phase (which changes as a function of time/space as determined by the groundwater flow velocity). The simplifying assumptions are that the solid phase composition and its porosity are homogeneous along the flow path. However, given this is an open system, ⁴He sources from outside the moving water parcel and outside the sample collection space $(\Delta x \Delta y \Delta z)$ can contribute to the accumulation of ⁴He within the water parcel. Thus, the calculation of a ⁴He model age for the water parcel is dependent upon specific knowledge of an open system for which the source and sink terms for ⁴He are known. Inadequate knowledge of the open system sources and sinks (potentially heterogeneous in time and space) will limit the interpretability or applicability of the ⁴He model age in addition to the conditions discussed above. Thus, the calculation of an appropriate ⁴He model age in a groundwater parcel is dependent upon the definition of a known initial condition, including:

- (a) Initial solubility equilibrium;
- (b) Excess air incorporated during the water table initialization process;
- (c) Possible gas loss (by, for example, bubble ebullition in situ);
- (d) Specific knowledge of the local, grain scale source strengths for ⁴He in the solid phase (which is changing as the water parcel moves) and how such sources vary in time and space with:
 - The volume of solid phase associated with the water parcel (as determined by the porosity, $\Phi = f(x,y,z,t)$);
 - Direct release of alpha particles from the solid phase (which may vary in space and time) to the fluid phase;
 - Diffusive release of solid phase, accumulated ⁴He and its variability over time/space;
 - Weathering release of solid phase, accumulated ⁴He and its variability over time/space by the dissolution of the solid phase during chemical reaction (a function of x,y,z,t);
 - Mechanically or thermally induced fracturing and subsequent diffusion of solid phase, accumulated ⁴He to the pore space (this term is applicable on both the microscale and the macroscale);
 - Specific knowledge of the external sources (and loss terms) for ⁴He to the pore space groundwater and how such external sources (and loss terms) vary with time/space including:
 - Fluxes across local aquifer/aquitard boundaries (sources and losses);
 - Sources from fluxes that permeate the crust and degas to the atmosphere;
 - Magma based sources as evidenced by excess ³He attributable to mantle sources and the ⁴He that accompanies such a source;
 - Tectonically controlled ⁴He fluxes and their variability that induce ⁴He fluxes as a result of extension, intrusion, volcanism and basin deformation.

The above forms a conceptual outline for the following discussion. As a part of the discussion, it will become apparent that calculation of a ⁴He model age requires measures of gases in addition to ⁴He (e.g. Ne, ³⁶Ar, Kr, Xe, N₂), some of which can also be used to provide temporal constraints with differing sensitivities to sources, sinks and variability (e.g. ⁴⁰Ar, fissionogenic ¹³⁶Xe, ⁸⁴Kr and nucleogenic (α , n)²¹Ne and (n, α)³He). Details about these other gases are provided elsewhere (Matsuda (1994) [501]; Ozima and Podosek (2002) [251]; Porcelli et al. (2002) [502]) and only those details especially pertinent to the discussion of ⁴He will be addressed. Information is also included on sampling

techniques, instrumentation and mass spectrometric constraints to enable intelligent negotiation when seeking collaborative ⁴He analyses.

8.3. SAMPLING AND ANALYSIS

8.3.1. Sampling methods

Sampling groundwater for ⁴He requires collection of in situ water that is (i) not subject to gas loss by the sampling process and (ii) not subject to air contamination during the sampling process. Additionally, ⁴He diffuses through typical glass/plastic containers with/without special caps on a timescale (hours to weeks) that is typically incompatible with shipping samples to the laboratory and mass spectrometer analysis schedules. Helium-4 also diffuses through borosilicate glass on a timescale of hours to weeks even when closed by flame sealing (Suckow et al. (1990) [503]). Consequently, the traditional method for collecting ⁴He samples has been in ~1 cm outer diameter crimped copper tubes (Weiss (1968) [504]). Soft refrigeration-type (dehydrated) copper tubing is used to avoid contamination by tritiogenic ³He and loss of gas (the crimping device creates a cold weld as opposing walls of the copper tube are pressed together). Such sampling devices are also suitable for other (non-reactive) gases although the volumes required for some gases may be larger, so multiple samples would need to be collected. In such cases, it is necessary to ensure that samples represent 'duplicates' of the groundwater and at least one gas should be measured in both sampling devices. Even for the case of He, Ne-only, replicate copper tube samples are often taken to evaluate the sampling procedure and the suitability of the well/borehole preparation.

The most common sampling approach for wells is to use a submersible pump connected via pressure tight tubing to a tee. One branch leads to an outflow that can be regulated and acts as a bypass. The other branch is connected to the copper tube with a clear piece of tubing and a needle valve on the other end. By adjusting the pump rate and the flow rates in the two outflows, it is usually possible to set the pressure in the copper tube to a level larger than the sum of the partial pressures of all dissolved gases to avoid degassing. The clear tube can be monitored for signs of bubbles, indicating leaks or degassing (for details, see, for example, http://water.usgs.gov/lab/3h3he/sampling/). Many old groundwaters are free of dissolved oxygen and a simple O₂ measurement with a chemical kit or an O₂ sensor can place an upper limit on contamination with atmospheric air during sampling. For wells with short screens, several bore volumes should be pumped out before a sample is collected. Wells with long screens should be packed-off at appropriate intervals to avoid cross-flow self-contamination (wellbore induced mixing). Alternatives to submersible pumps include borehole fluid samplers that can be used to retrieve water at depth (e.g. Kuster sampler (Solbau et al. (1986) [505])). If wells tap into artesian aquifers, flow at the surface is often sufficient to ensure a good sample but depressurization as water flows up the well may induce bubble formation which can strip gases from the fluid. As wellhead conditions are often not known before sampling and return visits are often not possible, backup sampling systems and variations on the sampling procedure are common, and creativity in the field is required.

Copper tube sampling has been shown to be robust and samples can be shipped with minimal concern and stored for considerable time prior to analysis. The most common shipping problem is loss of the crimped/exposed end of the copper tube which may lead to crimp failure and leakage of ⁴He or may create sample processing issues if one or both ends are lost (connection to vacuum processing line becomes difficult). As only the gas within the water parcel needs to be collected, some investigators have relied on gas only sampling in the field. Sanford et al. (1996) [506] describe a vacuum extraction technique. Sheldon (2002) [507] and Loose et al. (2009) [508] summarize techniques in which the dissolved gases are equilibrated with a sample host across a gas permeable membrane. After equilibrium is achieved, the sampler is removed and the equilibrium headspace in the sampler can be analysed. Sanford et al. (1996) [506] describe the use of a semi-permeable silicon tubing to sample for dissolved gases. Dyck and Silva (1981) [509], and Gascoyne and Sheppard (1993) [510] used pingpong balls to collect gases for ⁴He analysis (but these cannot be stored for long periods and require

measurement in the field). Spalding and Watson (2006) [511] used silicon tubing attached to a syringe for sampling and direct injection of samples analysed for H_2 , O_2 and CO_2 . Gardner and Solomon (2009) [512] recently described a passive headspace diffusion sampler that maintains the total dissolved gas pressure. In cases where wells are not available or the specific yield of the formation is too small, rock samples have been collected and stored in evacuated stainless steel vessels. Over time (often weeks to months), gases dissolved in the pore fluids accumulate in the headspace and can subsequently be extracted for measurement (Ali et al. (2010) [513]; Osenbrück (1996) [514]; Osenbrück et al. (1998) [515]).

8.3.2. Laboratory processing methods

Typical extraction procedures for the laboratory involve attaching the free end of the crimped copper tube to the processing line, opening the crimp or container into an evacuated processing system, degassing of the water under vacuum (or vacuum boiling) and isolation of the extracted gases on the downstream side of a fine capillary (Rudolph (1981) [516]; Torgersen (1977) [517]). The capillary allows a large flow rate of water vapour so that gases of interest cannot effectively back-diffuse against the large scale advection of water vapour. The isolated gases are then cleaned of water vapour and unwanted gases (CH₄, CO₂, O₂, etc.) with a series of traps that may retain gases (e.g. water vapour), adsorb gases or react gases to absorbable species (e.g. Smith and Kennedy (1983) [518]; Smith and Kennedy (1985) [519]). Gases are then quantitatively transferred into a sample container or directly into the mass spectrometer, originally by a toepler pump (Torgersen (1977) [517]), but now most commonly with a set of one or two cryogenically cooled traps used to accumulate the gases and separate the He/Ne fraction from the other gases. Reactive gases are removed using titanium (heated sponge or filament), Cu/CuO or alloy (ST101 or 707) getter pumps, either right after extraction and removal of water vapour; or after desorption from the cryogenic traps. Sample aliquots can be stored for analysis at a later time in all metal containers; or in flame sealed borosilicate (Ne, Ar, Kr, Xe), Corning 1720 or Pb (He) glass ampoules. The diffusion coefficients of He in these specific glasses are sufficiently low that samples can be stored for years at temperatures typically $< 0^{\circ}$ C (depending on gas and glass type (Suckow et al. (1990) [503])). In recent years, more and more analysis systems have been automated, at least from the water sample extraction step onwards, which has improved the reproducibility of the measurements and the sample throughput.

8.3.3. Mass spectrometry

Helium-4 and noble gases are measured mass spectrometrically and require specialized machines with defined resolution. For helium, measurement of ⁴He and ³He are often necessary (identification of mantle sources and tritiogenic ³He). Clear measurement of ³He requires separation of the HD⁺ peak from the ³He⁺ peak and, thus, machine resolution of over 630 is required. If only measures of ⁴He are required, much simpler mass spectrometers can be employed and very high concentrations can be measured with gas chromatography. However, unless the field site and the problem are well determined, ⁴He 'dating' in the research mode usually requires the use of a well equipped and specialized noble gas mass spectrometer which can produce (at a minimum) ³He, ⁴He, Ne, ³⁶Ar, ⁴⁰Ar, Kr and Xe measures. Measures of the complete noble gas suite aid in the definition of the initial condition and the recharge temperature. The better laboratories can additionally provide measures of ^{20,21,22}Ne (to potentially support ⁴He model age times with nucleogenic Ne model ages); and Ar, Kr and Xe isotopes (to potentially support ⁴He model ages isotopic measures is also important in the identification of mass dependent fractionation as an analytical problem. For analytical detail, the reader is referred to Bayer et al. (1989) [241], Beyerle et al. (2000) [276], Clarke et al. (1976) [242], Ludin et al. (1998) [520], Mamyrin and

Tolstikhin (1984) [521], Rudolph (1981) [516], Smith and Kennedy (1983) [518], Smith and Kennedy (1985) [519], Stute (1989) [522] and Torgersen (1977) [517].

8.4. IDENTIFYING MULTIPLE ⁴He COMPONENTS FROM MEASUREMENTS

The total ⁴He in a measured sample is a composite of ⁴He from multiple sources as well as sampling induced ⁴He additions and losses (e.g. degassing in situ or during sampling). These components can be generally expressed for any noble gas (ⁱNg) as:

$${}^{i}Ng_{tot} = {}^{i}Ng_{eq} + {}^{i}Ng_{exc} + {}^{i}Ng_{rad}^{is} + {}^{i}Ng_{nuc}^{is} + {}^{i}Ng_{fiss}^{is} + {}^{i}Ng_{rad}^{terr} + {}^{i}Ng_{nuc}^{terr} + {}^{i}Ng_{man}^{terr} - \Sigma L$$
(8.2)

where the subscripts tot, eq, exc, rad, nuc, fiss and man indicate total (=measured), equilibrium with air, excess air, radiogenic, nucleogenic, fissiogenic (only relevant for Ne, Kr, and Xe) and mantle origin, which correspond to the various source (sum of inputs, ΣI) terms as well as potential gas losses which are included as ΣL (sum of loss terms). All components marked 'is' (in situ) represent sources inside the water parcel (contained within a mobile $\Delta x \Delta y \Delta z$), while those with 'terr' (terrigenic) have their origin outside.

For ⁴He, the rad term is U–Th series alpha decay and for ³He the rad term is ³H decay, often termed ³He_{tri}. Fissiogenic He is not relevant, and nucleogenic ³He is produced by the reaction ⁶Li(n, α)³H(β ⁻)³He. He of mantle origin can often be found in areas affected by tectonic activity. The ³He/⁴He ratio of radiogenic and mantle He is on the order of 10⁻⁸ or 10⁻⁵, respectively. For He, separation of components in the total measured gas by a source/production process is easier than by origin (in situ or terrigenic). Additionally, the analysis must be able to recognize and correct for several gas loss, *L*, possibilities that presumably reduce each Ng component via equilibrium fractionation or bulk non-fractionating loss. Calculation of a ⁴He model age is based on in situ and terrigenic components.

8.4.1. Equilibrium with air, ⁴He_{eq}

The ⁴He_{eq} is governed by the solubility of noble gases in water as a function of Henry's law. As solubility is a function of temperature, pressure and salinity, most calculations of ⁱNg_{eq} are generalized from a limited suite of laboratory measurements. Weiss (1970) [523], Weiss (1971) [524], and Weiss and Kyser (1978) [254] provide empirical equations that yield solubility concentrations from air. Clever (1979) [525], Clever (1979) [526] and Clever (1979) [527] provide mole fraction solubilities which Aeschbach-Hertig et al. (1999) [302] have combined with the salting-out coefficients (Smith and Kennedy (1983) [518]) to provide solubilities as a function of pressure, temperature and salinity. Table 8.1 (after Kipfer et al. (2002) [528]) provides the equations by which to calculate noble gas solubilities.

It should be noted that calculation of ${}^{i}Ng_{eq}$ requires the definition of an assumed recharge elevation and pressure. Additional assumptions are required with regard to changes in temperature and salinity that may occur along the flow path from recharge to the sampling point. It is often assumed that recharge occurs and ${}^{i}Ng_{eq}$ is established at the mean annual temperature and pressure of the (assumed) recharge zone and that subsequent changes in temperature (as a result of heat gain along a geothermal gradient) have no impact on this initial equilibrium solubility. Changes in 'salinity' as a result of weathering and/or opening of fluid inclusions may also be assumed to have no impact on this initial equilibrium solubility. However, changes in salinity by mixing from different sources and/or halite dissolution cannot be viewed in such a simplistic sense: strong increases in salinity by halite dissolution were demonstrated to impact transport of noble gases (Suckow and Sonntag (1993) [529]). It is unknown to what extent mixing of waters impacts Ng concentrations versus the impacts that are the result of in situ increases in T and P. Some correlations between Cl and ⁴He could be the result of progressive NaCl addition by halite dissolution, whereas other changes in Cl could be the result of weathering and The equilibrium concentrations of He, Ne, Ar and Kr can be calculated as:

$$C_{\rm eq}^{\rm i} = \exp\left\{t + t2(100/T) + t3\ln(T/100) + t4(T/100) + S[s1 + s2(T/100) + s3(T/100)^2]\right\} \left(\frac{(\text{ptot} - \text{ew})}{(\text{pnorm} - \text{ew})1000}\right)$$

The equilibrium concentrations of Xe can be calculated as:

$$C_{\rm eq}^{\rm Xe} \exp\left[x1 + x2(100/T) + x3 \times \ln(T/100)\right] \times 0.00011 \times \exp\left[S(x4 + x5(100/T) + x6 \times \ln(T/100))\right]$$

Solubilities of ³He and ⁴He expressed as a function of the ³He/⁴He ratio (R_{eq}):

$$R_{eq} = 1.384 \cdot 10^{-6} \left[\exp((r1 + r2) / T + r3 / T^2)(1 + r4S) \right]^{-1}$$

where

$C_{\rm eq}^{\rm i}, C_{\rm eq}^{\rm Xe}$	concentration of noble gas (cm ³ STP/g);
ptot, phorm	iocal and reference (1 ann) atmospheric pressure (ann),
ew	water vapour pressure;
1, 5	water temperature (K) and satisfy (g_{salt}/kg) .

The coefficients are given after Kipfer et al. (2002) [528].

TABLE 8.1. NOBLE GAS SOLUBILITIES

			Coefficie	ent, i		
	$R_{ m eq}$	Не	Ne	Ar	Kr	Xe
t1		-167.2178	-170.6018	-178.1725	-112.684	
t2		216.3442	225.1946	251.8139	153.5817	
t3		139.2032	140.8863	145.2337	74.469	
t4	—	-22.6202	-22.629	-22.2046	-10.0189	_
s1	_	-0.044781	-0.127113	-0.038729	-0.011213	
s2		0.023541	0.079277	0.017171	-0.001844	
s3	_	-0.0034266	-0.0129095	-0.0021281	0.0011201	
r1	-0.0299645					
r2	19.8715					
r3	-1833.92			—		
r4	0.000464			—		
x1						-74.7398
x2	_			—		105.21
x3						27.4664
x4	_					-14.1338
x5	_			—	_	21.8772
x6	_					6.5527

release of fluid inclusions (presumably rich in Cl). Ballentine et al. (2002) [530] provide a discussion of the background theory. Nonetheless, the isolation and quantification of ${}^{i}Ng_{eq}$ and ${}^{4}He_{eq}$ requires a suite of assumptions not all of which have been checked and not all of which can be checked. This is a theme that will continue.

8.4.2. Excess 'air' components, ⁴He_{exc}

The creation of ${}^{4}\text{He}_{exc}$ is the result of soil processes by which excess air is occluded in the recharge process and is eventually dissolved as pressure increases. Bulk dissolution of unfractionated air is one possibility that requires the use of an Ng tracer that is controlled primarily by dissolution of air (e.g. Ne) rather than in situ and external sources (e.g. ${}^{4}\text{He}$). Early research used a definition of the Ne components in groundwater to define the excess air component of Ne which, for unfractionated air, could then be scaled to the ${}^{4}\text{He}_{exc}$, rewriting Eq. (8.2) for Ne:

$$Ne_{tot} = Ne_{eq} + Ne_{exc} - \sum L$$
(8.3)

and assuming no losses:

$$Ne_{exc} = Ne_{tot} - Ne_{eq}$$
(8.4)

This allows the excess ⁴He component to be calculated as:

$${}^{4}\text{He}_{\text{exc}} = \text{Ne}_{\text{exc}} \left(\frac{\text{He}}{\text{Ne}}\right)_{\text{air}}$$
(8.5)

As Ne solubility is the least temperature sensitive of the noble gases, such an assumption and calculation were tenable. However, this assumes that air is in excess and that its process of dissolution is non-fractionating and non-equilibrating. Cross-checking these assumptions with the noble gas suite has shown this to be oversimplified (Aeschbach-Hertig et al. (1999) [302]). Yet, in most cases, the Ne_{exc} component is less than 30% and, thus, the calculated ⁴He_{exc} is also small, especially considering that the ⁴He_{terr} and the ⁴He_{rad} are often orders of magnitude larger. As mass spectrometric measurement of ⁴He usually also acquires Ne, analytical costs can often be reduced by making these assumptions and acquiring He and Ne concentrations only.

If measures of the complete noble gas suite are acquired, such measures can be evaluated in terms of the palaeorecharge temperature that has found application in palaeoclimate research (Stute et al. (1995) [213]; Stute et al. (1995) [214]; Stute et al. (1992) [42]). Considerable research has been devoted to evaluating the ⁱNg_{exc} component in order to best fit the ⁱNg_{eq} components to a recharge temperature. Stute et al. (1995) [213] and Stute et al. (1995) [214] explored partial re-equilibration where an initial air bubble was dissolved and partial re-equilibration occurred by molecular processes across the water table. Peeters et al. (2002) [531] suggested the use of ${}^{20}Ne/{}^{22}Ne$ ratios to test the partial re-equilibration model but where measures have been made, no significant diffusive fractionation of the isotopes has been uniquely identified. Kipfer et al. (2002) [528] propose a multistep re-equilibration model that would allow for large excess air (accommodated at pressure well beyond the water table). However, as multistep re-equilibration reduces to partial re-equilibration in the limiting case and the lack of evidence for diffusive fractionation of ²⁰Ne/²²Ne (Peeters et al. (2002) [531]), such a model is also less than adequate. The closed system equilibration model (Aeschbach-Hertig et al. (2001) [532]; Aeschbach-Hertig et al. (1999) [302]; Aeschbach-Hertig et al. (2000) [55]; Peeters et al. (2002) [531]) appears to allow direct physical interpretation of the excess air component and its variance across the Ng suite in most cases. Direct verification of a mechanistic link between excess Ne and water table fluctuations is not available (Kipfer et al. (2002) [528]) but experiments with sand columns appear to support the basic mechanistic possibilities (Holocher et al. (2002) [533]). A widely used Excel/Matlab routine can be downloaded from: http://www.eawag.ch/organisation/abteilungen/wut/schwerpunkte/umweltisotope/ methoden/interp_EN

8.4.3. Radiogenic production, ⁴He_{rad}

Radiogenic production via alpha decay of U–Th series elements creates ${}^{4}\text{He}_{rad}$. Other sources of α particles (e.g. Nd decay) and ${}^{4}\text{He}$ as a result of (n, α) interactions can be considered quantitatively insignificant. Under the assumption that U–Th series elements have reached radioequilibrium, the ${}^{4}\text{He}$ production rate from rock can be expressed as:

⁴He cm³ STP ·
$$g_{rock}^{-1}$$
 · $a^{-1} = J'_{He} = 0.2355 \times 10^{-12} ([U](1 + 0.123([Th]/[U] - 4)))$ (8.6)

⁴He atoms
$$g_{rock}^{-1} \cdot a^{-1} = J'_{He} = 2.688 \times 10^{19} (0.2355 \times 10^{-12} ([U](1 + 0.123([Th]/[U] - 4))))$$
 (8.7)

where [U] and [Th] are concentrations expressed in parts per million (Craig and Lupton (1976) [534]; Torgersen (1980) [535]).

For groundwater calculations, it is then necessary to quantify how much of this in situ production becomes available to the fluid phase. This has been generalized as a release factor Λ_{He} and the accumulation of ⁴He in the fluid phase can be calculated as:

⁴He cm³STP ·
$$g_{H2O}^{-1}$$
 · $a^{-1} = J_{He} = J'_{He}(\rho \Lambda_{He}((1 - \Phi)/\Phi))$ (8.8)

where

 ρ is the density of the solid (g/cm³);

 Φ is the porosity (cm³_{H2O}/cm³_{total}).



FIG. 8.1. Mechanisms for the release of α decay ⁴He from rock: (1) recoil of the α particle (30–100 µm); (2) recoil followed by rapid diffusion along recoil damage tracks, grain imperfections and microfractures; (3) molecular diffusion in the solid state with no advantages from recoil damage or grain imperfections; (4) weathering and dissolution release (after Torgersen (1980) [535]).

Quantification of Λ_{He} is a challenge. Figure 8.1 (modified from Torgersen (1980) [535]) shows schematically the various mechanisms by which ⁴He can enter the pore space from the solid phase: (i) direct recoil, (ii) rapid diffusion in imperfections, (iii) slow diffusion in the solid phase and (iv) weathering or dissolution.

8.4.3.1. Mechanism 1: direct recoil

The recoil path length of an α particle in silicate material (R_{α}) is of the order of 30–100 µm (Andrews (1977) [536]) and the direct recoil loss of α particles by the solid phase has been evaluated by Flügge and Zimens (1939) [537], and summarized by Torgersen (1980) [535]. From the grain size and the recoil path length, Λ_{He} can be calculated as:

$$\Lambda_{\rm He} = \frac{3R_{\alpha}}{4r} - \frac{1}{16} \left(\frac{R_{\alpha}}{r}\right)^3 \qquad \text{for } 2r \ge R_{\alpha} \tag{8.9}$$

$$\Lambda_{\rm He} = 1 \text{ for } R_a > r \tag{8.10}$$

where

r is the grain radius;

 R_{α} is the recoil path length.



FIG. 8.2. Helium concentrations versus groundwater hydraulic (flow model) age (as supported by ³⁶Cl model ages) for the Great Artesian Basin, Australia. For groundwaters younger than 40 ka, the accumulation rate is 4.6×10^{-12} cm³ STP ⁴He \cdot cm⁻³_{H2O} \cdot a⁻¹ which agrees with the calculated rate ($A_{He} = 1$) of 3.95×10^{-12} cm³ STP ⁴He \cdot cm⁻³_{H2O} \cdot a⁻¹. For groundwaters greater than 100 ka, the rate of accumulation is 2.91×10^{-10} cm³ STP ⁴He \cdot cm⁻³_{H2O} \cdot a⁻¹ or 74× in situ production. An external bottom boundary flux provides the best explanation for the source and the timescale over which it can be seen (from Torgersen and Clarke (1985) [293]).

Most aquifer grain sizes (of the order of millimetres) are large compared to the recoil path length (of the order of 0.1 mm) and Λ_{He} can be approximated as:

$$\Lambda_{\rm He} = \frac{3R_{\alpha}}{4r} \qquad \text{for } R_{\alpha}/r < 0.5 \tag{8.11}$$

Calculations indicate that direct recoil release of α particles should be low (Λ_{He} of the order of 0.075), yet it is often observed (e.g. Heaton (1984) [538]; Torgersen and Clarke (1985) [293]) that ⁴He in the pore water increases as if $\Lambda_{He} = 1$ (Fig. 8.2). The implication of this common assumption ($\Lambda_{He} = 1$) implies that the diffusive (rapid or slow) loss of ⁴He from the solid phase to the fluid phase is balanced by the production of ⁴He in the solid phase by radioproduction of ⁴He. This is equivalent to the assumption that the grain has reached a condition of diffusive (rapid or slow) equilibrium with the local pore water. It should be noted that the timescale on which diffusive equilibrium is reached is much shorter for fast diffusion (mechanism 2) than for slow diffusion (mechanism 3) (see Fig. 8.1).

8.4.3.2. Mechanisms 2 and 3: rapid and slow (molecular) diffusion release

Using an idealized spherical geometry and the solution of Carslaw and Jaeger (1959) [539] (see Fig. 32 of Ref. [539]), a condition of diffusive (rapid or slow) equilibrium with the local pore water occurs in a grain with an initial concentration of ⁴He = 0 at a scaled time of $D_{\text{solid}}t/\Delta x^2 > 0.5$ (for spherical geometries, such as a sand grain, Δx is equivalent to the radius). As a generalization, the diffusive timescale $Dt/\Delta x^2 > 0.5$ implies that a >50% change has been achieved. With the (slow) molecular diffusion coefficient of ⁴He in silicate material on the order of $10^{-18}-10^{-22}$ cm²/s (typical crustal minerals; Lippolt and Weigel (1988) [540]; Trull et al. (1991) [541]), the 'steady state' condition (production in the grain = loss from the grain) can apply to a 0.1 cm grain on the timescale of 10^8 a (10^{-18} cm²/s) (Fig. 8.3). However, when grains are laced with imperfections, it is important to differentiate the screened grain size from the effective grain size (Ballentine et al. (2002) [530]; Torgersen (1980) [535]). For the effective grain size, internal defects, imperfections, dislocations and



FIG. 8.3. Simple scaled rates of diffusion for various grain sizes as a function of diffusion coefficient. The timescale $\Delta x^2/2D$ approximates the timescale for loss of the solid phase, accumulated ⁴He. Significant fluxes (>10% of max.) would be observable at timescales of $0.1\Delta x^2/2D$ and all initial ⁴He would be effectively lost by $3\Delta x^2/2D$. It should be noted that $D_{He}/D_{Ar}\sim 10^5$ and, therefore, closure for Ar is maintained for far longer timescales than closure for ⁴He.

microfractures render the distance to a pore space-available boundary to be significantly less than the screen-sorted grain size (the rapid diffusion case of Torgersen (1980) [535]; see Fig. 8.1). For example, an effective grain size of 0.01 cm will reach steady state (production = loss) on a timescale of the order of 10⁶ a (100 times faster) if transport time in the 'imperfection pathway' is not considered significant. Additionally, the (slow) diffusion coefficient of ⁴He in grains may increase with time due to radiation damage, microfracturing, etc. and the effective grain size may, therefore, decrease with time. As this loss of ⁴He from a grain is typically not measureable in the laboratory on a reasonable timescale, a measure of loss at a higher temperature can often be scaled to the in situ lower temperature (Mamyrin and Tolstikhin (1984) [521]). Although such measures are possible, this laboratory measure of *D*_{solid} will only reflect conditions now rather than conditions over the timescale of the ⁴He model age (the time over which solid material contributed to the fluid parcel). Of additional concern is the possibility of variability in Λ_{He} in space or time. Is the rock sample acquired representative of the 'average' rock the water parcel has seen over its residence time? As effective grain sizes in aquifers are typically small and the diffusion coefficients for ⁴He in the solid phase are typically large, an in situ production rate equivalent to $\Lambda_{He} = 1$ is often assumed.

8.4.3.3. Mechanism 4: bulk dissolution or weathering

Bulk dissolution or weathering of grains should also result in the release of ⁴He accumulated within the grain (see Fig. 8.1). As grains dissolve from the outside and diffusion will create gradients in the solid phase that decrease the concentration towards the outside of grains, quantification of a priori dissolution release of ⁴He is difficult. Both Torgersen and Clarke (1985) [293], and Heaton (1984) [538] calculate a simple rate for dissolution release of ⁴He based on an assumed uniform concentration of ⁴He in the grain. These concentrations are usually based on the metamorphic or depositional age of the formation and, hence, represent a maximum value. Both Torgersen and Clarke (1985) [293], and Heaton (1984) [538] calculate the rate of 'weathering' release of ⁴He from their systems to be <1% of the $\Lambda_{He} = 1$ condition and, thus, weathering release may be unimportant. However, it is still to be determined whether this is a general condition.

Heaton (1984) [538] estimates a bulk rate of surface chemical weathering from the chemistry of world rivers to be 3 mg_{rock} \cdot kg⁻¹_{rock} \cdot a⁻¹. Simplistically, this is equivalent to a timescale for dissolution of 0.3 Ma. However, Heaton (1984) [538] advises that subsurface dissolution will be of the order of 0.1–0.01× slower, indicating subsurface timescales for dissolution of the order of 3–30 Ma. This 'dissolution timescale' can be compared to the timescale for solid phase loss of ⁴He by molecular diffusion. Using a 'fast' molecular diffusion coefficient (10⁻¹⁸ cm²/s) for grains of 0.1 cm, yields of the order of 300 Ma as a timescale for loss (Fig. 8.3). Thus, one might expect weathering release or chemical dissolution to be an important release mechanism. However, the observation that release equivalent to $\Lambda_{\text{He}} = 1$ is often observed suggests that effective grain sizes for diffusion might be as small as 0.5×10^{-3} cm ($\Delta x = (D\Delta t)^{0.5}$, where $D = 10^{-18}$ cm²/s and $\Delta t = 10$ ka; Fig. 8.3). These arguments suggest that ⁴He release via chemical dissolution should be considered but may often be dismissed.

8.4.3.4. Effective release at low rates ($\Lambda_{He} < 1$)

Under conditions where $D_{\text{solid}}t/\Delta x \ll 0.5$, the solid phase can release ⁴He at a rate that is equivalent to $\Lambda_{\text{He}} \ll 1$. However, the authors are aware of no documented cases for which $\Lambda_{\text{He}} \ll 1$ has been unequivocally shown. This condition may require formation of new grains from new material (authigenic material) with no pre-existing ⁴He, which is likely an artificial case.



FIG. 8.4. The accumulation of ⁴He in various groundwater aquifers as a function of travel time (flow model age). Typical in situ production is 0.18 μ cm³/kg over 60 a. The data indicate rates >100 times the expected in situ production via radiodecay. This enhanced source is the result of slow release of solid phase, accumulated ⁴He (accumulated over the metamorphic age of the rock) that occurs as a result of comminution of large blocks/grains into smaller grains. The source is exemplary of mechanism 3 of Fig. 8.1. (From Solomon et al. (1996) [295], reproduced with permission of the American Geophysical Union.)



FIG. 8.5. Model calculations showing the timescale over which solid phase, accumulated ⁴He can be released into the groundwater. The fluxes from the solid phase to the groundwater are a function of the grain size (labelled on various curves), the initial ⁴He concentration before comminution (metamorphic age of the solid; compare initial concentration of 60 μ cm³/g to 6 μ cm³/g) and the diffusion coefficient for ⁴He in the solid (graphs present the case for only a single diffusion coefficient D^{He} = 4.5 × 10⁻²¹ cm²/s). (From Solomon et al. (1996) [295], reproduced with permission of the American Geophysical Union.)



FIG. 8.6. The bulk fracturing model of Torgersen and O'Donnell (1991) [543] illustrated the 1-D case for simple comminution. Before fracturing, the slab of thickness L can acquire a noble gas concentration that is (initial condition 1) 0.005 times the steady state or (initial condition 2) the steady state concentration of $A_o L2/D$. Fracturing then reduces the slab thickness from L to 1. Fracturing is quantified as the ratio L:1 and can have any value >1. It should be noted that the higher L:1, the larger the surface area available for diffusion into the pore space. (From Torgersen and O'Donnell (1991) [543], reproduced with permission of the American Geophysical Union.)

8.4.3.5. Enhanced release ($\Lambda_{He} > 1$) by comminution, microfracturing and macrofracturing

The case where $\Lambda_{He} > 1$ can and does occur as a result of a decrease in effective grain size by comminution, micro- and macrofracturing. In such a case, a large effective grain size (>1 cm) may retain most of its in situ production of ⁴He but release that ⁴He when the grain size is reduced. In the case of the Sturgeon Falls site in Ontario, Canada, Solomon et al. (1996) [295] hypothesized that Precambrian Canadian Shield rocks (>1 Ga) that occur in large blocks (fracture to fracture spacing on the order of 1–10 m) were reduced by glacial action to the 1 mm grains that comprise the aquifer. The accumulated ⁴He would then be released from 1 mm grains on a timescale of the order of 10⁸ a (10⁻¹⁸ cm²/s) to 10¹⁰ a (10⁻²⁰ cm²/s) (see Fig. 8.3). Such release (Λ_{He} order 100) was confirmed by laboratory measuresments (Solomon et al. (1996) [295]). Based on a comparison of groundwater ⁴He accumulation rates and independently estimated travel times (Fig. 8.4), this scenario (glacially produced comminution and $\Lambda_{He} >> 1$) may be common at high latitudes. The enhanced release of ⁴He input within an aquifer.

This concept of comminution/fracturing is scalable. Honda et al. (1982) [542] have shown in laboratory experiments that rock fracturing can lead to the release of ⁴He. In the 1-D case, Torgersen and O'Donnell (1991) [543] have shown that fracturing creates large gradients and surface areas that lead to high ⁴He fluxes ($\Lambda_{He} >> 1$) (Fig. 8.6). The resultant 'pieces' continue to lose ⁴He ($\Lambda_{He} >> 1$) for timescales on the order of $2 < Dt/\Delta x^2 < 5$ depending on the initial condition. It should be noted that the flux from the slab (Fig. 8.7) is reduced by half in the timescale defined by $Dt/\Delta x^2 = 1$, but that, in some cases, the flux remaining to be released may still be larger than in situ production. Thus, increased stress leading to microfracturing can result in $\Lambda_{He} >> 1$ through new surfaces and/or the creation of imperfections and microcracks which creates shorter routes and higher gradients to enable high transport rates to imperfections. At the larger scale (1–1000 m), it has been shown that 1 km of uplift



FIG. 8.7. The flux of noble gas (y axis) to the pore space relative to in situ production as a function of diffusion time, Dt/l^2 (from the general case $Dt/\Delta x^2$). Dashed lines are calculated for the IC1 (0.005 times steady state concentration at time of fracturing) and solid lines are calculated for IC2 (steady state concentration at time of fracturing). (From Torgersen and O'Donnell (1991) [543], reproduced with permission of the American Geophysical Union.)

or downdrop will result in thermal stresses sufficient to produce stresses approaching the yield strength of rock (Knapp and Knight (1977) [544]; Savage (1978) [545]). The 1-D modelling of Torgersen and O'Donnell (1991) [543] shows that stress-induced macrofracturing leads to large fluxes from blocks ($\Lambda_{\text{He}} > 10^4$) and although such fluxes decrease with time, they can produce $\Lambda_{\text{He}} >> 1$ for timescales on the order of $2 < Dt/\Delta x^2 < 5$ (see Fig. 8.7). The results in Fig. 8.7 show that fracturing/comminution can result in large local sources of ⁴He to the pore space that can persist for characteristic timescales of $1 < Dt/l^2 < 5$ but $Dt/l^2 = 0.5$ marks the point where approximately half of the accumulated noble gas has been lost to the pore space. Given that $D_{\text{He}}/D_{\text{Ar}} \sim 10^5$, the entire accumulated ⁴He could be lost from the slab while ⁴⁰Ar loss continues for a considerable longer time. It should be noted that the concentration in the pore fluid is governed not only by the flux from the slab but also by the residence time in the post-fractured system.

The net result of microscale fracturing coupled to larger scale (km) macrofracturing is that retention of ⁴He in the crust becomes difficult and there can be a resultant significant flux of ⁴He from the crust to the atmosphere.

8.4.3.6. Crustal fluxes of ⁴He_{rad}

The concentration and residence time of ⁴He in the atmosphere suggest that on a continental space scale and a megayear (Ma) timescale, the flux of ⁴He from the Earth's crust to the atmosphere is comparable to the net in situ production by U–Th series element α decay in 30–40 km of the crust (Torgersen (1989) [546] and Torgersen (2010) [547]). This is not equivalent to a steady state loss of ⁴He from the crust to the atmosphere as implied by Ballentine et al. (2002) [530], as any measure of flux contains within it a characteristic time and space scale, whereas steady state implies that the flux is constant in time and space. However, the implication of the atmospheric ⁴He mass balance is that in situ crustal production of ⁴He must both be released to a mobile phase (see above discussion of Λ_{He}) and that that mobile phase must be transportable to the Earth's surface on timescales of the order of 1 Ma although it may take longer (10⁹ a) for that flux to be established (see Fig. 8.8).

With regard to the interpretation of ⁴He in groundwater systems, the issue becomes one of a possible dominant flux of ⁴He into a water parcel from external sources rather than the internal production terms encountered in the space $\Delta x \Delta y \Delta z$ (acknowledging that $\Delta x \Delta y \Delta z$ is heterogeneous and that the solid phase



FIG. 8.8. The effective time for diffusive transport as a function of layer thickness and effective diffusion coefficient. The timescale $\Delta x^2/2D$ approximates the timescale for diffusive exchange of produced/accumulated ⁴He. Significant fluxes into the layer and/or out of the layer (~20% of the max.) would be observable at timescales of $0.1\Delta x^2/2D$ and all exchangeable species would be effectively lost/gained in $3\Delta x^2/2D$.



FIG. 8.9. A statistical analysis of the measured flux of ⁴He into 271 Canadian Shield lakes using the data of Clarke et al. (1977) [548], Clarke et al. (1983) [549], and Top and Clarke (1981) [550]. These data typically provide one sample per lake, including both a measure of excess ⁴He and the ³H/³He model age.

remains in place while the water flows). Table 8.2 shows the measured ⁴He degassing flux in locations around the world. Although the analysis of Torgersen and O'Donnell (1991) [543] suggests fluxes from individual blocks can be 10⁴ times in situ production and that $\Lambda_{\text{He}} < 1$ remains an unobserved possibility, it is of note that area- and time-weighted mean flux (3.3×10^{10} ⁴He atoms \cdot m⁻² \cdot s⁻¹) is approximately equivalent to the mean crustal production. When the fluxes of Table 8.2 are evaluated with respect to their log-normal mean (4.18×10^{10} ⁴He atoms \cdot m⁻² \cdot s⁻¹), the variability in measured ⁴He flux is approximately ±1.5 orders of magnitude (Torgersen (2010) [547]; see also Fig. 8.9).

Region	${}^{4}\text{He flux} \label{eq:hermitian} (atoms \cdot m^{-2} \cdot s^{-1} \times 10^{10})$	Method	Plotted, evaluated 4 He flux (atoms·m ⁻² ·s ⁻¹ × 10 ¹⁰)	Timescale	Space scale (km)	Reference
Continents	2.8	calculation from U,Th	2.8	2 Ma	>5000	1,2,3
Great Artesian Basin	3.1	Measured accum in gw	3.1	1 Ma	500	0
Great Hungarian Plain	0.07-0.45	Measured accum in gw	0.2	1 Ma	200	7
Great Hungarian Plain	8	Measured accum in gw	8	1 Ma	200	8
Paris Basin	0.44	Measured accum in gw and model	1	10 ka	100-500	11,12,13,14
Paris Basin	0.4	Measured accum in gw and model	0.4	10 ka	100-500	11
Molasse Basin	0.2	Measured accum in gw	0.2	250 ka	50	6
Carrizo Aquifer, TX	1	Measured accum in gw and model	1	100 ka	75	23
Black Sea	1.3	Profile and model	1.3	440 a	661	26
San Juan Basin, NM	0.8	Measured accum in gw and model	0.8	40 ka	40	23
Eastern Paris Basin	3.8–15	Measured accum in gw and model	10	10 ka	75	15
Auob Sandstone	0.09–3	Measured accum in gw	1	20 ka	50	5
Auob Sandstone	2.6	Measured accum in gw	2.6	20 ka	50	2
Serra Grande, Brazil	2.4	Measured accum in gw	2.4	20 ka	40	24, 28
Caspian Sea	1.9–5.9	Lake profile	4	25 a	609	22
Lake Baikal	14–28	Lake profile	21	10 a	177	22
Lake Huron	Not detectable	Lake profile	0.001*	0.5 a	243	20, 28
Lake Erie	Not detectable	Lake profile	0.001*	0.5 a	161	20, 28
Lake Ontario	Not detectable	Lake profile	0.001*	0.5 a	136	20, 28
Lake Van	25	Lake profile, volcanic area	25	2 a	09	22

TABLE 8.2. THE HELIUM FLUX FROM CONTINENTAL REGIONS

Lake Taupo	3	Lake profile, volcanic are:	a 3	10 a	15	19, 28
Lake Nyos	30 000	Lake profile, volcanic are	a 30 000	18 a	1	22
Lake Lugano	4.8	Lake profile	4.8	12 a	L	22
Lake Nemrut	600	Ice covered, volcanic area	a 600	36 a	3	22
Crater Lake	55	Lake profile, volcanic are	a 55	3 a	L	22
Lake Lucerne	2.1–14	Lake profile	8	1 a	10.7	22
Lake Zug	1.6	Lake profile	1.6	3 a	9	22
Lake Mashu	92	Lake profile, kz, volcanic a	rea 92	2 a	5	22
Teggau Lake	300-600	Lake profile	450	1 a	4	18, 28
Lake Alpnach	1.1	Lake profile	1.1	0.5 a	5	22
Green Lake	811	Lake profile	811	10 a	1	16, 28
Lake 120	14	Lake profile	14	3 a	0.5	17, 28
Lac Pavin	60	2 Lake profiles, volcanic ar	ea 60	1–2 a	0.66	22
Laacher Lake	1000	2 Lake profiles, volcanic ar	ea 1000	0.26 a	1.4	22
271 Clarke Lakes	$4.6^{a/3}.9 \times$	271 Lakes; 1 sample each		0.3 a	0.5	21, 28
World Ocean	0.1	Profile	0.1	500 a	22 609	25
Ocean flux	0.04-0.26	Theory	0.1	510 a	22 609	27
^a the flux is $<10^9$ ⁴ He atom	$s \cdot m^{-2} \cdot s^{-1}$; the f	lux is chosen to be the best estimates ((symmetric log-normal error bou	nds).		
 O'Nions and Oxburgh Torgersen and Clarke (Torgersen and Ivey (198 Craig et al. (1975) Heaton (1984) Sano et al. (1986) Stute et al. (1989) Martel et al. (1989) Andrews et al. (1985) 	1983) 1985) 55)	10) Tolstikhin et al. (1996) 11) Marty et al. (1993) 12) Pinti and Marty (1995) 13) Pinti et al. (1997) 14) Castro et al. (1998) 15) Dewonck et al. (1981) 16) Torgersen et al. (1981)	 17) Campbell and lorgerser 18) Torgersen and Clarke (1 19) Torgersen (1983) 20) Torgersen et al. (1977), Cla 21) Clarke et al. (1977), Cla 22) Kipfer et al. (2002) 23) Castro et al. (2000) 24) Stute et al. (1995) 	(1980) 978) rke et al. (1983),	 25) Well et al. (Schlosser al 26) Top and Cla 27) Torgersen (28) This study 	2001) (ref. in nd Winckler (2002)) rke (1983) 989)

It is acknowledged that the fluxes in Table 8.2 represent fluxes distributed over an area appropriate to the measurement. For instance, the quantified external flux into the Great Artesian Basin (Torgersen and Clarke (1985) [293]) is roughly equivalent to whole crustal production and is influxed to the base of the aquifer over the space/timescale of the basin. This, of necessity, means that the flux above the aquifer directly from the soil to the atmosphere is very low. Furthermore, the net flux to the atmosphere in the discharge zone would be locally very large since it reflects the input of crustal production over the whole basin and not just the discharge zone. These measures of the degassing fluxes of ⁴He must, therefore, be carefully interpreted with respect to their applicable time and space scale. For the range of basin scale fluxes to be this constrained, vertical transport must not be only relatively rapid but also relatively pervasive.

Figure 8.9 shows a simple analysis of the U prospecting data of Clarke and others (Clarke et al. (1977) [548]; Clarke et al. (1983) [549]; Top and Clarke (1981) [550]) for 271 lakes for which only one sample is obtained per lake. The calculation in the figure assumes the depth of sampling (most often below the thermocline) is an approximation of the mean lake depth. The calculation likely has an error based on assumptions that is of the order of three times. Also shown are fluxes based on the data in Table 8.2 for which both an area multiplied by a time weighted mean has been calculated, as well as a log-normal mean and deviation. The agreement between the mean and standard deviation for the Clarke lakes and Table 8.2 data suggest the magnitude of the crustal degassing flux is approximately equivalent to whole crustal production with variance of a factor of 44.6 times or 1.5 orders of magnitude. One, therefore, has a 68% probability of measuring a flux between 0.1×10^{10} and 186×10^{10} atoms ⁴He \cdot m⁻² \cdot s⁻¹ in any one study. The analysis suggests strong spatial and temporal variability in the measured flux.

Although such data only captures of the order of 0.5 a of ⁴He flux over a specific lake area and is likely subject to errors on the order of three times due to the assumptions necessary (the assumptions also suggest the estimate is ~50% too high), the mean flux measured by these lakes is 4.57×10^{10} ⁴He atoms \cdot m⁻² \cdot s⁻¹ (log-normal mean with a standard deviation of a factor of 3.9 times written as */3.9×). The lake regions sampled by Clarke and others is an area of the Precambrian Canadian Shield which was depressed by about 1 km due to coverage by 3 km of ice sheet approximately 20 ka ago. Thus, it is noteworthy both that the mean measured flux $(4.57 \times 10^{10} \text{ }^{4}\text{He atoms} \cdot \text{m}^{-2} \cdot \text{s}^{-1} \text{ log-normal})$ mean with a standard deviation of $(3.9\times)$ is not much larger than whole crustal production (3 \times 10¹⁰ ⁴He atoms \cdot m⁻² \cdot s⁻¹ (Torgersen (1989) [546]; Torgersen and Clarke (1985) [293]); and that the variance of the flux is consistent with the range reported from much larger basins (see Table 8.2). While the coverage of the planet with regard to crustal flux measurements remains limited, these measurements (Table 8.2, Fig. 8.9) support a hypothesis that the mean flux of ⁴He from the continental crust is of the same order as the in situ production from U-Th series decay in the continental crust. However, the variance of the crustal degassing flux is significant (a factor of 10^6 (95th per centile) for short time (0.5 a) and short space scales (1 km) (Torgersen (2010) [547])) and is likely unpredictable, thus, complicating the potential use of ⁴He as a method of groundwater 'dating'. Such a conclusion also requires that the net rate of vertical transport in the crust be examined.

8.4.3.7. Vertical transport of ${}^{4}He_{terr}$ in the crust

Simple scaling arguments can be used to evaluate the necessary rates of vertical transport in the continental crust in order to achieve surface crustal fluxes equivalent to the rate of whole crustal in situ production. As the data in Fig. 8.9 and Table 8.2 represent multiple time and space scales, the problem is constrained by the limit: continental degassing and basin scale measures of the degassing flux (on the time and space scale of 10⁶ a and 1000 km) can be approximated as equivalent to the in situ production from 30–40 km of crust but with considerable variance (Torgersen (2010) [547]). This does not imply steady state degassing is applicable everywhere at all times; but it does acknowledge that the range exhibited in Table 8.2 and Fig. 8.9 is relatively small. In order to achieve the crustal degassing

flux in the Great Artesian Basin, Torgersen and Clarke (1985) [293] used a timescale of 2×10^8 a (corresponding to a Jurassic age for the aquifer material) and assumed that most of the U–Th resided in the upper 7 km of crust to calculate a scaled effective diffusion coefficient (Fig. 8.8) of 8×10^{-6} cm²/s for that 7 km of crust. Torgersen (1989) [546], using a solution from Carslaw and Jaeger (1959) [539], scaled these observations to effective vertical diffusivities of 10^{-5} – 10^{-6} cm²/s (Torgersen (1989) [546]) or vertical velocities of 0.1–1cm/s. Given the diffusivity of gas in water is of the order of 10^{-5} cm²/s and that the porosity ($\Phi = 0.1$) and tortuosity effects will reduce this quiescent water to $D\Phi^2 = 10^{-7}$ cm²/s, it is clear that over the long time and space scale, continental crust must transport significant quantities of ⁴He and water at rates that are significantly faster than would be measured by typical (short time and space scale) well tests.

Such rates of transport are surprising when one considers the hydraulic conductivity of consolidated, non-granular rocks (Freeze and Cherry (1979) [11]) but less surprising when the rates of metamorphic processes are considered (Etheridge et al. (1984) [551]; Etheridge et al. (1983) [552]). The low hydraulic conductivities and transport often encountered in bulk non-granular rock are measured over small timescales (<1 a) with small space scale (of the order of centimetres) pieces of rock. In contrast, metamorphic processes reflect the transport in the crust on the larger time/space scales. This conclusion of rapid transport and high volumes of water is consistent with the requirements of the observed products in metamorphic geology (e.g. Etheridge et al. (1984) [551]; Etheridge et al. (1983) [552]). Metamorphic rock structure also suggests that fluid transport is episodic with periods of 'no transport' followed by periods of 'very high transport'. Thus, the effective degassing of continental crust is supportive of and supported by the fluid transport required by metamorphic processes. When the time/space scale for transport is large, the effective rate of crustal scale transport is higher than might be predicted. However, any specific quantification of vertical transport in the crust may yield numbers which suggest that such crustal scale transport is not viable. This feature was specifically addressed by the Torgersen and Clarke (1992) [294] study at Cajon Pass drillhole, where the vertical transport measured by borehole tests showed rates of 10^{-5} cm/a while effective rates estimated from the apparent ⁴He tracer ages of the fluid implied vertical rates of 0.04-0.6 cm/a. Vertical transport in the continental crust must, therefore, be episodic (as required by metamorphic geology; Etheridge et al. (1984) [551]; Etheridge et al. (1983) [552]), with long periods of slow transport and short periods with a very high transport rate. Thus, what is 'seen' in the crustal scale transport of ⁴He is comparable to travel in city subway systems: one can travel by subway from downtown Manhattan to uptown in a specific period of time (effectively several kilometres per hour) but when viewed in detail, this transport is accomplished by a series of stops (velocity of 0 km/h) interrupted by bursts of high speed (tens of kilometres per hour) travel. It would, thus, not be surprising for the external flux of 4 He (4 He_{terr}) to become quite important in many aquifer systems. For a more detailed discussion of vertical transport of ⁴He_{terr}, see Torgersen (2010) [547].

8.4.3.8. In situ production of ${}^{3}He$

Radiogenic production of ⁴He is accompanied by a small but important nucleogenic production of ³He as a result of thermal neutron interactions with ⁶Li in the solid phase:

$$^{6}\text{Li}(n, \alpha)^{3}\text{H}(\beta^{-})^{3}\text{He}$$
(8.12)

Helium-3 produced according to Eq. (8.12) is defined as nucleogenic ³He whereas radiogenic (tritiogenic) ³He is produced by an atmospheric source of ³H. To initiate the reaction (Eq. (8.12)), the production of neutrons in the solid matrix by (α , n) reactions and spontaneous fission neutrons must be calculated:

$$n = (n, \alpha)U + (sf, n)U + (\alpha, n)Th$$
(8.13)

Element	Molecular weight (g/mol)	ϕ_{th} (barns)
Li	6.94	71
В	10.81	755
Na	22.989	0.534
Mg	24.305	0.064
Al	26.981	0.232
Si	28.086	0.16
Cl	35.453	32.6
K	39.098	2.07
Ca	40.080	0.44
Ti	47.900	6.1
Cr	51.996	3.1
Mn	54.938	13.3
Fe	55.847	2.56
Ni	58.71	4.54
Со	58.933	37.5
Sm	150.4	5820
Gd	157.25	49 000

TABLE 8.3. PARAMETERS FOR CALCULATION OF ³He/⁴He PRODUCTION RATIOS (after Andrew and Kay (1982) [463])

The dominant target elements for the (α , n) reactions are Na, Mg, Al, Si and C (although water is also a viable and variable sink for neutron capture) and the net production of thermal neutrons (*n* (neutrons $\cdot g^{-1} \cdot a^{-1}$)) can be expressed as (Ballentine and Burnard (2002) [553]):

$$n = 0.01[U](13.8[Na] + 5.4[Mg] + 5.0[Al] + 1.31[Si] + 2.0[C])$$

$$+0.4788[U] + 0.01[Th](6.0[Na] + 2.45[Mg] + 2.55[Al] + 0.56[Si] + 0.83[C])$$

$$(8.14)$$

where [U] and [Th] are expressed in parts per million and the remaining components are in per cent.

These thermal neutrons are captured by further interactions with the solid phase where typical slow neutron path lengths in silicate are of the order of 1 m. This suggests that the bulk solid phase composition can be used to estimate ³He production. Such calculations are well developed. Based on the initial work by Morrison and Pine (1955) [554] and Fiegge et al. (1968) [555], the fraction of the thermal neutron flux captured by ⁶Li (F_{Li} ^{Thn}) can be calculated as (Andrews (1985) [556]; Andrews and Kay (1982) [463]):

$$F_{\rm Li}^{\rm Thn} = \frac{\sigma_i N_i}{\sum \sigma_i N_i}$$
(8.15)

where

 $\sigma_{\rm i}$ is the thermal neutron cross-section;

 $N_{\rm i}$ is the molar abundance for important components of the rock composition (see Table 8.3).

Rock type	3 He/ 4 He calculated $\times 10^{8}$	$^{3}\text{He}^{/4}\text{He}$ measured × 10 ⁸	Reference	
Upper continental crust	3.90		Torgersen and Clarke (1987), Torgersen (1989)	
Lower continental crust	0.21		Torgersen and Clarke (1987), Torgersen (1989)	
Upper crust	1.08		Ballentine and Burnard (2002)	
Middle crust	0.40		Ballentine and Burnard (2002)	
Lower crust	0.37	_	Ballentine and Burnard (2002)	
Oceanic crust	0.029		Torgersen and Clarke (1987), Torgersen (1989)	
Basalt	1.3	_	Andrews (1985)	
Ultramafic	0.114	_	Andrews (1985)	
Hooray sandstone	2.2–3.3		Torgersen and Clarke (1987)	
Sandstone, UK	2.23		Andrews (1985)	
Sandstone, avg	0.58	_	Andrews (1985)	
Clay and shale	1.99		Andrews (1985)	
Limestone	0.1		Torgersen et al. (1981)	
Limestone, UK	1.14		Andrews (1985)	
Limestone, avg	0.23		Andrews (1985)	
Typical granite	5-15		Fiege et al. (1968)	
Granite	2.23		Andrews (1985)	
Wr, stripa	0.594		Andrews et al. (1989)	
Whole rock	1.6	1.6		
Orthoclase	_	40		
Biorite	_	12		
Plagioclase	_	5	Gerling et al. (1971), samples from Ranakiwi	
Quartz	_	15	Sumples nom Rupuktivn	
Amphibole		4.5		
Zircon	—	2		
1-Whole rock	1.6	1.6		
2-Whole rock	1.7	1.9		
4-Whole rock	1.4	0.3	Tolstikhin and Drubetskoy (1977), Mamyrin and Tolstikhin (1984)	
43-Whole rock	0.7	0.8	Mamyrin and Tolstikhin (1984)	
27-Whole rock	0.09	6		
ss1-WR	—	0.21		
ss1-feldspar	—	0.238		
ss1-mica	—	0.462		
ss1-quartz	_	0.0084	Martel et al. (1990),	
rh1g-WR	6.4	0.21	samples from Carnmenellis	
rh12d-WR1	6.7	0.154	samples nom Cammenents	
rh12d-WR2	6.7	0.49		
Uraninite	_	0.0098		

 TABLE 8.4. ³He/⁴He PRODUCTION RATIOS (after Ballantine and Burnard (2002) [553])

Combining Eqs (8.14, 8.15) yields a rate of production of ³He which can be further combined with Eq. (8.7) to calculate the ³He/⁴He production ratio. It should be noted that the rate of ³He production is based on the neutron production rate which is a function of [U] and [Th], but the ³He/⁴He production ratio is determined by the rock composition and is a function of the Li/U–Th ratio.

Table 8.4 shows the ³He/⁴He production ratio for average crust as well as selected rock types based on specific rock compositions from the literature. While there is a large degree of agreement, the observed differences and variability are significant. Table 8.4 further shows that differences between the observed ³He/⁴He production rate and the calculated ³He/⁴He production rate are also significant. As (α, n) reactions occur within one alpha path length (0–40 μ m) of the decaying nuclei, inhomogeneities in rock chemistry on the space scale of 40 µm can impact the specific ³He yield. Furthermore, the assumption of homogeneous rock over a space scale of 1 m may be problematic for the thermal neutron capture and the relative siting/separation of the trace elements, U, Th, Li, Gd and Sm (the last two elements have very large cross-sections), or the relative presence of water may significantly impact the specific ³He yield. Such issues were discussed by Martel et al. (1990) [557] who investigated Carnmenellis granite ³He/⁴He production (see also discussion by Ballentine and Burnard (2002) [553]). Chazal et al. (1998) [558] revisited Stripa granite and found that the measured ³He/⁴He ratio was 4 times the calculated ratio. Specific causes for the differences between the observed/measured ³He/⁴He ratios and calculated production ratios have not been unequivocally identified but the data in Table 8.4 and analysis of studies mentioned above serve to provide context for the use of calculated ${}^{3}\text{He}/{}^{4}\text{He}$ production ratios and an interpretation of the errors that might be appropriate to that value. Based on the data in Table 8.4 and the discussion of Martel et al. (1990) [557], Ballentine and Burnard (2002) [553], and Tolstikhin et al. (1996) [559], it would appear that a calculated ³He/⁴He production ratio is uncertain up to a factor of ten of the given figure. The best way to determine the ³He/⁴He production ratio is by collecting a number of ³H free groundwater samples from the aquifer and to use the component separation process described below.

8.4.3.9. Separation of He components

As multiple He sources are likely in groundwater systems and each source may have a different isotope composition, separating the various components and specifically identifying the He isotope ratio associated with that component can improve the analysis of He. Transforming the isotopic mass balances for ⁴He and ³He (e.g. Eq. (8.2)) to a measured ratio:

$$\left(\frac{{}^{3}\text{He}}{{}^{4}\text{He}}\right)_{\text{tot}} = \left(\frac{{}^{3}\text{He}}{{}^{4}\text{He}}\right)_{\text{measured}} = \frac{{}^{3}\text{He}_{\text{eq}} + {}^{3}\text{He}_{\text{exc}} + {}^{3}\text{He}_{\text{tri}} + {}^{3}\text{He}^{\text{is}} + {}^{3}\text{He}^{\text{terr}}}{{}^{4}\text{He}_{\text{eq}} + {}^{4}\text{He}_{\text{exc}} + {}^{4}\text{He}^{\text{is}} + {}^{4}\text{He}^{\text{terr}}}$$
(8.16)

where

³He_{tri} is tritiogenic ³He;

ⁱHe_{is} and ⁱHe_{terr} represent in situ produced and terrigenic contributions, respectively.

The latter two contain He of radiogenic, nucleogenic and sometimes mantle origin. Using the method of Weise (1986) [560] (see also Castro et al. (2000) [88]; Stute et al. (1992) [561]; Weise and Moser (1987) [562]) yields an equation in the form of (y) = [m]x + b:

$$\left(\frac{{}^{3}\operatorname{He}_{tot} - {}^{3}\operatorname{He}_{exc}}{{}^{4}\operatorname{He}_{tot} - {}^{4}\operatorname{He}_{exc}}\right) = \left[R_{eq} - R_{is,terr} + \frac{{}^{3}\operatorname{He}_{tri}}{{}^{4}\operatorname{He}_{eq}}\right] \frac{{}^{4}\operatorname{He}_{eq}}{{}^{4}\operatorname{He}_{tot} - {}^{4}\operatorname{He}_{exc}} + R_{is,terr}$$
(8.17)

where $R_{is,terr}$ represents the ³He/⁴He ratio originating from both in situ and terrigenic sources.



FIG. 8.10. Graphical separation of the individual He components. (a) This panel outlines the meaning of the various mixing lines with their end members; (b) Data from the Great Hungarian Plain. Samples containing more than 1 TU of tritium and samples collected in recharge areas (with vertical downward hydraulic gradient) are highlighted with open circles. (After Stute et al. (1992) [561]).

They are merged into one isotope ratio, because they are difficult to separate based on field measurements only:

$$R_{\rm is,terr} = \frac{{}^{3}\text{He}_{\rm is,terr}}{{}^{4}\text{He}_{\rm is,terr}} = \frac{{}^{3}\text{He}_{\rm nuc}^{\rm is} + {}^{3}\text{He}_{\rm nuc}^{\rm terr} + {}^{3}\text{He}_{\rm nuc}^{\rm terr}}{{}^{4}\text{He}_{\rm rad}^{\rm is} + {}^{4}\text{He}_{\rm rad}^{\rm terr} + {}^{4}\text{He}_{\rm man}^{\rm terr}}$$
(8.18)

As radiogenic and mantle helium may both contribute to in situ and terrigenic ⁴He, the graphical determination of the ratio $R_{is,terr}$ provides specific information regarding the source of non-atmospheric ⁴He in the system. The y axis is the measured ³He/⁴He isotope ratio corrected for the excess air addition; the x axis measures the relative importance of ⁴He_{eq} to the other ⁴He components minus ⁴He_{exc}. ³He_{exc} and ⁴He_{exe} can be either derived from Ne measurements using Eq. (8.5) or by using concentrations of all stable noble gases and the inverse model as discussed above (Aeschbach-Hertig et al. (2001) [532]; Aeschbach-Hertig et al. (2000) [55]).

Data plot along linear (He component) mixing lines if $R_{is,terr}$ is constant for the data set and if the amount of ³He_{tri} is constant or negligible (Fig. 8.10(a)). If ³He_{tri} is present, data will scatter somewhat around the mixing line because the variable ⁴He_{eq} is part of the slope in Eq. (8.17). However, the temperature and recharge elevation dependence of ⁴He_{eq} is small and slopes typically do not vary by more than 2% due to this effect. The addition of mantle derived helium (assuming $R_{man} = 1.2 \times 10^{-5}$, e.g. Craig and Lupton (1981) [563]) increases the y axis intercept, while the presence of ³He_{tri} anchors the right end of the mixing lines (Fig. 8.10(a)). If $R_{is,terr}$ is variable in a data set and ³He_{tri} is present and variable, He components cannot be separated in a unique way. Assuming that the pre-nuclear bomb ³H concentrations in precipitation were fairly constant, a ³H measurement on the samples can be used as an indicator of anthropogenic ³He_{tri} and serve as a flag for those cases where a separation may be more complicated or impossible. It should be noted that the area underneath the lowest mixing line in Fig. 8.10(a) is a forbidden area because no known process can produce data that fall into this domain. Similar appearing graphs can be obtained by plotting ³He/⁴He_{tot} versus Ne/⁴He_{tot} or just versus 1/⁴He_{tot}. However, because of variable amounts of ⁴He_{exe}, it is not possible to draw accurate mixing lines in these diagrams.

As an example of the component separation, the He data set from the Great Hungarian Plain aquifers (Stute et al. (1992) [561]) is discussed. For the purpose of this paper, He_{eq} and Ne_{eq} were
calculated using the solubility data of Weiss (1971) [524], assuming an elevation of the recharge area of 200 m and an average recharge temperature of 6 ± 6 °C, which covers the glacial/interglacial temperature range derived from noble gas temperatures in the Great Hungarian Plain (Stute (1989) [522]; Stute and Deak (1989) [564]). He_{exc} was then determined with Eq. (8.5) by using Ne concentration data.

Samples from recharge areas (characterized by a downward hydraulic gradient) and samples containing ${}^{3}\text{H} > 1$ TU at the time of sampling (1985) are highlighted by open symbols (Fig. 8.10(b)). Error bars reflect 1 σ analytical errors and the uncertainty in recharge temperature. The inverse model (see Aeschbach-Hertig et al. (2001) [532] and Aeschbach-Hertig et al. (2000) [55] discussed above) was also used to determine He_{exc} from all of the noble gas concentrations. It yields slightly smaller error bars, but the two plots (not shown) are identical within the error bars of Fig. 8.10(b).

Assuming ${}^{3}\text{He}_{tri} = 0$, the upper limit of $R_{is,terr}$ may be estimated by placing an envelope line below the data points (Fig. 8.10(b)). The resulting intercept with the y axis, $(4 \pm 4) \times 10^{-8}$, is consistent with isotope ratios of He released from sediments (Mamyrin and Tolstikhin (1984) [521]) and is our best estimate for the ³He_{nuc}/⁴He_{rad} ratio in the Great Hungarian Plain. If $R_{is,terr}$ is assumed to be constant, data points above the lower line in Fig. 8.10(b) have to contain either ³He_{tri} or ³He_{man}. There are no ³H data for many of the deeper samples. However, they can be assumed not to contain ³H because of their low radiocarbon content (Stute and Deak (1989) [564]; Stute et al. (1992) [561]). Samples from the recharge areas plot slightly above the lower envelope line, and are unlikely to contain significant amounts of mantle He. Tritium measurements indicate that samples are of pre-nuclear bomb test origin. The sum of derived ${}^{3}\text{He}_{\text{tri}}$ (1.6 ± 1.7 TU) and measured ${}^{3}\text{H}$ (0.5 ± 0.2 TU) is 2.1 ± 1.7 TU, providing an estimate of the natural ³H in recharge before anthropogenic ³H was added to the hydrological cycle. This value is lower than the pre-bomb estimate by Roether (1967) [565] of 5 ± 1.5 TU, possibly as a result of partial loss of ³He_{tri} across the water table due to low recharge rates in Hungary (Schlosser et al. (1989) [566]; Stute et al. (1992) [561]). Assuming ${}^{3}\text{He}_{nuc}/{}^{4}\text{He}_{rad} = 4 \pm 4 \times 10^{-8}$, ${}^{3}\text{He}_{tri} = 1.6 \pm 1.7 \text{ TU}$ and $R_{\rm man} = 1.2 \pm 0.1 \times 10^{-5}$ are representative for the Great Hungarian Plain, the mantle component $({}^{4}\text{He}_{max}/({}^{4}\text{He}_{is} + {}^{4}\text{He}_{terr}))$ yields values up to 16%, consistent with the geological history of the Pannonian Basin undergoing extension. A detailed discussion of the interpretation of this He data set can be found in Stute et al. (1992) [561].

8.4.3.10. Nucleogenic and fissionogenic noble gases: ${}^{i}Ng_{nuc}$, ${}^{i}Ng_{fiss}$

The contribution of nucleogenic and fissionogenic processes in the production of other noble gas isotopes can be an important diagnostic for ⁴He. In particular, nucleogenic ^{20,21,22}Ne, and fissionogenic ^{83,84,86}Kr and ^{129,131,132,134,136}Xe can be produced, although only the dominant isotope can be observed in very old groundwater systems (Kennedy et al. (2002) [567]; Lippmann et al. (2003) [568]). In such cases, the nucleogenic isotope and fissionogenic isotope accumulation can be compared to the accumulation of ⁴He. If the release factor for each noble gas isotope is assumed to be $\Lambda_{Ng} = 1$, then apparent ^{21,22}Ne, ⁸⁶Kr and ¹³⁶Xe tracer model ages should concur with apparent ⁴He tracer model ages. However, because D_{Ng} decreases with increasing atomic mass, the release factor for each noble gas is likely to follow the order $\Lambda_{He} > \Lambda_{Ne} > \Lambda_{Kr} > \Lambda_{Xe}$ (Drescher et al. (1998) [569]), and one might expect the simple noble gas tracer model age (τ_{Ng}) to reflect the order $\tau_{He} > \tau_{Ne} > \tau_{Kr} > \tau_{Xe}$. Such diagnostics can be critical in the evaluation of noble gas model ages from very old groundwaters (Lippmann et al. (2003) [568]).

The difference between ${}^{i}Ng_{rad}$, ${}^{i}Ng_{nuc}$, ${}^{i}Ng_{fiss}$ and ${}^{i}Ng_{terr}$ is often defined by whether the observed isotopic ratios can be produced in the host rock (${}^{i}Ng_{rad}{}^{is}$, ${}^{i}Ng_{nuc}{}^{is}$, ${}^{i}Ng_{fiss}{}^{is}$) or whether the isotopic ratio indicates that it must have its source in another type of rock (${}^{i}Ng_{rad}{}^{terr}$, ${}^{i}Ng_{nuc}{}^{terr}$, ${}^{i}Ng_{fiss}{}^{terr}$), including the aquitard. ${}^{3}\text{He}/{}^{4}\text{He}$ ratios can often suggest a terrigenic (external) contribution to the groundwater, especially where aquitard rock has significantly different bulk compositions to the aquifer rock, although the reader is cognizant of the error in calculation of the ${}^{3}\text{He}/{}^{4}\text{He}$ production ratio. However, because the external terrigenic sources are not known a priori, a comparison with the possible production ratio

calculated for an adjacent rock may not constrain the problem when the observed anomalous isotopic composition could also be explained by a mixture between local aquifer rock and an external 'exotic' rock. While one could feel fairly confident regarding the input of a mantle source of ³He, calculation of a per cent mantle contribution is potentially misleading because the mantle end member has inherent variability (hot spots have ³He/⁴He ratios of 4–35 R_a where R_a is the ratio in air, $R_a = 1.384 \times 10^{-6}$ (Clarke et al. (1976) [242]) and such ratios will also vary with the age (time since eruption; Torgersen (1993) [570] and Torgersen et al. (1994) [571]). This suggests that evidence of a non-local contribution (Ng^{terr}) based on measured isotopic ratios should be seen as evidence to evaluate and model several different mechanisms by which such observations could be produced and observed in situ. The calculation of the per cent mantle ³He contribution when that mantle source is of the order of millions of years old begins to lose meaning.

8.4.3.11. The special case of ^{40}Ar

The above discussion can be generalized to include ${}^{40}Ar_{rad}$ which is the decay product of ${}^{40}K$. The production rate for ${}^{40}Ar_{rad}$ (atoms $\cdot g^{-1} \cdot a^{-1}$) is:

$$^{40}\text{Ar}_{\text{rad}} = 102.2[\text{K}]$$
 (8.19)

where [K] is the concentration of potassium in parts per million.

The ${}^{4}\text{He}_{rad}/{}^{40}\text{Ar}_{rad}$ production ratio can be derived from Eqs (8.19, 8.7) to give:

$${}^{4}\text{He}_{rad} / {}^{40}\text{Ar}_{rad} = \{3.242 \times 10^{6} [\text{U}] + 7.710 \times 10^{5} [\text{Th}]\} / \{102.2 [\text{K}]\}$$
(8.20)

In many cases, ${}^{40}Ar_{rad}$ model ages can be calculated for comparison to ${}^{4}He$ model ages. For the calculation of Λ_{40rad} , the above criteria generally apply. However, it should be noted that K is typically associated with major phases within the rock whereas U–Th series elements are associated with minor phases. In this sense, K may be located in very large grains and/or U–Th may be associated with the surface of grains. Thus, it is often encountered that the release factor for ${}^{40}Ar_{rad}$ (Λ_{40rad}) is less than the release factor for ${}^{4}He$ ($\Lambda_{40rad} < \Lambda_{4rad}$). This has been confirmed by the experiments of



FIG. 8.11. The ${}^{4}He/{}^{40}Ar_{rad}$ ratio measured in gas/oil reservoirs which reflect the accumulation of local and crustal degassing sources and their mode of release from the solid phase production. It should be noted that as time increases (as defined by increasing ${}^{4}He$ or ${}^{40}Ar/{}^{36}Ar$), the ${}^{4}He/{}^{40}Ar_{rad}$ ratio decreases from values well above the production ratio to values that integrate and approach the production ratio. (From Torgersen et al. (1989) [573].)

Krishnaswami and Seidemann (1988) [572], and is intuitive with regard to the difference in their respective diffusion coefficients ($D_{Ar}/D_{He} = 10^{-5}-10^{-6}$; see Ballentine and Burnard (2002) [553]; for calculating diffusion coefficients, see Table 9 of Ref. [553]). Alternatively, the combination of grain size and diffusion coefficient may have enabled ⁴He to reach steady state after comminution, whereas the slower loss of ⁴⁰Ar_{rad} may still impose a local input of ⁴⁰Ar_{rad} that is significantly in excess of local production (Torgersen and O'Donnell (1991) [543]). Thus, ⁴⁰Ar_{rad} model ages can be non-confirmatory of ⁴He model ages, but yet still provide knowledge about processes within the aquifer system. This separation of ⁴He and ⁴⁰Ar_{rad} can be explicitly seen as noble gases accumulate in oil production reservoirs (see Fig. 8.11). Initially, with short times suggested by low concentrations of ⁴He or small ⁴⁰Ar/³⁶Ar ratios, ⁴He/⁴⁰Ar_{rad} ratios are far in excess of in situ production. However, with time and the integrated accumulation of the late release of ⁴⁰Ar_{rad}, the ⁴He/⁴⁰Ar_{rad} ratio approaches that typical of crustal production (~5; Torgersen et al. (1989) [573]).

In the case where ⁴⁰Ar_{rad} and ⁴He_{rad} may both have viable external (to the aquifer) sources (⁴⁰Ar_{rad}^{terr} and ⁴He_{rad}^{terr}), the above possibilities, with respect to relative release factors in the external source, apply. Additionally, diffusive transport into the local water parcel may separate ⁴⁰Ar_{rad} and ⁴He_{rad}. Torgersen et al. (1989) [573] found that the Great Artesian Basin was dominated by external fluxes of ⁴He_{rad} and ⁴⁰Ar_{rad}, both of which were approximated by the whole crustal rate of in situ production (with some degree of variation). Yet, Torgersen et al. (1989) [573] emphasize that ⁴⁰Ar_{rad} has spatial heterogeneity not apparent in ⁴He_{rad} and ⁴⁰Ar_{rad} across aquitards within the Paris Basin created differing and contrasting mechanisms of ⁴He_{rad} or ⁴⁰Ar_{rad} accumulation in different layers. Thus, a comparison of terrigenic ⁴⁰Ar_{rad} ^{terr} and ⁴He_{rad}^{terr} may again not be confirmatory, and ⁴⁰Ar_{rad} requires additional boundary and initial conditions that make any solution non-unique.

8.4.4. Summary

The various components that contribute to the total measured ⁴He in a groundwater sample show that noble gas isotopic measures in addition to ⁴He are a requirement for the separation of components. Furthermore, the overall complexity of noble gas groundwater processes suggests that any tracer model age calculation should be cross-checked with other methods (e.g. ³⁶Cl, ⁴⁰Ar_{rad}). It is then necessary to use such information within a simplified basin flow model (Bethke and Johnson (2008) [84]; Bethke et al. (2002) [574]; Castro and Goblet (2003) [89]; Castro et al. (1998) [96]; Castro et al. (1998) [97]; Castro et al. (2000) [88]; Fritzel (1996) [575]; Zhao et al. (1998) [98]) to arrive at the best conceptualization of the aquifer and its timescale of transport, which may still provide a non-unique solution.

8.5. CASE STUDIES

8.5.1. Setting the stage

In spite of the potential for the application of ⁴He model ages to groundwater transport, it was recognized early that the method raises considerable questions. Geochemists are, of necessity, sceptical of direct application of concepts and have rightly devoted considerable time to testing the underlying assumptions for the use of ⁴He in groundwater systems. Marine (1979) [576] evaluated ⁴He model ages in groundwater based on assumptions regarding Λ_{He} but cross-checked Λ_{He} with measures from the solid phase indicating $0.73 < \Lambda_{He} < 0.97$. However, his analysis did not include external, open system sources of ⁴He (large fluxes from the crust and/or aquitards) that could transport ⁴He into the system (it should be noted that solid phase measures indicating $\Lambda_{He} \sim 1.0$ almost demands a resultant crustal flux). Andrews and Lee (1979) [577] evaluated ⁴He model ages of the Bunter sandstone based on only-local ⁴He inputs but cross-checked such ages with ¹⁴C analysis. The results indicated significant excess ⁴He

(four times) and excessively large ⁴He model ages. Torgersen (1980) [535] evaluated ⁴He model ages based on only-local sources from gas wells, geothermal systems and groundwater, and found ⁴He model ages of the order of 1000 times in excess of ³H–³He model ages for cold springs. Heaton (1984) [538] compared ⁴He model ages to ¹⁴C model ages for two aquifer systems and found only-local source ⁴He model ages were 10–100 times the calculated ¹⁴C model ages. Heaton (1984) [538] calculated the rate of ⁴He addition due to weathering (dissolution) input of ⁴He (Torgersen (1980) [535]) but dismissed that source as insignificant. Torgersen and Clarke (1985) [293] also evaluated a ⁴He source associated with weathering input and also found that source to be insignificant. Notable in the Heaton (1984) [538], and Torgersen and Clarke (1985) [293] studies was an increase in the rate of ⁴He accumulation down the presumed flowline (assuming a flow model). These studies clearly demonstrated an inherent complication in the calculation of ⁴He model ages in groundwater that had yet to be specifically identified, although Heaton (1984) [538] did note that an external flux of ⁴He from below the aquifer could be an important source.

8.5.2. Simple open system aquifer models

In a study of the Great Artesian Basin in Australia, Torgersen and Clarke (1985) [293], and Torgersen and Ivey (1985) [93] had the good fortune of evaluating a well defined system with existing and available hydraulic ages (flow model ages based on Darcy's law), ¹⁴C model ages and ³⁶Cl model ages (Airey et al. (1983) [363]; Airey et al. (1979) [578]; Bentley et al. (1986) [301]). After evaluating local ⁴He production and its downflow variability via ²²²Rn, in situ U–Th-series abundances and possible sources via weathering release from the solid phase, Torgersen and Clarke (1985) [293] concluded ⁴He in the Great Artesian Basin must have a dominant external source from outside (below) the aquifer. A key component in this analysis is that simple local-source-only ⁴He concentrations agree with ¹⁴C model ages and hydraulic flow model ages for timescales less than 40 ka. Yet, for longer timescales, ⁴He concentrations exceed the local-source-only production rate is likely to be constant throughout the aquifer without large scale variation and this was confirmed with ²²²Rn analyses (Torgersen and Clarke (1985) [293]). Torgersen and Ivey (1985) [93] used a simple, piston flow, 2-D model adapted from Carslaw and Jaeger (1959) [539] which included a 2-D aquifer of uniform vertical diffusion and uniform horizontal velocity:

$$v_{x}\frac{\partial C}{\partial x} = D_{z}\frac{\partial^{2}C}{\partial z^{2}} + I$$
(8.21)

With v_x , D_z and *I* constant, a constant flux across the bottom boundary and zero flux across the top boundary, Torgersen and Ivey (1985) [93] were able to evaluate the variability of ⁴He as a tracer of groundwater processes rather than as a groundwater dating methodology. They demonstrated that the change in the apparent rate of ⁴He accumulation with time/distance along the aquifer was related to the time needed to diffuse a bottom boundary flux vertically through the aquifer. Secondly, they were able to demonstrate that the external bottom flux dominated the sources of ⁴He at long timescales. Although the simple model (Torgersen and Ivey (1985) [93]) did not allow a loss term for the ⁴He flux out the top of the aquifer, their analysis shows that such a flux would be minimal on the timescale of the Great Artesian Basin system. Their analysis proceeded to evaluate simply the parameter sensitivity of the tracer flow model (from Carslaw and Jaeger (1959) [539]) by evaluating the sensitivity of the ⁴He measures obtained with regard to relative depth within the aquifer, aquifer thickness, aquifer porosity and the vertical rate of diffusion/dispersion. The model was also applied to the Aoub sandstone data of Heaton (1981) [210], which was much thinner and much younger and allowed a sensitivity analysis of the impact of the bottom boundary input flux. Castro et al. (2000) [88] ultimately re-sampled and re-evaluated the (Stampriet) Auob aquifer (Heaton (1981) [210]; Heaton (1984) [538]), and obtained a bottom boundary ⁴He flux ~2 times larger than estimated by Torgersen and Ivey (1985) [93]. Castro et al. (2000) [88] additionally quantified the Carrizo aquifer in Texas and the Ojo Alamo and Nacimiento aquifers (San Juan Basin, NM). These crustal fluxes are reported in Table 8.2. Torgersen et al. (1989) [573] showed that the accumulation of ⁴⁰Ar_{rad} from an external bottom boundary flux of ⁴⁰Ar_{rad} in the Great Artesian Basin system also dominated in situ production of ⁴⁰Ar_{rad} in the aquifer. The key contribution of these papers is the transition from a theoretical calculation of a ⁴He model age to the incorporation of ⁴He into simplified groundwater flow models as a component subject to reaction and transport in the groundwater systems. As such, ⁴He allows finer scale tuning of knowledge about transport, mixing, sources and sinks to/in aquifer systems. The disadvantage is that some prior knowledge about the structure of the aquifer system is required.

Stute et al. (1992) [561] used a 2-D model of flow in the Great Hungarian Plain with a bottom boundary flux equivalent to 0.25 times the value of Torgersen and Ivey (1985) [93]; equivalent to whole crustal production, but allowing flux out of the top boundary. Fitting the observed ⁴He and ³He concentrations to the 2-D model, Stute et al. (1992) [561] were able to constrain vertical flow velocities in this aquifer system and provide an estimate of groundwater turnover in the system to be of the order of 10^5 a. An important contribution of this work is the ability to examine the discharge region of an aquifer system in terms of the Peclet number $(\Delta z v_z/D_z)$ which defines the basic transport of the system. Castro et al. (2000) [88] further evaluated the model of Torgersen and Ivey (1985) [93] for the Carrizo aquifer system and verified the basic assumptions of the system, including the assumption of a topmost no-flux boundary. Although emphasizing that fluxes across boundaries can be the result of advection, dispersion and diffusion, they concluded that many systems are sufficiently young or short to operate as if there were no flux across the top boundary. The corollary to this observation is that ⁴He fluxes measured at the land surface will be highly variable; for such an aquifer, the flux leaving the ground surface to the atmosphere will be very low, while the ⁴He flux to the atmosphere at the discharge zone will be very high. The transport properties and mechanisms of the continental crust dictate a high degree of spatial variability.

8.5.3. Helium-4 as a component in groundwater flow models evolves

Fritzel (1996) [575] and Zhao et al. (1998) [98] inserted ⁴He (and ³He) within established groundwater flow models (Bethke et al. (1993) [579]). Zhao et al. (1998) [98] show (Fig. 8.12) that for a base case (in situ production plus a large basal bottom flux; Fig. 8.12.2), ⁴He in the vertical section of the aquifer increases from the top to the bottom, reflecting the importance of the basal flux. However, for the exemplar case in which the bottom boundary flux is insignificant (Fig. 8.12.3), the ⁴He concentration in the aquifer increases from the top to the bottom, reflecting the importance of 'old water' in the upper confining shale as a source of high ⁴He concentration. The Zhao et al. (1998) [98] examination of an irregular basal flux (Fig. 8.12.4) shows that if ⁴He basal flux is confined to an area one tenth of the original and is ten times the original, then ⁴He decreases downstream of the basal flux region as a result of hydrodynamic dispersion and mixing. As shown by both Torgersen and Ivey (1985) [93], and Zhao et al. (1998) [98], increasing the vertical rate of dispersion/mixing results in a shorter period of local in situ production dominance, less vertical variation and a system dominated by horizontal variability over vertical variability (Fig. 8.12.5). Zhao et al. (1998) [98] also evaluate the impact of subregional flow cells induced by basin topography as a control on aquifer ⁴He distribution (Fig. 8.12.6). These studies show how the quantification of large scale average aquifer transport properties can be fine-tuned with the inclusion of ⁴He in reaction and transport models, even under conditions where the details of the basal flux variability may not be explicitly defined.

In relation to Fig. 8.12, the utilization of He data for quantification of groundwater flow requires consideration of the aspects listed below. It should be noted that in all cases in the figure, the (a) panel shows ⁴He concentrations in units of 10^{-5} cm³ STP ⁴He/cm³_{H2O} while the (b) panel shows the ³He/⁴He ratio in units of 10^{-8} .

- Fig. 8.12.1: The conceptual model for numerical simulations is as follows: 1000 km basin with a basin tilt of 0.7 km/1000 km and an aquifer thickness of 1 km.
- Fig. 8.12.2: The base case scenario proscribed with a basal flux from Torgersen and Ivey (1985) [93] shows (Fig. 8.12.2(a)) an increase in ⁴He along flowlines and from the top to the bottom of the aquifer. Figure 8.12.2(b) shows a decrease in the ³He/⁴He ratio downstream that is the result of both in situ dilution of the air-saturated initial condition with in situ production as well as the basal flux which has been set to have a greater ³He/⁴He ratio than in situ production.
- Fig. 8.12.3: The condition where the basal flux is zero shows (Fig. 8.12.3(a)) the ⁴He concentration decreasing with increasing depth in the aquifer as a result of input from the overlying shale aquitard and (Fig. 8.12.3(b)) a lower ³He/⁴He ratio resulting from the lower in situ production ratio.
- Fig. 8.12.4: The condition where the basal flux is highly localized (one tenth of the area but at ten times the flux). Fig. 8.12.4(a) shows that the localized basal flux is significantly diluted downstream by dispersion.
- Fig. 8.12.5: The variability of the ⁴He concentration as a result of different dispersivities (Fig. 8.12.5(a)) used assumes no mechanical dispersion (Fig. 8.12.5(b)), and shows the condition for a longitudinal dispersivity of 100 m and transverse dispersivity of 10 m. It should be noted that Fig. 8.12.2(a) shows the intermediate case of longitudinal dispersivity of 10 m and a transverse dispersivity of 1 m.



FIG. 8.12. The utilization of He data in the quantification of groundwater flow and transport problems (from Zhao et al. (1998) [98]) in the Great Artesian Basin, Australia.

- Fig. 8.12.6: The variability of ⁴He under the influence of subregional flow cells is imposed by regional topography.
- Fig. 8.12.7: A comparison of the ⁴He concentrations along the top of the aquifer and the bottom of the aquifer is shown for each illustrated case. It should be noted that all cases show a general increase with distance but that variability along the flow path can be identified with specific cause/effect hypotheses that are model testable.

Unless otherwise specified, the model is defined with:						
Aquifer length	1000 km					
Aquifer thickness	1 km					
Topographic slope	700 m/1000 km					
Permeability sandstone	$1 \ \mu m^2$					
Permeability shale	$5 imes 10^{-5}\ \mu m^2$					
Dispersivity longitudinal	10 m					
Dispersivity transverse	1 m					
Diffusion coefficient	$3 \times 10^3 \text{ cm}^2/\text{a}$					
In situ production of ⁴ He, sandstone	$3.07 \times 10^{-13} \text{ cm}^3 \text{ STP }^4 \text{He} \cdot \text{cm}^{-3}_{\text{H2O}} \cdot \text{a}^{-1}$					
In situ production of ⁴ He, shale	$8.78 \times 10^{-12} \text{ cm}^3 \text{ STP }^4\text{He} \cdot \text{cm}^{-3}_{\text{H2O}} \cdot a^{-1}$					
Basal flux	$0.14 \times 10^{-5} \text{ cm}^3 \text{ STP }^4\text{He} \cdot \text{cm}^{-2}_{\text{tot}} \cdot \text{a}^{-1}$					
³ He/ ⁴ He meteoric recharge	138.6×10^{-8}					
³ He/ ⁴ He production in sandstone	$1.80 imes 10^{-8}$					
³ He/ ⁴ He production in shale	$1.85 imes 10^{-8}$					
³ He/ ⁴ He of basal flux	3.5×10^{-8}					

Bethke et al. (1999) [95] re-evaluated the ⁴He data of Torgersen and Clarke (1985) [93] with the helium capabilities of the enhanced basin flow model (Bethke et al. (1993) [579]). They show that ⁴He measurements obtained in the upper 20% of the aquifer vertical section are controlled not only by the lateral flow (v_x) and the vertical mixing (D_z) of the basal flux up into the aquifer, but also by the vertical water velocity encountered in the recharge area and the discharge area, a subject that was also addressed in simpler form by Stute et al. (1992) [561]. Such dependency is not discernable in the simplistic model of, for example, Torgersen and Ivey (1985) [93] because it is based on a piston flow concept. Significantly, Bethke et al. (1999) [95] were able to address the high concentrations and variability of ⁴He in this Great Artesian Basin aquifer system without resorting to stagnant zones (Mazor (1995) [580]). This did much to reconcile the geochemical concepts of ⁴He inputs, sources and accumulation with established concepts of flow in large aquifer systems. Bethke et al. (2000) [94] combined the use of ³⁶Cl and ⁴He to conclude that isotope distributions can be used to obtain internally consistent descriptions of deep groundwater flow directions and rates.

Castro et al. (1998) [96] and Castro et al. (1998) [97] used a finite element code model of transport in the Paris Basin (Wei et al. (1990) [581]), with multiple aquifers arranged vertically. Within this study, Castro et al. (1998) [96] and Castro et al. (1998) [97] examined the vertical flux of not only ⁴He and ³He but also ⁴⁰Ar_{rad} and ²¹Ne. This study demonstrated the potential for diffusive separation of noble gases as they are transported across various aquitards in the system (very small Peclet numbers). While this analysis is not disputed here, Castro et al. (1998) [96] admit that the model is extremely sensitive to parameter variations, in particular to changes in flow rate and permeability. Given the degree of structural complexity in the model, the sheer number and spatial variability of parameters that control water flow and noble gas transport, together with the relatively few noble gas measures and aquifer transport parameter measures from the Paris Basin, the question is raised as to whether the conclusion (diffusion controlled separation of ⁴He and ⁴⁰Ar_{rad}) is unique. Sensitivity to parameter choice/variability is an important constraint in modelling and the tests run by Zhao et al. (1998) [98] (see Fig. 8.12) and Bethke et al. (2000) [94] provide for greater interpretation around the conclusions. The study of Castro and Goblet (2003) [89] in the Carrizo aquifer system suggests that ⁴He can and often does constrain the conceptual transport model for the aquifer system as only one of five conceptual models of the Carrizo successfully captured the ⁴He distributions that had been measured. Berger (2008) [92], reported in Bethke and Johnson (2008) [84], used the Paris Basin model and optimized the flow field with constraints provided by ⁴He, head, salinity and temperature.

Bethke and Johnson (2008) [84] discuss in detail the use of ⁴He, ³⁶Cl, etc. as tracers in groundwater modelling, and assimilate a rigorous definition of groundwater age. The concept of groundwater age incorporates many complexities, as discussed in Chapter 3, because groundwater flow systems are subject to: (i) lateral dispersion/diffusion; (ii) vertical groundwater velocity distributions resulting from recharge area downflow and discharge area upflow; and (iii) convergence and divergence of streamlines. The interpretation of, for example, a ⁴He model age as an idealized groundwater age is, thus, specific and limited. The most important of the groundwater flow field complexities is the mixing of water parcels. Such issues of groundwater mixing are well established in short timescale groundwater flow where multiple tracers (³H–³He, CFC, bomb ¹⁴C, etc.) are often used to quantify both v_x and D_x in a 1-D system (Ekwurzel et al. (1994) [582]; Plummer et al. (2004) [50]). This is possible because the input function for ³H is much different to, for example, the input function for CFCs, and a comparison of the distribution of both tracers enables the quantification of two controlling parameters. In very old groundwater systems, the viable groundwater 'dating' methods are ¹⁴C, ⁴He, ⁸¹Kr and ³⁶Cl. Since ⁴He is typically controlled by (i) an internal production of ⁴He that is often constant and (ii) a large external flux that may be assumed to be constant, the use of combined dating methods of, for example, ⁴He and ³⁶Cl (with its exponential decay control) provides a powerful means by which to constrain the parameter values describing flow and mixing in aquifer systems, although model optimization with other tracers including temperature (Berger (2008) [92]) are possible and enlightening.

8.5.4. Summary

The concept of using ⁴He to derive an idealized groundwater age has largely been abandoned in favour of the use of ⁴He (other noble gas isotopes, ³⁶Cl and ⁸¹Kr) as a component in groundwater reaction and transport models to constrain the complexity of transport in specific aquifers. The inclusion of ⁴He in standard groundwater transport models has the ability to constrain the fundamental aquifer flow conceptualization as well as to refine the quantification of the controlling flow parameter values and their distribution. Building such conceptual transport models of aquifer systems requires some degree of foreknowledge about the basic aquifer structure, the general transport properties of the structure (hydraulic conductivity of the aquitards versus hydraulic conductivity of the aquifer) as well as the in situ ⁴He production (concentration of U–Th and porosity) of the basin structural components. In such cases, the use of ⁴He and adequate samples of ⁴He across the groundwater flow system can provide significant constraints on flow. Still to be addressed, however, are systems for which little structural information is known and for which the basic parameters controlling flow are poorly known in space/

8.6. CONCEPTUAL ⁴He TRACER AGES AS A CONSTRAINT ON GROUNDWATER AGE

The material presented above shows the simple concept of ⁴He model ages as a proxy for idealized groundwater age is likely inapplicable in most systems. This does not negate the value of ⁴He tracer applications, but it does imply that the physical meaning of the ⁴He model age must be evaluated. Simple ⁴He model age calculations in the idealized 1-D system (piston flow and vertical gradients of ⁴He as a result of bottom flux) demonstrate that direct comparison of 1-D piston flow model ages and

⁴He model ages is inappropriate at best. Furthermore, the possibility that a bottom boundary flux could also be lost out of the top of the control volume further indicates that the ⁴He model age calculated is applicable only to ⁴He and that it has no parallel in groundwater flow.

The calculation of a ⁴He model age, in most cases, will involve the amount of ⁴He in a control volume (atoms/m³) as well as fluxes (atoms \cdot m⁻² \cdot s⁻¹) across boundaries of that control volume. This necessitates the definition of a layer thickness to which the ⁴He concentration measures apply. Even if one can obtain closely spaced ⁴He concentrations to define a gradient, one would be pressed to define whether the influx across the bottom boundary were advection controlled or diffusion controlled, and knowledge of v_z and/or D_z would require additional knowledge about the aquifer structure, its composition and its transport properties. The calculation of ⁴He model age as a proxy for groundwater age, thus, becomes a geochemical 'artform'.

Calculations of the ⁴He model age are more specifically generalized as:

$$\tau_{\rm He} = \left[{}^{4} \text{He}\right] \left(\Lambda_{4} J'_{\rm He} \rho_{\rm rock} \frac{1 - \Phi}{\Phi} + \frac{\Sigma F_{\rm He}}{\rho_{\rm H20} \Phi z} \right)^{-1}$$
(8.22)

where

 J'_{He} is the internal rate of ⁴He production from U–Th series decay (Eqs (8.6, 8.7));

 $\rho_{\rm rock}$ is rock density;

 $\rho_{\rm H2O}$ is water density;

 Φ is porosity;

 ΣF_{He} are the boundary fluxes of ⁴He into/out-of the system (atoms $\cdot \text{ m}^{-2} \cdot \text{a}^{-1}$) of thickness z (m).

The first term in Eq. (8.22) bracket represents the local source of ⁴He as a result of local U–Th series element decay and the second term in the same equation represents the external flux to the system across a (bottom) boundary. The 'artform' comes not only in choosing Λ_{He} , F_{He} and z but also in explicitly defining meaning for τ_{He} in relation to a ⁴He model age and an idealized groundwater age. One example is the case where the vertical flux through the system has reached a steady state and the flux into the bottom is equal to the flux out of the top. ΣF_{He} for this case is zero but the concentration in the vertical position is linearly variable, giving linearly variable ⁴He model ages in the vertical. The loss terms will be specifically avoided in the following analysis for this reason. Nonetheless, the concept of a ⁴He model age calculation is worth exploring in unique opportunities.

8.6.1. Helium-4 fluxes determined by vertical borehole variation in ³He/⁴He

Sano et al. (1986) [583] examined natural gas wells in Taiwan and identified a ³He/⁴He ratio that decreased as samples approached the surface. This scenario can be modelled if the base of the system is 'tagged' with a mantle ³He (³He/⁴He ~ 10⁻⁵) signature, the system is vertically controlled and in situ production by radioactive decay of U–Th series elements in the layer (thickness = z_i) between measures supplies an input of crustal He of known ratio (³He/⁴He ~ 10⁻⁸) that dilutes the mantle ³He flux with crustal production as it is transported vertically in the rock column. For a horizontally homogeneous system with both a ³He enriched component at depth and an in situ production of helium, the flux of helium from the top of the layer (F_1) is (generalized from Sano et al. (1986) [583]):

$$F_{1} = \frac{P_{i}z_{i}(R_{2} - R_{i})}{(R_{2} - R_{i})}$$
(8.23)

and the flux into the bottom of a layer (F_2) is:

$$F_2 = \frac{P_i z_i (R_1 - R_i)}{(R_2 - R_1)}$$
(8.24)

where	
$P_{\rm i}$	is the production rate of ⁴ He;
R_1 and R_2	are the isotopic ratios of ³ He/ ⁴ He at the top and bottom of the layer, respectively;
$R_{\rm i}$	is the production ratio of ³ He/ ⁴ He in the layer;
Zi	is the thickness of a layer.

If the system contains multiple layers with differing rates of in situ production, the appropriate equations are:

$$F_{1} = \frac{\sum P_{i} z_{i} R_{i} - \left[\sum P_{i} z_{i}\right] R_{2}}{(R_{1} - R_{2})}$$
(8.25)

and

$$F_2 = F_1 - \Sigma P_i z_i \tag{8.26}$$

where $P_{i}z_{i}$ is the in situ production of individual layers between the surfaces defining F_{1} and F_{2} .

Using Eqs (8.23) and (8.24), Sano et al. (1986) [583] quantified the fluxes of ⁴He in two Taiwan natural gas fields to be 2.7 0.6×10^{10} atoms ⁴He \cdot m⁻² \cdot s⁻¹ and 2.4 \pm 0.8 $\times 10^{10}$ atoms ⁴He \cdot m⁻² \cdot s⁻¹ (Table 8.2). These continental degassing fluxes are in agreement with measures from the Great Artesian Basin (Torgersen and Clarke (1985) [293]; Torgersen and Ivey (1985) [93]) and the atmospheric mass balance (Torgersen (1989) [546]), and could have been used to calculate apparent ⁴He model ages as per Eq. (8.22). Torgersen and Marty (unpublished data)¹ applied such relations to the Paris Basin and obtained ages that were roughly ten times larger for the Dogger aquifer than were obtained by Castro et al. (1998) [96] and Castro et al. (1998) [97] using a full scale hydrological flow model. These results suggest that although the mathematics of the approach is appealing, the underlying assumptions are likely too restrictive to apply to the general case. It would be interesting to apply Eqs (8.23–8.26) to modelled results of Zhao et al. (1998) [98], for example, to determine when/whether these simple relations have meaning.

8.6.2. Cajon Pass

Torgersen and Clarke (1992) [294] evaluated the ⁴He model age for waters collected in the Cajon Pass scientific drillhole to constrain groundwater flow and heat transport in and around the San Andreas Fault. Samples were collected with a downhole sampler (Solbau et al. (1986) [505]) after the drillhole had been given over wholly to fluid inflow during a prolonged period of no drilling (due to lack of funds). The drillhole was pumped and the water remaining was spiked with fluorescein to differentiate contaminant water from fracture water inflow. Specific intervals were packed-off to define layers of fracture water inflow that were allowed to accumulate over periods of months. Careful sampling enabled some vertical structure in the inflow water to be defined but the evaluation of ⁴He tracer model ages was based on bulk concentrations of the fluorescein (contaminate)-corrected inflow water ⁴He concentration.

CASE (1) calculations in Torgersen and Clarke (1992) [294] assumed $F_{\text{He}} = 0$, used a Λ_{He} value quantified by the ²²²Rn concentration after the method of Torgersen (1980) [535] and calculated the source function from U–Th series decay (J'_{He}) from estimated rock composition. The resultant apparent ⁴He model age was 0.9–5 Ma which implies a vertical fluid velocity of 0.04–0.2 cm/a ($v = \Delta z / \Delta t$ where $\Delta z = 2000$ m). CASE (2) calculations in Torgersen and Clarke (1992) [294] assumed a release factor of $\Lambda_{\text{He}} = 1$. The resultant ⁴He model age was 33–330 ka, implying a vertical fluid velocity

¹ TORGERSEN, T., Marine Sciences, University of Connecticut, MARTY, B., Centre de Recherches Pétrographiques et Géochimiques, Nancy, unpublished data.

of 0.6–6 cm/a. They further evaluated the possibility of a non-steady state source (loss of 4 He as a result of fracturing (Torgersen and O'Donnell (1991) [543])) which possibly mimics the $\Lambda_{\text{He}} > 1$ defined by Solomon et al. (1996) [295] and concluded that $\Lambda_{\text{He}} = 1$ was a good approximation. This gives a range for the vertical fluid velocity of 0.04-6 cm/a. CASE (3) is added to their analysis, where it is assumed that the accumulation of ⁴He in the Cajon Pass groundwater was dominated by the crustal degassing flux. Assuming an externally imposed degassing flux equivalent to the whole crustal production and assuming the concentration measured at ~ 2000 m applies to the whole layer from 0–2000 m depth, a ⁴He model age of 1667 a would be calculated, giving a vertical fluid velocity of 120 cm/a. Torgersen and Clarke (1992) [294] show that excess heat generated by fault zone friction is not significantly removed by vertical fluid flow estimate for CASE (1), demonstrating that the San Andreas Fault system is likely a low strength/low coefficient of friction system. Furthermore, the vertical fluid velocity estimated from ⁴He model ages was compared to drillhole well tests that estimate vertical fluid velocities of 10^{-5} cm/a. If one assumes that both quantifications represent reality but over different timescales (the drillstem test provides an estimate of fluid velocity on the timescale of months for a space equivalent to the open hole section; and the ⁴He tracer age based velocity is applicable over the residence time (tracer age) and the 2000 m depth of the sample), then the comparison suggests that fluid transport is episodic with short intervals of rapid fluid transport and longer timescales of very slow fluid transport. Such a conclusion is in agreement with metamorphic geology literature and the mechanisms of fluid transport suggested by Nur and Walder (1990) [584]. Adding CASE (3) does not change the conclusion with regard to episodic transport but it does enable hydrothermal heat flow (estimated to be $<65-130 \text{ W/m}^2$) to remove any fault zone generated heat (estimated to be <85-90 W/m²) if such a vertical fluid transport rate can be verified. Thus, the principles of ⁴He model age calculations can be applied to constrain systems for which little information is available.

8.6.3. South African ultra-deep mine waters

Lippmann et al. (2003) [568] evaluated the noble gas isotope composition of groundwaters collected from seeps in the ultradeep mines of South Africa. They calculated noble gas tracer ages based on ⁴He, ⁴⁰Ar_{rad}, ¹³⁴Xe and ¹³⁸Xe on the basis of the generalization of Eq. (8.22) from ⁴He to other noble gases. Scenario 1 calculations were based on in situ local-only sources of noble gas isotopes $(\Sigma F_{\text{He}} = 0)$ with an assumed $\Lambda_{\text{He}} = 1$ and $\Lambda_{\text{Ar}} = 1$. For Xe isotopes, $0.1 < \Lambda_{\text{Xe}} < 0.5$ was artfully fit based upon a much smaller recoil distance involved in the fissionogenic production of these isotopes. Scenario 2 includes the possibility of a whole crustal production degassing flux ($F_{\rm He} = 8 \times 10^9$ atoms ⁴He \cdot cm⁻² \cdot s⁻¹; see Table 8.2) applicable over the layer from the surface to the depth of sampling. Their calculations indicate noble gas tracer model ages on the order of 10-100 Ma (scenario 1) and 0.1-20 Ma (scenario 2). Given that ³⁶Cl measures in the same water indicate ³⁶Cl model ages in excess of 1.5 Ma, the noble gas estimated ranges for tracer age can be used as a zeroth order estimate of the idealized groundwater age. The vertical fluid velocities estimated (sample depth is of the order of 2000–3000 m) from these noble gas tracer ages are 0.003–0.02 cm/a which are consistent with hydraulic conductivity in tight rock (Freeze and Cherry (1979) [11]; unfractured metamorphic and igneous rocks assuming hydrostatic gradients) as well as in situ measures of vertical transport rates at the Cajon Pass, California (Coyle and Zoback (1988) [585]; Torgersen and Clarke (1992) [294]).

8.6.4. Deep borehole sampling

Osenbrück (1996) [514] explored a new sampling method for deep borehole rock in which either inflow of water was minimal and/or the restrictions of the drilling schedule/cost were such that direct groundwater sampling was not feasible. The method (Osenbrück (1996) [514]) depends upon the relatively slow diffusion of noble gases in the matrix pore fluids of intact rock (hours) to enable

rock sampling (drillcore retrieval) that preserves noble gas concentrations from matrix pore fluids recovered from depth. The principle assumption is that matrix pore fluids are equivalent to fracture filling pore fluids which are likely the major mode of transport. In a typical sampling operation, drillcore is recovered at the surface within hours of being cut and intact rock is subcored to avoid rock on the exterior of the drillcore that had already been microfractured and had begun to release pore fluids. The subcored rock is then introduced into a vacuum container, purged of air and left either under low N₂ pressure or vacuum for an extended period of time. The natural relaxation of the rock then causes expansion, dilatation and draining of pore fluids into the sealed container. The container may be maintained at room temperature or at elevated temperatures (e.g. equivalent to in situ temperatures) to increase the diffusivity in water and, thus, speed the release of pore fluid to the container (Ali et al. (2008) [586]; Ali et al. (2010) [513]). Opening the container to the mass spectrometer will then enable measures of the amount of water released as well as the noble gases contained in those pore fluids.

Using the method of Osenbrück (1996) [514] to obtain pore fluid samples, Osenbrück et al. (1998) [515] explored the tracer model ages in a potential nuclear waste repository in Morsleben, Germany. Their results show a profile of ⁴He in pore fluids that is consistent with vertical diffusive transport in a horizontally homogeneous system. They assume that transport occurs at a rate determined by tortuosity- and porosity-corrected molecular diffusivity, and calculate a diffusion coefficient of $D = 2 \times 10^{-6}$ cm²/s. Using this diffusion coefficient and the measured gradient in pore fluid ⁴He concentration, they calculate a vertical flux of 2×10^{-7} cm³ STP ⁴He \cdot cm⁻² \cdot a⁻¹ which is in agreement with other measured fluxes (see Table 8.2). Using the characteristic timescale for such a steady state profile to be obtained (from Carslaw and Jaeger (1959) [539]):



FIG. 8.13. The release fraction, Λ_{Ng} , as determined from whole rock samples recovered from the German Continental Deep Drilling programme borehole (Drescher et al. (1998) [569]). The results represent an analysis of rock and the results confirm the general trend of $\Lambda_{He} > \Lambda_{Ne} > \Lambda_{Ar} > \Lambda_{Xe}$ as would be expected from their respective diffusion coefficients in the solid phase. (From Drescher et al. (1998) [569].)

$$\tau = 4 \frac{\Delta x^2}{\pi^2 D} \tag{8.27}$$

they calculate a lower limit on the pore water age of 6 Ma. Here, the tracer model age based on the ⁴He concentration and the sum of the in situ production and the crustal flux can be calculated for comparison. For depths of 300–700 m, where ⁴He is approximately constant at 4×10^{-4} ccSTP ⁴He/g_{H20}, the tracer model age is given by Eq. (8.22). The data of Osenbrück et al. (1998) [515] yield 7.5 Ma using the calculation of the local crustal flux (which is circular reasoning) or 4.3 Ma if the local ⁴He crustal flux is equivalent to the whole crustal production as estimated from the measures in Table 8.2.

The Osenbrück (1996) [514] methodology for sampling pore fluids opens the more general case for dating deep borehole pore fluids. Drescher et al. (1998) [569] collected deep borehole rock samples from the German Continental Deep Drilling (KTB) programme (depths from 100–9000 m) and measured the solid phase concentration of ⁴He, ⁴⁰Ar_{rad}, ²¹Ne, ^{84,86}Kr and ^{134,136}Xe. These are converted to an effective noble gas tracer model age of the rock which can be compared to the metamorphic age of the rock as determined by, for example, ⁸⁷Sr/⁸⁶Sr, ⁴⁰Ar_{rad}/K and/or other dating methods. The release fraction for each noble gas to the pore fluid can then be quantified as (Drescher et al. (1998) [569]):

$$\Lambda_{\rm Ng}^{\rm meas} = 1 - \frac{\tau_{\rm Ng}^{\rm nock}}{\tau_{\rm meta}}$$
(8.28)

Direct measurements and Eq. (8.28) (Drescher et al. (1998) [569]) indicate the release factor from the KTB borehole rock to be $\Lambda_{\text{He}} = 0.88 \pm 0.11$ (Fig. 8.13), which is in agreement with the generally assumed value of $\Lambda_{\text{He}} = 1.0$. Similar values can be obtained from the case study of Tolstikhin et al. (1996) [559]. Assuming the rock samples of Drescher et al. (1998) [569] are representative of the crust, they imply a crustal flux of 0.88 times whole crustal production with similar estimates for ²¹Ne, ⁴⁰Ar_{rad} and ¹³⁶Xe (Fig. 8.13). It should be noted that the depth at which these samples were collected removes a significant fraction of the crust as a contributor to the net crustal flux. The approach can be further generalized.

These simple measures of τ_{rock} need to be corrected for the time necessary to establish a gradient through which to diffuse the in situ production. τ_{rock} , therefore, establishes a minimum constraint on the true value of Λ_{He} and a best estimate for Λ_{He} might be:

$$1 - \frac{\tau_{\text{Ng}}^{\text{rock}}}{\tau_{\text{meta}}} < \Lambda_{\text{Ng}}^{\text{meas}} < 1 - \frac{\tau_{\text{Ng}}^{\text{rock}} - \Delta x^2 / D_{He}}{\tau_{\text{meta}}} = \frac{\tau_{\text{corr-Ng}}^{\text{rock}}}{\tau_{\text{meta}}}$$
(8.29)

where

 Δx is the effective grain size;

 D_{He} is the diffusion coefficient of He in the grain.

Since $D_{\text{He}} > D_{\text{Ne}} > D_{\text{Ar}} > D_{\text{Xe}}$, the correction will be relatively more important for the heavier noble gases.

Drescher et al. (1998) [569] were unable to collect pore fluid samples from the KTB by the method of Osenbrück et al. (1998) [515], but this analysis can proceed in the theoretical sense. Parts of this analysis are applied to Ali et al. (2010) [513]. Any one sample obtained at depth can be evaluated with respect to local or external sources with measures of $[Ng]_{H2O}$ and $[Ng]_{rock}$, and a metamorphic age of the rock. If it is assumed that the sample operated as a closed system, then conservation of mass indicates that:

$$[Ng]_{rock} \cdot (1-\Phi) + [Ng]_{H20} \cdot \Phi = J_{internal} \cdot \rho \cdot \tau_{meta} (1-\Phi)$$
(8.30)

and all (for example) ⁴He produced in the metamorphic age of the rock (at which time it was assumed that ⁴He was initialized to zero) is contained in either the rock or the pore fluid. Rearranging Eq. (8.30) and including the internal production from the solid phase with regard to the release fraction gives:

$$\frac{[\mathrm{Ng}]_{\mathrm{rock}}}{J_{\mathrm{internal}} \cdot \rho} + \frac{[\mathrm{Ng}]_{\mathrm{H2O}}}{\Lambda_{\mathrm{Ng}} J_{\mathrm{internal}} \cdot \rho} \cdot \frac{\Phi}{(1 - \Phi)} = \tau_{\mathrm{meta}}$$
(8.31)

or:

$$\tau_{\rm rock} + \tau'_{\rm H20} \Lambda_{\rm Ng} = \tau_{\rm meta} \tag{8.32(a)}$$

where τ'_{H2O} is the ⁴He tracer model age in the water calculated with the assumption that (Eq. (8.22)) $F_{He} = 0$ and the appropriate solution should be bracketed by corrected (Eq. (8.29)) and uncorrected values of τ_{rock} . Thus, for the closed system sample volume, $\Delta x \Delta y \Delta z$, for example, the helium age of the rock (τ_{rock}) plus a portion (Λ_{He}) of the ⁴He tracer model age in the fluid (τ'_{H2O}) is equal to the metamorphic age of the rock (as determined by ⁴⁰Ar and/or ⁸⁷Sr/⁸⁶Sr dating of specific mineral separates). Clear indications of an open system with respect to, for example, ⁴He in the volume $\Delta x \Delta y \Delta z$, but with distinctly different meanings, are expressed as:

$$\tau_{\text{rock}} + \tau'_{\text{H20}} \Lambda_{\text{Ng}} < \tau_{\text{meta}}$$
 open system, 'no' external source (8.32(b))

$$\tau_{\text{rock}} + \tau'_{\text{H2O}} \Lambda_{\text{Ng}} > \tau_{\text{meta}}$$
 open system, significant external source (8.32(c))

For the inequality expressed by Eq. (8.32(b)), there has been a net loss of Ng from the local crustal volume $\Delta x \Delta y \Delta z$. The most likely means to lose ⁴He (or ⁴⁰Ar) is by transport in the fluid phase. Thus, τ'_{H2O} (Eq. (8.22) with the assumption $F_{He} = 0$) provides a first order estimate of the age of fluids within the matrix porosity in the sample and the tracer model age. With the assumption that matrix pore fluids have equilibrated in situ with the fracture-filling and transporting pore fluids, the Ng tracer model ages and the transport in the deep crust can be estimated.

For the inequality expressed by Eq. (8.32(c)), there is a clear indication of an external source of noble gas to the system (or noble gas enrichment due to phase separation and re-dissolution which must be handled in an alternative manner). Again, the mechanism of transport is most likely to be via the fluid phase in fractures and, as was seen above, the first order estimate of the external flux is 3.63×10^{10} ⁴He atoms \cdot m⁻² \cdot s⁻¹ with a variability of 36 times. The methods discussed in this section are actively being applied for samples recovered from the San Andreas Fault Observatory at Depth (Ali et al. (2008) [586]; Ali et al. (2010) [513]; Stute et al. (2007) [587]).

8.6.5. Summary

The application of ⁴He model ages in groundwater as a proxy for the idealized groundwater age and a method for groundwater 'dating' has proven to be difficult to apply but ultimately valuable. The most common complication is the dominance of external fluxes of noble gas which occurs as the result of small and large scale transport within the crust. Estimates of the crustal flux of ⁴He range from 0.03 to 36 times the total crustal in situ production and have been documented in a number of areas. It is to be appreciated that such crustal fluxes have associated with them a specific time and space scale. Furthermore, it is to be recognized that these fluxes are generally conceptualized as near-uniform over the basin in question. Hence, a flux into an aquifer may result in little vertical flux to layers above as well as a concentrated outflux at the discharge zone.

Over the past several decades, research has moved the application of ⁴He model ages from the case where individual samples might be 'datable' to the case where large suites of samples are utilized and

⁴He is incorporated as a constituent tracer in large scale reaction and transport models. Such models then optimize the groundwater transport parameters and the ⁴He tracer distributions relative to the various in situ production and crustal flux terms. However, the field has also enlightened the subject to the degree that open system methodologies for placing bounds on groundwater ages using ⁴He are possible and may be applicable. This is especially true in the field of deep borehole sampling where the number of samples is limited and samples are limited to vertical profiles.

Chapter 9

SYSTEM ANALYSIS USING MULTITRACER APPROACHES

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Previous chapters of this book (i) introduced the subject of dating 'old' groundwater (Chapter 1); (ii) reviewed information needs and approaches for refining conceptualization of flow in groundwater systems and how the aquifer properties can be constrained with geoscientific knowledge (Chapter 2); (iii) provided more detailed discussion of the concept of groundwater 'age' and its implications for groundwater systems (Chapter 3); and (iv) summarized approaches for estimating the age of old groundwater, based on measurements of chemical and isotopic environmental tracers in groundwater (¹⁴C, ⁸¹Kr, ³⁶Cl, ²³⁴U/²³⁸U and ⁴He), and the special strengths and problems connected with each of these methods (Chapters 4–8, respectively). The present chapter offers a qualitative or semi-quantitative step towards a synthesis of the information that the different tracers provide. It also offers some criteria that can be used to help assess the reliability of selected tracer data in evaluating tracer model ages from measurements of concentrations of multiple environmental tracers in the system. In most of the literature on isotope hydrology, the term 'apparent age' is used instead of 'tracer model age', and within this chapter the two terms are considered synonymous. This approach testing reliability of tracer data is only a first step and performs a black and white selection of the tracer data. Some consistency tests are performed, and for data passing these tests there is at least no obvious reason known that the tracer model age is not a valid description. For data that fail these tests, it is obvious that a straightforward calculation of tracer model ages will not give the intended result.

This enables the user to perform the following two steps: (i) find a description of the groundwater system which consistently describes all of the tracer model ages for those data that pass the test and (ii) find a system description which can explain the measured values for all (tracer) data. It should be noted that, during the second step, calculation of ages is no longer necessary. This chapter is complemented by the modelling chapter (Chapter 10), which presents a more detailed and quantitative approach to such a synthesis. Finally, four case studies are presented that demonstrate how the techniques in this book have been applied in actual groundwater systems.

In Chapter 3, there was discussion of some of the terminological and practical questions arising when a term such as 'age', with an obvious meaning for human beings, is applied to groundwater, where this meaning is by no means obvious. One of the statements was that for principal reasons it is impossible to deduce the exact shape of the frequency distribution of ages in a single sample. This remains true in general terms. However, this chapter presents some methods and approaches to constrain the age distribution when tracer data for many samples or data from multiple tracers (or ideally both) are available. For a single sample, this is achieved by excluding parts of the age distribution when combining the results for several tracers. For the aquifer as a whole, this is achieved by examining patterns in measured tracer concentrations in vertical profiles or along horizontal transects. This way, the tracer data can be tested against observations which are to be expected based on very simple hypothetical models of groundwater flow. It was also demonstrated in the introductory chapters how the conceptual model of groundwater flow is refined and evolves as new data, including environmental tracer data, are considered. This chapter presents some graphical methods that can test aspects of the conceptual model of groundwater flow.

As seen in Chapters 4–8, each tracer has weaknesses and every tracer needs to constrain parameters and assumptions to allow interpretation in terms of age of groundwater. Examples include:

(i) determination of the initial ¹⁴C content; (ii) estimating the strength and isotopic composition of external helium fluxes or internal helium production; (iii) accounting for the secular variations in the ³⁶Cl production, initial values of the ³⁶Cl/Cl ratio and underground production of ³⁶Cl. Therefore, another purpose of this chapter is to demonstrate how some of the necessary parameters for one tracer can be deduced by using other tracers.

This chapter uses some examples of groundwater flow for which the idealized groundwater age is described analytically by mathematical functions, and in all but one case the discussion is made without calculating an age from tracer data. The intention is to provide a toolbox for estimating hypothetical tracer patterns where tracer model ages are close to idealized ages and to distinguish these patterns from mixing scenarios where idealized ages and tracer model ages are very different and, consequently, the tracer model ages are not very meaningful. Utilizing data from a single tracer, the distinction between dominant advective flow and mixing cases is almost never possible, which is why, in this chapter, multiple tracers are considered in the same groundwater system.

9.1. VERTICAL PROFILES

Vertical profiles of tracer values in an aquifer system are among the most valuable data to understanding the flow system. As a general rule, discrete samples from well defined depths in a vertical profile can provide more insight into the flow system than samples taken along an assumed flowline or samples randomly selected over an aquifer system. However, samples from well defined depths in vertical profiles within an aquifer are often difficult to obtain. Although the number of multilevel well nests used in scientific studies is increasing, and although these wells are probably optimal in detailed aquifer studies, the number of vertical profiles that can be sampled is often limited. Therefore, most groundwater studies rely on sampling of 'wells of opportunity', that is, single wells, often with several screens or fracture zones within one borehole, or wells that are open to wide intervals of the aquifer, which may be all that are available. Sophisticated packer systems can be used to sample some wells with multiple completions. Other methods employ dual-valve bailers, and, for some gas tracers, chains of passive samplers have been used. There will be discussion on some of the effects of large-screen mixing to demonstrate how to identify mixed samples and why they are difficult to interpret, although they start with ideal sampling conditions.

As a general accepted geoscientific convention, depth profiles are always presented with depth increasing downwards along the y axis. The presentation in this chapter proceeds from simple to more complicated hydrological systems, starting with a very simple flow system in a homogeneous aquifer, continuing with a more complicated flow system in a homogeneous aquifer and finally discussing inhomogeneous cases.

9.1.1. Unconfined homogeneous aquifer

Although homogeneous phreatic (unconfined) aquifers with long travel times are uncommon and very often an oversimplification, this conceptual model presents a useful starting point for examining tracer patterns in aquifers. First, vertical profiles will be considered at one site and with two simple cases for which analytical solutions exist.

First, consider the hypothetical case where groundwater flow is purely vertical downward, with a constant speed, as might conceptually apply to infiltration at a groundwater divide in an unconfined homogeneous aquifer. On a small scale, this could be an infiltration area, and the downward movement could be caused by recharge. In this case, the distance velocity is the recharge rate divided by the aquifer porosity. Any tracer evolution with time will be translated into a tracer evolution with depth, as shown in Fig. 9.1. A radioactive tracer showing exponential decay with time, such as ¹⁴C (green line), will show exponential decrease with depth, a tracer with linear increase in time, such as ⁴He (red line), will



FIG. 9.1. Conversion of time evolution into a depth profile for the hypothetical case of purely downward vertical movement.

show a linear increase with depth, and any historical change in tracer concentration, such as the seasonal pattern of stable isotopes (blue) or the shift in stable isotopes and noble gas recharge temperatures at the last glaciation (black), will be translated into a corresponding depth pattern.

This simple conceptual construct is sometimes a valid approach for short timescales: seasonal variations in stable isotope signals are discernible after crossing several metres of unsaturated zone in the outflow of a lysimeter and can be used to age-date the water (Stumpp et al. (2009) [588]; Vitvar and Balderer (1997) [589]), and tritium depth profiles can show the historical record in precipitation over the past 50 a (Lin and Wei (2006) [590]). For long timescales, however, this approach is completely unrealistic, since the following simplifications are not valid:

- (a) On long timescales, the vertical downward movement changes into horizontal and later to upward movement, simply because with increasing depth there is not enough space for all of the groundwater.
- (b) Diffusion and dispersion will dampen any sharp transitions, such as the palaeoclimate signal, as well as the amplitude of any variations as discussed in Section 5.5.6. This is shown for the blue and black lines in Fig. 9.1.
- (c) Mixing of different groundwaters, infiltrated at different locations and times, will create new patterns which are an averaged combination of those in Fig. 9.1 for the corresponding point in time and the mixing ratio.

This chapter cannot discuss all of these effects in detail but will outline the impact of some of them. The first step is to consider the influence of the transition into horizontal groundwater movement if the aquifer depth is limited. Two analytical solutions exist for this problem.

9.1.1.1. The 'Vogel' aquifer

Vogel (1967) [137] described a simple homogeneous 2-D aquifer system and derived analytical solutions for the resulting frequency distribution of ages that can be used to calculate the resulting tracer depth profiles. The concept of the Vogel aquifer is illustrated in Fig. 9.2. The aquifer is assumed to have a rectangular vertical cross-section of thickness, L, to be of homogeneous transmissivity and homogeneous porosity Φ and to receive uniform recharge at a rate of R at the top. The left



FIG. 9.2. Geometry and boundary conditions of the Vogel aquifer.

and bottom boundaries are impervious, such that all recharge has to leave the flow system through the right boundary.

Vogel (1967) [137] deduced the following formula which describes the idealized groundwater age as a function of depth (z) within the aquifer:

$$t = \frac{\varphi L}{R} \ln \left(\frac{L}{L-z} \right)$$
(9.1)

This age distribution is independent of the horizontal position x within the Vogel aquifer. While this aquifer model has been used widely to interpret age distributions for young groundwater (0–50 a timescale) using environmental tracers, such as tritium, ⁸⁵Kr and the CFCs (IAEA (2006) [85]), it can of course be easily scaled to large timescales if the parameters R, L and Φ are chosen accordingly. It is, therefore, a good starting point to derive the expected pattern for age-dating tracers in general. In the following, idealized ages were computed from Eq. (9.1) and converted into tracer concentrations using the equation for first order decay for an assumed initial tracer activity and a decay time of the idealized age. These tracer concentrations were then averaged numerically over the well-screen lengths.

9.1.1.2. Tracer depth profiles for the Vogel aquifer

A depth profile for an exponentially decaying tracer such as ¹⁴C, ⁸¹Kr or ³⁶Cl in a Vogel aquifer will always decrease with depth due to radioactive decay with increasing age. However, this decrease will be visible in the depth profile of the aquifer only if the timescale of the aquifer is similar to the timescale of the tracer. A tracer with too short a half-life ($1/\lambda << \Phi L/R$) will decay within the topmost part of the aquifer. A tracer with too long a half-life ($1/\lambda >> \Phi L/R$) will show its decay only at the very bottom of the aquifer, which in many practical cases may not be observed.

Radiocarbon

Figure 9.3 shows the case for a set of parameters describing an aquifer in which radiocarbon shows a discernible decay ($\Phi = 0.2$, L = 1000, R = 0.01). Initial radiocarbon content is assumed to be 100 pmc in this and all following computations in this chapter, such as might be observed under open-system conditions, and ¹⁴C activity changes only by radioactive decay, as might be observed in a siliciclastic aquifer (Chapter 4).

The red squares in Fig. 9.3, which closely follow the blue line, represent mixed samples from 100 m filter screens with midpoints at depths of 50, 250, 450, 650 and 950 m below the water table.



FIG. 9.3. Depth profile for ¹⁴C activity to be expected in a Vogel aquifer: the blue line indicates idealized point sampling and a direct conversion of idealized age (Eq. (9.1)) into ¹⁴C activity. Vertical error bars represent hypothetical screen lengths of 100 m. Red squares give the average ¹⁴C activity of five separate samples, if averaged over each 100 m screen length for each depth range. The red diamonds indicate the average ¹⁴C activity from a single well with five contributing zones, corresponding to those of the red squares — 34.8 pmc. A larger green triangle displays the average ¹⁴C activity if the whole aquifer is sampled with homogeneous inflow — 29.3 pmc.

At the topmost sample, it is obvious that the initial radiocarbon activity can only be observed if near the groundwater surface and sampling is possible with a very narrow depth resolution. As it is, the topmost sample with a screen length from the groundwater surface down to 100 m results in an average ¹⁴C activity of 88.5 pmc. Often, this screen resolution from five separate zones is not feasible in practice, but wells are encountered having several screens at different depths. Such a case in this example results in an averaged ¹⁴C activity of 34.8 pmc if all five depth zones contributed equally to a single well. Also indicated in Fig. 9.3 as a green triangle with error bars over the whole thickness of the aquifer is the ¹⁴C activity of 29.3 pmc which is obtained if a sample is taken from a well that is fully screened from the top to the bottom of the aquifer.

If the radiocarbon data in this simple case were to be converted into ¹⁴C tracer model age with an initial condition of 100 pmc, the ¹⁴C tracer model ages from the single screens would correspond well to the idealized age (Fig. 9.4, idealized ages indicated as a blue line). The three shallowest samples would fit a linear relation of age to depth, which can be used to deduce the recharge rate of the system. In the case of the chosen parameters, a fit would result in a vertical distance velocity of 0.04 m/a, which is indicated by the broken red line in Fig. 9.4. The slope of this fit corresponds nearly but, due to the non-linearity of the system, not exactly to the vertical distance velocity at the groundwater surface ($\Phi \times R = 0.05$). The deepest two samples, however, would not follow this trend, but indicate a much older age due to the non-linearity of idealized ages versus depth in Eq. (9.1).

The more common sampling situation of all five screens averaged in one single sample will result in a ¹⁴C tracer model age of 8726 a, indicated by the vertical line of red diamonds and error bars. The continuous flow-weighted sampling over the whole depth of the aquifer results in a ¹⁴C tracer model age of 10 150 a and is indicated as a green triangle in Fig. 9.4. The blue curve in the figure indicates



FIG. 9.4. Depth profile for ¹⁴C idealized ages, ¹⁴C tracer model ages and mean age (MRT) to be expected in a Vogel aquifer.

idealized ages, assuming neither mixing nor dispersion/diffusion and corresponding to Eq. (9.1). Red squares, following the blue line, with vertical error bars indicating screen length, display ¹⁴C tracer model ages calculated for five screens averaging the sampled waters and ¹⁴C values over a depth of 100 m in each sample. The vertical line of red diamonds corresponds to the tracer model age resulting when all five screens are mixed together in one sample. A bigger green triangle displays the value of 10 150 a resulting for the ¹⁴C tracer model age if the whole aquifer is sampled. In contrast, the blue diamond indicates the (mathematically true) mean age of 20 000 a for the system.

The Vogel aquifer corresponds to the exponential model, which is one of the standard lumped parameter models described in various textbooks (see, for example, IAEA (2006) [85]). It obtains its name for the exponential function that is used as frequency distribution of ages. As described in Chapter 3 and in more detail in IAEA (2006) [85], lumped parameter models are described by the mean residence time (MRT), which for the case of the Vogel aquifer is:

$$MRT = \frac{\varphi L}{R}$$
(9.2)

In the context of this book, the term 'mean age' is used instead of the more common term 'mean residence time'. As for 'apparent age' and 'tracer model age', the terms 'mean age' and 'mean residence time' are treated as synonyms. For the parameters chosen above, the mean age has a numerical value of 20 000 a. This value corresponds to the average of idealized ages in the aquifer and is, therefore, indicated as a blue diamond and vertical line in Fig. 9.4.

The radiocarbon results discussed here for the Vogel aquifer once more illustrate the statement in Chapter 3 that the 'idealized age', the average value of the frequency distribution of ages (the 'mean age' or MRT) and the 'tracer model age' are three fundamentally different numerical values that can all be attributed to the same hydrogeological system. Figure 9.4 simply displays these different values and provides visual evidence for their differences. Evidently, any study aiming for a tracer model age representing the idealized age as closely as possible, should try to obtain samples with the highest depth resolution practically possible.



FIG. 9.5. Depth profile for helium in a Vogel aquifer. Parameters are indicated in the text and correspond to the cases in Fig. 9.2.

Helium

All computations for helium in this chapter assume homogeneity of in situ production and no external flux source (see Chapter 8). Under these assumptions, the amount of in situ produced helium can be computed according to Eqs (8.6–8.8) in Chapter 8 and is proportional to the idealized age. Andrews and Lee (1979) [577] gave an equation for the in situ production rate of helium which is mathematically equivalent to Eq. (8.6) but more easily formulated and comprehensible with any nuclide chart:

$$J(^{4}\text{He}) = \Lambda \cdot \frac{\rho_{R}}{\rho_{W}} \frac{1 - \varphi_{tot}}{\varphi_{eff}} (1.19 \times 10^{-13} [\text{U}] + 2.88 \times 10^{-14} [\text{Th}])$$
(9.3)

where

<i>J</i> (⁴ He)	is the helium flux into the groundwater (in units of cm ³ STP \cdot g _{water} ⁻¹ \cdot a ⁻¹);
Λ	is the release factor;
$ ho_{ m R}$	is the rock density;
$ ho_{ m W}$	is the water density;
$\varphi_{\rm tot}$ and $\varphi_{\rm eff}$	are the total and effective porosities.

For all computations in this chapter, a rock density of 2.655 g/cm³, a water density of 1 g/cm³, a release factor of one, and uranium and thorium concentrations of 40 and 30 ppm, respectively, are assumed. Together with the earlier mentioned porosity ($\varphi = 0.2$), assuming total and effective porosity being equivalent, this results in an in situ helium production rate of 6×10^{-11} cm³ STP \cdot g⁻¹ \cdot a⁻¹). This in situ production has been used throughout this chapter for all plots and model computations.

A depth profile of helium concentration in a Vogel aquifer, thus, shows a logarithmic shape as indicated in Fig. 9.5.

It is observed that the highest ⁴He concentrations in the aquifer (corresponding in this case to the highest tracer model ages) will not be observed in most sampling campaigns because they require a very high depth resolution of sampling very near the base of the aquifer. It is also observed that in

the case of helium, the fully screened sample (green triangle in Fig. 9.5) corresponds more closely to the average of screens (red triangles in Fig. 9.5), since helium concentration increase with time is linear and mixing is linearly weighted. However, an additional crustal flux of helium from below the aquifer would further increase the helium concentration at the bottom of the aquifer. In this case, helium would not show identical depth profiles for every x coordinate within the aquifer, but higher helium concentrations would be observed at x coordinates of elevated crustal flux.

Tracer combination

In this section, consideration is taken of possible interpretations resulting from measurement of concentrations of a suite of environmental tracers (in this case, tritium, ¹⁴C and ⁸¹Kr) in discharge from a multilevel well in a Vogel aquifer (Fig. 9.6). Keeping the parameters constant, tritium as a tracer for the time range younger than 60 a can, of course, only be observed near the water table, down to a depth of approximately 3 m where the idealized age in this model reaches 60 a. However, because the uppermost screen in the multilevel well receives water from this layer, tritium is detectable in this sample, and for a northern hemisphere tritium input function, the sample contains nearly 1 TU if measured in the year 2000. As the half-lives of ⁸¹Kr and ³⁶Cl are considerably greater than that of ¹⁴C, the decay effect of ⁸¹Kr (and ³⁶Cl, not shown in Fig. 9.6) is much less visible than for ¹⁴C (Fig. 9.6) in the depth profile from the five open intervals in the well.

Combining various tracers in a simple homogeneous aquifer such as that described by Vogel (1967) [137], thus, gives age information specific to each of the tracers, each tracer displaying more details of the whole aquifer system. Only if the sampling conditions are good, do tracer model ages for the different tracers agree. Good sampling conditions include short screens and the tracer chosen fitting to the time range of ages in the mixture. Table 9.1 displays the calculated results for samples obtained in the screens for each of the tracers and for the case of equal mixing across each screen



FIG. 9.6. Depth profiles of tritium, ¹⁴C and ⁸¹Kr in a Vogel aquifer. Solid lines represent concentrations obtained for idealized ages. Full symbols with error bars represent values obtained for sampling a screened well, where the error bar represents the screened interval. Vertical lines with open symbols represent concentrations obtained for a full-screened well. Colours represent tritium (purple), ¹⁴C (blue), ⁴He (red) and ⁸¹Kr (green).

Well	⁴ He		¹⁴ C		⁸¹ Kr		³⁶ Cl	
	Value (cm ³ STP/g)	Tracer model age (a)	Value (pmc)	Tracer model age (a)	Value (% mod.)	Tracer model age (a)	Value (³⁶ Cl/Cl × 10 ⁻¹⁵)	Tracer model age (a)
0–100 m	6.71e ⁻⁸	1140	88.5	1010	99.7	1140	498	1140
200–300 m	3.47e ⁻⁷	5902	49.2	5866	98.2	5901	493	5901
400–500 m	7.15e ⁻⁷	12 167	23.1	12 100	96.4	12 166	486	12 166
600–700 m	1.23e ⁻⁶	21 353	7.71	21 186	93.7	21 350	476	21 351
900–999 m	4.45e ⁻⁶	75 710	0.09	57 697	80.0	73 657	422	74 117
Mix of all screens	1.37e ⁻⁶	23 254	34.8	8726	93.7	21 390	476	21 703
Full screened	1.26e ⁻⁶	21 197	29.2	10 163	94.3	19 418	477	20 334

TABLE 9.1. TRACER VALUES AND TRACER MODEL AGES FOR THE VERTICAL PROFILE IN THE VOGEL AQUIFER DISCUSSED IN THE TEXT

and for mixing across the full screened aquifer. As expected, high resolution sampling yields the most consistent results over most of the tracers. However, there is poor agreement between ¹⁴C and the other tracers at the deepest screen, because a significant part of the flowlines entering the screen has idealized ages that are beyond the radiocarbon dating range.

The results demonstrate that, for the case in which the sample represents a mixture of very different ages, the radiocarbon age is significantly too young, because exponential decay biases a mixture to the young side as shown in Fig. 3.3 (Bethke and Johnson (2008) [84]). This is evident in the results of tracer model ages for the fully screened case and the case of equal mixture of all screens. In any case, the disagreement of a factor of two between tracer model ages for different tracers should be taken as an indication that the tracer model ages — at least for some tracers — do not represent a meaningful water age.

With the exception of the fully screened wells, the assumed sampling conditions were quite idealistic. Section 9.3 further elaborates on the resulting patterns, if, for example, mixing between different depths occurs. The Vogel aquifer type represents the infiltration area of a large aquifer system. Thus, it is of interest to investigate whether an aquifer system as a whole, still described as a homogeneous case, will display different patterns in zones of infiltration, of horizontal flow or in zones of upward groundwater flow.

9.1.2. Homogeneous aquifer with different recharge and discharge zones

Tóth (1963) [28] analytically described a simple flow system which displays different areas of recharge and discharge in a homogeneous aquifer. The flow system shown in Fig. 9.7 consists of a trough with impervious left, bottom and right boundaries. The groundwater surface consists of a constant gradient which is modulated by an overlain sine function. As such, the concept is a possible description of one side of a large valley, having a water divide on the right and a discharge system (e.g. a river) on the left. Tóth describes in his classical paper that — depending on the parameters chosen, where the ratio of depth to horizontal extension is probably the most important — different hierarchical orders of flow systems emerge, which correspond to more local or regional flow (Fig. 9.7). This system is still an idealization because it considers a homogeneous aquifer only and neglects mixing, dispersion,



FIG. 9.7. Vertical cross-section for a groundwater flow system in a homogeneous aquifer as described by Tóth (1963) [28]. Lines of equal groundwater potential are shown in red, lines of groundwater flow in blue, with arrows indicating the flow direction. The vertical exaggerated profile on top indicates the groundwater surface creating this flow field. Vertical age and tracer profiles at horizontal positions A (infiltration), B (horizontal flow) and C (upward flow) are discussed in the text.

diffusion and external fluxes. Nevertheless, it is useful to distinguish age patterns observed in recharge areas, areas of horizontal flow and discharge areas.

The parameters chosen for this example are: depth L = 5000 m, horizontal extension = 20 000 m, linear gradient = 0.001, amplitude and wavelength of the hills around this gradient = 5 and 6100 m, respectively, porosity = 0.3 and the k_f value = 10^{-6} m/s. Tóth (1963) [28] gives an equation for the potential as a function of horizontal extent, x, and the vertical coordinate, z. To create depth profiles, an approximate depth below groundwater surface is also displayed, which is computed as L-z (right z axis in Fig. 9.7) and will be used in all subsequent graphs. For the discussion in the following, this formula was differentiated and multiplied by porosity to obtain the (distance) velocities. Idealized ages were computed by integration of this flow field to obtain idealized ages. The tracer values were computed from these idealized ages. These tracer values were then averaged over different screen positions as above in the Vogel case.

9.1.2.1. Infiltration areas

The horizontal locations indicated with the large letter A in Fig. 9.7 correspond to infiltration areas of different flow systems and are always associated with the hilltops in the groundwater surface. Evidently, these infiltration areas feed different flow (sub)systems in the Tóth aquifer: A1 at $x = 19\ 800\ m$ corresponds to the infiltration area of the largest flow system, whereas A2 ($x = 14\ 000$) and A3 (x = 8000) correspond to smaller watersheds with one (A2) or two (A3) underlying larger flow systems. For each of the depth profiles, the calculations that follow assume that there are eleven screens, the shallowest one centred at z = 4985 with 28 m screen length and the deeper ones built with



FIG. 9.8. Depth profiles of ⁴He, ¹⁴C, ⁸¹Kr in infiltration areas. Locations of profiles A1 (red), A2 (blue) and A3 (purple) are indicated in the flow field (top left). Vertical bars correspond to extension of well-filter screens.

a 280 m screen length at regular intervals of 500 m starting at a centre of z = 4650 (Fig. 9.8). Figure 9.8 shows the resulting depth profiles for ⁴He, ¹⁴C and ⁸¹Kr.

The mathematical solution of the Tóth model has zones of very low groundwater velocity between the first and the second flow system. This results in high idealized ages that create high ⁴He concentrations and low ¹⁴C and ⁸¹Kr activities in areas of low groundwater velocity. However, unless the depth resolution in sampling is extremely high, these 'stagnant' zones will probably not be sampled and in most cases will be of no practical importance. The transition from one flow system to the next, however, results in concentration steps in the tracer depth profile. Depending on the depth resolution during sampling, probably not all of these transitions are visible in the tracer depth profile: it would be possible from the ⁴He and ⁸¹Kr depth profiles of filtered screens, to postulate a second circulation system at greater depth, but hard to decide whether there are one or two different ones in the A3 case in Fig. 9.8. With the parameters used here, ¹⁴C will not be measurable in the older, underlying flow systems.

With the appropriate combination of tracers covering the timescales of the aquifer, and with suitable depth resolution, it is feasible to determine recharge rates, to discern whether a recharge area belongs to a regional or only-local flow system, and if further flow systems are beneath. It is, thus, of interest if depth profiles for the more vertical downward flow of an infiltration area can be distinguished from areas of horizontal flow.

9.1.2.2. Areas of horizontal flow

The horizontal locations indicated with the large letter B in Fig. 9.7 correspond to areas where the flowlines are mainly horizontal in the selected Tóth model. They are associated with the maximum head gradient, where the sine wave determining the local groundwater gradient in Fig. 9.7 equals the straight line determining the regional groundwater gradient. In all cases, the depth profiles tap



FIG. 9.9. Depth profiles of ⁴He, ¹⁴C, ⁸¹Kr in areas of horizontal flow. Locations of profiles B1 (red), B2 (blue) and B3 (purple) are indicated in the flow field (top left). Vertical bars correspond to extension of well-filter screens.

different flow systems, and the positions chosen for further discussion are B1 at $x = 18\ 000$ m, B2 at $x = 12\ 000$ m and B3 at x = 6200 m. Figure 9.9 shows the resulting depth profiles for ⁴He, ¹⁴C and ⁸¹Kr.

At first glance, there seems to be little difference in the shape of the tracer profiles between Figs 9.8 and 9.9. Again, the transition from a shallow flow system to the next deeper flow system appears as a step in the depth profile of the age tracers. A closer comparison reveals that the numerical values are different: there is more ⁴He and less of the radioactive tracers at similar depths in the profiles of the horizontal flow situation as compared to infiltration areas. For ¹⁴C, it is remarkable that the different profiles cross each other (Fig. 9.9, lower left): ¹⁴C has the highest time resolution since its half-life is best suited for the timescale of flow in the shallow systems. Therefore, the different age gradients of the shallow flow systems become more evident here — although they are present in the top parts of the depth profiles of ⁴He and ⁸¹Kr, they are not as clearly discernible as in the ¹⁴C profile. Profile B1 represents the infiltrates down to a depth of 4000 m within the dating range of ¹⁴C (50 000 a). Profile B3 represents the shallowest system. Here, the idealized ages cover values between zero and the dating range of ¹⁴C within a depth interval of 0–2500 m.

Without a conceptualization of the hydrology of the flow system, it would be difficult to even distinguish recharge areas from regions of dominant horizontal flow on the basis of tracer data alone. This illustrates that hydrogeological knowledge of the flow system is necessary before age studies are initiated (see Chapter 2), and that the purpose of the age tracers is to help quantify the flow system, not to a priori investigate its dominant direction of groundwater flow. However, this similarity of patterns between recharge area and area of horizontal flow raises the question of whether the regions of upward directed flow, where groundwater discharges to surface water or to shallower systems, show different patterns.

9.1.2.3. Areas of upward flow

A naive understanding of 'upward flow' might lead to the expectation that water ages increase in the upward direction, because this is the flow direction. Basically, it would be as though the patterns in the right part of Fig. 9.1 were flipped upside down. This would result in an upward increase of ⁴He and an upward decrease of the radioactive tracers ¹⁴C and ⁸¹Kr and is called an 'age inversion' in stratigraphy. Closer investigating the details of the flowlines in Fig. 9.7 reveals that a vertical profile in an area of upward directed flow will hardly ever sample only one flowline. This easily explains why the tracer depth profiles for ⁴He, ¹⁴C and ⁸¹Kr, in regions with partly or dominant upward flow, seldom show an age inversion (Fig. 9.10). Vertical profiles for this case are situated at x = 10000 m for profile C1 and at x = 4830 m and x = 80 m for profiles C2 and C3, respectively. Regions of upward directed flow may show age inversions in part of the vertical profile, as the upper three screens in profile C1 show for ⁴He and ⁸¹Kr. However, even in this profile, the values for ¹⁴C do not show this inversion for the last two screens, because the screen at a depth of 350 ± 150 m samples a mixture of very different ¹⁴C concentrations and, as such, is biased young. For the aquifer parameters chosen here, radiocarbon is measurable only in profiles C1 and C2, and in these radiocarbon content is so small (<1 pmc) that in many practical cases it will probably provoke discussions about contamination during sampling among the scientists in the project.

As a summary, depth profiles in areas of upward flow are generally characterized by large depth regions where the age-indicating tracers are constant with depth. This is observed on a level of activity (¹⁴C and ⁸¹Kr) or concentration (⁴He) that indicates considerable age. In areas where the upward directed flow belongs only to the local groundwater systems, such as the C3 profile, again steps in the tracer profile may occur, but these are less pronounced as in the case of horizontal flow. With these characteristic features, discharge zones should, in many cases, be clearly discernible from recharge zones and areas of horizontal flow, given an adequate resolution in the vertical scale of sampling.



FIG. 9.10. Depth profiles of ⁴He, ¹⁴C and ⁸¹Kr in discharge areas. Locations of profiles C1 (red), C2 (blue) and C3 (purple) are indicated in the flow field (top left). Vertical bars correspond to extension of well-filter screens.

All of these considerations of course neglect two natural processes important for the depth profiles: first, dispersion and diffusion are neglected. Taking these into consideration, the 'singularities' shown in Figs 9.8–9.10 at the transition zones from one flow system to the next will be considerably smoothed. The general shape of the depth profiles computed for screened well intervals, however, will not be altered. Second, external fluxes are neglected. Especially for the ⁴He depth profiles, this may be an unrealistic assumption, as pointed out in detail in Chapter 8. Qualitatively, external fluxes will increase the ⁴He concentration towards the bottom of the aquifer in all depth profiles. If this mainly diffusion driven flux is not too large, the profile in the 'global' infiltration area (profile A1, Fig. 9.8) will not be altered too much, since the downward groundwater movement will flush the helium influx from the bottom of the aquifer. In areas of horizontal flow, however, ⁴He gradients with depth will be considerably larger, especially near the base of the aquifer. In the areas of upward flow, ⁴He concentrations will be orders of magnitude higher, although the general shape of the profiles is not necessarily altered.

The most unrealistic assumption of the Tóth model (Tóth (1963) [28]) is to assume homogeneous aquifer transmissivity. The next step is, thus, to consider a layered aquifer with varying transmissivity. This is not as easily examined in a quantitative and detailed manner, because analytical solutions to the flow system are not available as they are for the Vogel or Tóth models.

9.1.3. Aquifer systems — confined or partly confined

While the case considered in Section 9.1.2 is easily understandable, it is not very realistic. In natural systems, a sediment layer of 5 km thickness with only one k_f value is rarely the case. Although sedimentary basins of this thickness exist in various areas of the world, the sedimentation processes changed, and these changes created layers of varying grain size, different sorting of grain sizes and different compaction, resulting in different transmissivity. This transmissivity can vary by orders of magnitude, as discussed in Chapter 2. Deep systems tend to be layered into aquifers (comparably high transmissivity), aquitards (smaller transmissivity) and aquicludes (transmissivity so low that groundwater flow is negligible as compared to flow in aquifers). Even if a layer is regarded to be 'homogeneous' from the sedimentological point of view, variations of a factor of five in the k_f value are still possible, simply because deducing the k_f from sedimentological information involves an uncertainty of this magnitude. All smaller variations are very difficult to detect by sedimentological methods or even from data obtained from sophisticated pump tests.

9.1.3.1. Single depth profile in various aquifers

As an example, the depth profile sketched in Fig. 9.11 is considered. The sediment consists of several aquifers of different thicknesses, separated by aquitards, which are assumed to be impervious with respect to flow and diffusion. Horizontal flow is assumed through each aquifer layer, the distance velocity is calculated from Dary's law and porosity, and this idealized age is converted into tracer concentrations as in the previous sections. In detail, this implies the following assumptions: the aquifers are assumed to have different k_f values. For the sake of simplicity, all aquifers (i) are assumed to be recharged in the same area at a distance of 100 km, (ii) are assumed to have the same gradient of 1×10^{-4} in hydraulic potential and (iii) are assumed to have the same properties in the infiltration area which leads to identical ⁴He production rates, and all have ¹⁴C and ³⁶Cl ('no decay') initial conditions. In fact, the only varying parameter is the k_f value, which is indicated for the aquifers in Fig. 9.11.

The first impression looking at the tracer depth profiles is the absence of the systematic patterns observed in the homogeneous aquifers. In the homogeneous case, the radioactive tracers ¹⁴C and ⁸¹Kr decreased in a more or less monotonic manner with depth in nearly all cases, whereas ⁴He increased



FIG. 9.11. Vertical tracer profiles in an aquifer system with separating aquitards.

with depth. The inhomogeneous case is completely dominated by the transmissivity values and shows a very irregular pattern of decreasing and increasing tracer values with depth.

A closer inspection of the depth profile of different tracers in this multi-aquifer system shows the expected pattern with lower values for the radioactive decaying tracers ¹⁴C and ⁸¹Kr (larger age) in aquifers of lower k_f value. Important to note is that a comparably small difference in k_f values can be easily discerned from the tracer results: the difference of 1×10^{-3} and 2.5×10^{-3} m/s between the topmost two aquifers results in clearly different ¹⁴C signals. It is also important to note that different tracers with different timescales are necessary to cover the transmissivity values in this example: aquifers IV and V show 'infinitely old' water on the ¹⁴C timescale whereas ⁴He and ⁸¹Kr give results which are clearly different from the aquifers of high transmissivity above and below, and which are still discernible from each other.

Since purely advective flow to simulate the tracers is again considered, a qualitative discussion is helpful with regard to the difference between the derived tracer values in this artificial case and tracer values in a more realistic case. One important but neglected parameter is aquitard leakage between aquifers. Only rarely do aquifer stacks in nature have the same hydraulic potential; often, pressures are different between aquifers. This means that flow is induced in the vertical direction through the aquitards. Although the amount of water flowing per square meter through the aquitards between adjacent aquifers may be very small, it has to be multiplied by the entire area over which the pressure difference exists; an area that may amount to many square kilometres. Therefore, the amount of crossaquifer flow will, in many cases, have a measurable effect on the tracer values, caused by mixing of different waters. Cross-aquifer flow will generally decrease the differences of tracer values between aquifers. In this case, this will probably influence aquifers III, IV and V the most, because these have the largest differences in tracer values compared to their neighbours. If the flow through the aquitard needs a considerable amount of time, however, it will not cause water of the age $a_{\rm B}$ of the adjacent aquifer B to mix into aquifer A but water of an age $a_{\rm B} + t$ where t is the time needed for the transfer through the aquitard. The same also holds true for any other parameter changed within the aquitard (amount of dissolved solids, ion exchange, etc.).

Diffusion of radioactive tracers into the aquitards or of helium out of the aquitards may also have a noticeable influence. This can be simulated with the theory of dual porosity aquifer systems which are discussed in Chapters 4, 5, 8 and 10. Finally, any helium flux from external sources was neglected, in this case from below the whole aquifer system sketched in Fig. 9.11. As discussed in detail in Chapter 8, such an external flux will increase the helium concentration in the deepest aquifers, until an aquifer is reached which is able to transport all of the helium of this flux to the surface. Above this aquifer — in this case probably the deepest one, VII — helium from crustal flux is negligible, but helium from the adjacent aquitards may still increase the concentration above the one produced in situ.

9.1.4. Summary

Section 9.1 has demonstrated possible tracer patterns that can be obtained sampling an aquifer with multilevel wells. It also demonstrated how mixing of waters from different depths with different age can influence the result. It demonstrated that it will be difficult or impossible from tracer data alone to distinguish recharge areas from areas of horizontal flow, because their tracer patterns are very similar. Therefore, a conceptual model of the groundwater flow system is necessary before starting the tracer study. In contrast, discharge areas can be more easily detected. Section 9.1 also demonstrated that in aquifer systems consisting of aquifers and intercalated aquitards, tracer results will be dominated by the transmissivity of the aquifer.

There are some conclusions of this section which can be translated into practical advice for the application of environmental tracers to study groundwater age:

- (a) Optimum wells for the purpose of age dating of groundwater are constructed to obtain an unmixed sample from a defined depth with a depth range being very small as compared to the total depth of the well. Well nests constructed this way to obtain a depth profile of samples are the optimum choice.
- (b) Optimum depth resolution of multilevel well nests should be higher near the groundwater surface and near the bottom of the aquifer. This is because, at these interfaces, the largest variation of tracer data is to be expected.
- (c) Whenever it is possible in the early stage of a groundwater study to influence the construction of observation wells, the facts above should be taken into consideration.
- (d) Section 9.1 also allows the following conclusions to be drawn for most practical cases where sampling conditions are not optimal, for example, where only wells completed with multiple screens are available, where open boreholes in fractured rock have to be sampled, etc.

Geotechnical methods should be considered to obtain samples with optimum depth resolution for the given case (packer systems, sampling with the dual-pumping technique (Rapp et al. (1998) [591]), chains of passive samplers, etc.).

Different (hydrochemical and isotopic) tracers should be applied to enable the deconvolution of mixtures (see Section 9.3 for further multitracer techniques to detect mixtures).

Direct conversion of tracer values to tracer model ages in most such cases will give no useful results; therefore, this should be considered only after the deconvolution of mixtures was possible.

Tracer concentrations and activities for these samples should be directly described (without converting them to tracer model ages), applying the knowledge about the sampling conditions and using an interpretation model that describes the transport conditions as closely as possible.

For instance, for the Vogel case discussed in Section 9.1.1.1 where the sample was obtained from a full screened well penetrating the whole aquifer, the direct conversion of tracer values into tracer model ages will not give a reasonable result. Fitting the tracer values for the fully screened well to an exponential model, however, will result in the correct mean age time of 20 000 a. An exponential model applied to interpret the single well completed with five screens will also give a more useful result than the direct conversion of the tracer data into a tracer model age.

As discussed, vertical profiles will only in rare cases display an evolution along a line of groundwater flow. Given the fact that most aquifers have a much larger horizontal than vertical extension, horizontal transects seem better suited to show development along a flowline.

9.2. HORIZONTAL TRANSECTS

Vertical tracer transects provide useful insight into the age structure of an aquifer or aquifer system. Horizontal sampling along assumed flowlines in aquifers can also provide very useful information on the flow field, including estimation of distance velocities. However, one of the most difficult problems in this approach is in recognizing the flowlines and sampling along actual flowlines in aquifers.

9.2.1. Transect along an assumed flowline

Figure 9.12 qualitatively displays a possible scenario for horizontal flow in an ideally confined aquifer. The top part sketches the aquifer, which shows a constant thickness for a flow distance of 100 km until the thickness increases by a factor of four, possibly due to intersection of a fault. A constant $k_{\rm f}$, potential gradient and porosity are assumed and a constant distance velocity at least up to x = 100 km is calculated. This means that distance linearly translates into age and, for tracers with exponential decay, this situation results in an exponential decrease in tracer concentration with flow distance, starting with whatever the initial value was at the first sampling point along the flow path. With parameters $k_{\rm f} = 4 \times 10^{-4}$ m/s, gradient = 1×10^{-4} and porosity = 20%, such curves are shown for ¹⁴C and ⁸¹Kr in Fig. 9.12 (right y axis). For tracers increasing linearly with age, for example ⁴He, a linear increase with flow distance results and is also shown in Fig. 9.12 (left y axis).

Also shown in Fig. 9.12 is the effect of change in thickness for a confined aquifer. In the present case, the thickness changes at flow distance x = 100 km to be four times larger than before. As in this



FIG. 9.12. Transects of ⁴He (left axis), ¹⁴C and ⁸¹Kr (right axis) along a flowline in a confined aquifer where aquifer thickness and, therefore, flow velocity vary.

example the aquitards above and below the aquifer are impervious, and all other parameters are assumed to be constant, the new aquifer thickness results in a flow velocity that is a factor of four lower than in the thinner section of the aquifer. This lower flow velocity changes the relation between flow distance and age, and results in new rates of decrease of radioactive tracer concentration with distance for ¹⁴C and ⁸¹Kr, and new rates of linear increase with distance for ⁴He. Calculation of distance velocity as the difference in tracer model ages divided by flow distance provides an estimate for the combination of $k_{\rm f}$ and porosity. Provided enough samples were taken at flow distances smaller and larger than 100 km, the result will be two significantly different numbers for effective aquifer transmissivity. Estimates for these important hydrogeological parameters are often difficult to obtain by other means. If the fault zone and the possibility of varying aquifer thickness are known from hydrogeological information, it can be taken into account for calculation of different distance flow velocities from the tracer transects. In this case, the two parts of the transect will result in two different distance (and Darcy) velocities. On the other hand, information on actual aquifer thickness is comparably difficult to obtain. Therefore, the example above demonstrates that calculation of distance velocity from tracer transects along a flow path may, in some cases, be more cost effective and easier to obtain than a detailed hydrogeological or seismic study.

As in all cases before, this case contains several simplifications that probably are not generally valid in all aquifer systems: diffusion of tracers into aquitards (radioactive tracers such as ¹⁴C, ³⁶Cl and ⁸¹Kr) and from aquitards (⁴He) is neglected as well as a possible crustal flux of helium from below. These effects will not be homogeneous with depth or distance and will tend to change the tracer values towards larger ages. More important, the discussed case is only valid if the samples are actually located along the same flowline. This is less severe an assumption in a confined aquifer although many aquifers will likely have a flow component perpendicular to the plane of Fig. 9.12. This can only be studied with a case of higher dimension — sampling for a map of tracer values in one aquifer, instead of sampling only along an assumed flowline. Using the analytical Vogel and Tóth flow models, discussed in Section 9.1, will give further insight as to how severe the effect of not being on the same flowline might be.

9.2.2. Horizontal transects intersecting different flowlines

The Vogel model described in Fig. 9.2 obviously describes not only an infiltration area but also a horizontal flow of groundwater in this idealized aquifer as a whole. However, the ages in the Vogel aquifer are described by Eq. (9.1), which does not depend on the *x* coordinate, but only on the depth within the aquifer. This means that a horizontal transect of samples, all taken from the same depth in a Vogel aquifer, will result in identical tracer values and identical tracer model ages. This is a result of the fact that none of the flowlines in the Vogel model (Fig. 9.2) are horizontal, so no horizontal transect will sample the same flowline twice. Of course, any real sample will originate from a well with a finite screen interval and, therefore, will integrate Eq. (9.1) over the depth between the lower screen coordinate, z_L , and the upper screen coordinate, z_U . However, if the screen lengths are equal for all samples, this integral is still a constant. Thus, the average of idealized age over the screened interval and, therefore, the tracer concentrations will be identical along a horizontal transect.

If the screen lengths vary, different tracer values and different tracer model ages will result, even if the centre of the screen is always at the same depth. If, for this reason, the tracer model age increases on a horizontal transect, this age increase would lead to incorrect estimates of distance velocities. The two examples of horizontal transects discussed up to now demonstrate two extreme cases: in the first, the confined aquifer, horizontal distance directly translates into age and the corresponding tracer values; in the second, the unconfined (Vogel) aquifer, horizontal distance is completely independent of age and will, therefore, result in identical tracer values. This once more emphasizes that a depth profile in the practical case may give more insight into the flow system than many horizontal samples, because a detailed understanding of the flow system is already necessary to perform a useful horizontal sampling.



FIG. 9.13. Three horizontal transects for ⁴He, ¹⁴C and ⁸¹Kr in the Tóth aquifer of Fig. 9.7. The depth of the transects is 4200 m (purple), 2500 m (blue) and 700 m (red), corresponding to model-z coordinates of 800, 2500 and 4300 m, respectively.

The case of the Tóth aquifer is more complicated, since local infiltration and upward directed flow alternate in this case. Figure 9.13 shows three horizontal transects, sampled at depths of 700 m (shallow, red curves), 2500 m (intermediate, blue curves) and 4200 m (deep, purple curves) for ⁴He, ¹⁴C and ⁸¹Kr in the Tóth aquifer discussed in Fig. 9.7. As before, computed tracer values were averaged over depths corresponding to 200 m of well-screen.

From all tracers, it is evident that the shallow transect samples the local circulation systems and only the deep transect shows an increase of age with flow distance. For example, ⁴He in the deep transect shows monotonous increase in flow direction (right to left in this picture). The shallow ⁴He transect in contrast in most areas shows hardly any excess ⁴He but does contain local spikes that might be missed without detailed horizontal sampling. A similar pattern is observed for ⁸¹Kr, although in the opposite sense, since this tracer shows radioactive decay. The values for ⁸¹Kr in most screens of the shallow transect show minimal variation; only if, by chance, one of the screens is situated at a position of upward directed flow, a sudden decrease in ⁸¹Kr values may be observed. The deep transect shows the expected decrease of ⁸¹Kr with flow distance. Both of these tracers, ⁴He and ⁸¹Kr (and ³⁶Cl), are on a timescale too long to produce discernable age variations in the shallow transect.

Radiocarbon, in contrast, has a decay constant that is on an appropriate timescale for the shallow transect and partly also for the intermediate transect. Carbon-14 clearly reflects the infiltration areas with high radiocarbon values and the zones of upward directed flow with low radiocarbon values. In the intermediate transect, ¹⁴C also indicates evidence of young water at the right side, close to the deep-reaching infiltration area. Later in the intermediate transect and in the whole deep transect, groundwater circulates on a timescale too large for detection of flow patterns using ¹⁴C.

The assumption to sample the same flowline along a horizontal transect following the gradient of groundwater potential may be a reasonable and valid approach in confined aquifers. It is, however, normally invalid in phreatic aquifers with only small variations in aquifer transmissivity. In phreatic aquifers, horizontal transects along an assumed flow direction can result in constant tracer values as demonstrated in the Vogel case, or in tracer values reflecting a series of locally young and old waters in the regional flow direction. This may seem unexpected on first sight, but is nevertheless in accordance with the general direction of flow. As Tóth (1963) [28] pointed out, a regional flow system circulation on long timescales may be present depending on aquifer parameters, but will then be observable only with very good depth resolution and only in the deep parts of the aquifer.

9.2.3. Summary

Section 9.2 demonstrated that horizontal tracer transects along an assumed flowline can help to obtain important information on the groundwater flow system such as distance velocity and aquifer transmissivity. The discussion of the Vogel aquifer in Section 9.1.1 also demonstrated that a horizontal transect in the direction of groundwater flow does not necessarily result in an increase of tracer model age in the flow direction. The discussion of the Tóth aquifer even demonstrated the possibility of locally decreasing ages in the general flow direction which pointed to the existence of local flow systems.

The first two sections of this chapter, 9.1 and 9.2, demonstrate the following:

- (a) To understand the details of a flow system, many measurements of age-dating tracers are necessary, not just a single measurement of one particular tracer.
- (b) A combination of different tracers covering different timescales is necessary, if a flow system as a whole is to be understood.
- (c) If development of a conceptual understanding of the flow system is still in its initial state, a depth profile of tracer measurements is advantageous to gain further understanding.
- (d) Horizontal transects aiming to sample a single flowline promise further useful details if the flow system is well constrained — either because it is a confined aquifer or because a detailed flow model has already been constructed. Only this allows the choice of sampling wells that may be on a flowline.
- (e) Horizontal transects not showing the tracer pattern expected are a clear indication that either the flow model needs refinement or that unexpected tracer specific phenomena are occurring. Possible reasons include changes in aquifer thickness, changes in flow direction, flow convergence, changes in tracer fluxes in or out of the aquifer (especially for ⁴He) and geochemical alteration of the tracer (in the case of ¹⁴C or ³⁶Cl). Isotope hydrological tracers demonstrated their suitability to boost the necessary model refinements (see Chapters 11–14). Often, new sampling on a different spatial scale is necessary to achieve the necessary insight for such refinements.

The results here were obtained assuming excellent sampling conditions: multilevel sampling with several well isolated screens at different depths was a prerequisite for the considerations in Sections 9.1 and 9.2. Of course, this gives rise to the question of what may happen if the sampling conditions were not as ideal. What happens if there are several screens, but all in one borehole, leading to mixed samples from different depths? The next section presents methods that use measurements of several different tracers to resolve instances of borehole mixing.

9.3. IMPORTANT PATTERNS OF TRACER VERSUS TRACER

The combination of tracers reflecting different timescales is both a powerful and necessary approach when studying old groundwater. Whenever a tracer for a long timescale is used with the final goal of deriving an age, it should be supplemented by tracers for young components and, if possible, also by tracers for the next longer timescale. The reason is that most groundwater samples represent mixtures of an a priori unknown kind. As discussed in the introductory chapters, it is very

improbable that the frequency distribution of ages represented by a water sample consists only of one (idealized) age. In most cases, it will at least be broadened by diffusion and dispersion. As discussed using the Vogel and Tóth aquifer models, it can also show different, sometimes systematically varying idealized ages over the length of the screen. It may also consist of different non-overlapping age ranges (see Fig. 3.1) which normally are described as (binary, ternary, etc.) mixtures. Such mixtures will result in tracer model ages that may be very different from the ages of the (two or more) water end members that dominate the mixture. As seen in Table 9.1, such a multicomponent mixture manifests itself by tracer model ages that are different for each tracer. Often, these mixtures can be identified plotting one tracer versus another. In addition, if the age of the groundwater approaches the maximum dating range of a certain tracer, any small admixture of younger water will keep this tracer close to but not within the dating range. For example, a 2% admixture of 150 a old water to a 100 ka old water body will keep the ¹⁴C value near 2 pmc and the tracer model age near 32 ka — which surely will not be a representative age for the bulk of the water. However, combining the measurements of two different tracers with very different dating ranges can make the presence of such mixtures obvious by showing discrepant ages for the different tracers. Even before calculating any ages with the tracers, simple plots of one tracer relative to another can characterize samples consisting of waters of different age. Such tracer-tracer plots are presented below.

9.3.1. Combination of tracers for different timescales

Plotting a tracer A which decays fast or is relevant only for a small timescale versus another tracer B for a larger timescale gives insights into mixtures, initial conditions and practical detection limits. A typical plot is sketched in Fig. 9.14: in this case, the short-time tracer is plotted on the y axis and the long-time tracer on the x axis. If the long-time tracer is radioactive, it is best to plot the x axis with a logarithmic and descending scale. Doing so, a distance on the x axis represents a distance in time, independent of any initial 'no decay' value and without calculating an age. A possible tracer combination might be tritium on the y axis and ¹⁴C on the x axis. Instead of tritium, CFCs can be used



FIG. 9.14. A plot of tracers of different timescales reveals initial values for the old tracer, shows practical detection limits for the young tracer and makes mixtures of waters with different ages obvious.
(see Chapter 4). However, the same principle applies for radiocarbon as a short-time tracer on the y axis in combination with ³⁶Cl as a long-time tracer on the x axis.

What are the patterns that can be observed on such a plot? In the simplest case, showing only idealized ages, all samples would plot along and very close to the x and y axes of Fig. 9.14. This is because short timescale tracers (e.g. tritium or CFCs) will decrease with age to zero before long timescale tracers (e.g. ¹⁴C) will show any noticeable decrease. The young samples containing short timescale tracers plot along the y axis, with the x value (long timescale tracer) close to the initial value. As age further increases, the long-time tracer will decrease while the short-time tracer is already at zero, plotting the older samples along and close to the x axis. However, because many other processes and factors can affect tracer concentrations, this simple picture is disturbed.

First, the short-time tracer may show some behaviour with time. Tritium and the CFCs show peaks with time, the peak of tritium being around 1963 and the peaks of CFCs in the early 1990s. If the long-time tracer shows no such anthropogenic influence, such as ⁸¹Kr, then still all points containing the short-time tracer lie along the y axis. However, as discussed in Chapter 4, radiocarbon in atmospheric CO_2 raised by nearly a factor of two above natural values due to the bomb tests, and this happened and remained measurable during the same time span as the peaks in tritium and CFCs. As a consequence, a plot of tritium and CFCs versus radiocarbon will — even for idealized ages — plot along a curve close to the y axis. This is similar for the combination ¹⁴C/³⁶Cl, because both show anthropogenic increase due to bomb production.

Second, some long-time tracers have no well defined initial value. This is true for ¹⁴C because the 'no decay' value is influenced by chemical processes in the unsaturated zone and in the aquifer, as discussed in detail in Chapter 4. This is true for ³⁶Cl, since the initial ³⁶Cl/Cl ratio depends on the recharge area and the climatic conditions during recharge, as discussed in Chapter 6. Therefore, a plot of tritium versus ¹⁴C or of ¹⁴C versus ³⁶Cl/Cl can give information on the initial value of the longtime tracer on the x axis (¹⁴C and ³⁶Cl/Cl, respectively) as indicated by the red bracket 'initial value' in Fig. 9.14.

Third, all tracers have practical detection limits. These depend on the method of measurement and on the sampling conditions. For tritium, the analytical detection limit is typically around 0.5–0.1 TU for beta-counting after enrichment; for the ³He ingrowth technique, it can be as low as 0.005 TU; and for CFCs it is around 0.01–0.03 pmol/L. For ¹⁴C and ³⁶Cl/Cl, it is around 0.1 pmc and 10×10^{-15} , respectively, as discussed in Chapters 4 and 6. Practical detection limits due to the sampling conditions (leaky well casing, reagents used in the field, contamination due to difficult field conditions, etc.) may be higher than these analytical detection limits. For instance, using normal sampling and transport methods, one would not interpret tritium values greater than 0.05 TU as representing samples containing significant amounts of young water, or treat samples with 0.3 pmc as 'radiocarbon free'. The plot in Fig. 9.14 can provide an estimate of these practical detection limits, because this is the range where the concentrations of the short term tracers level off as the long-time tracer concentration decreases, as indicated by the horizontal red line and the crosses below.

Fourth, actual groundwater samples do not contain water of only one idealized age. Instead, a sample consists of waters containing a narrow or wide age distribution, or can even be a mixture of two or more waters with disjunctive ages. Imagine, for instance, a deep borehole with several screens or an open borehole in fractured rock with several water-bearing fractures. Such binary or multicomponent mixtures will plot in the triangle area in Fig. 9.14, denoted 'mixtures'. Any sample plotting in this triangle area of Fig. 9.14 is a mixture of young and old water and, generally, within this triangle the tracer model age is not a good estimate for the groundwater age.

In principle, mixtures from the triangle area may be deconvoluted into the components, and ages for the mixing components may be computed. This is a difficult task, however, and often not possible in the practical case. Deconvolution of the mixture needs at least as many analysed parameters as mixing components are present, to narrow down the original water masses and their 'initial' tracer values. In general, the age of the two components is also unknown, which needs at least two additional age-tracer



FIG. 9.15. Plots of tracers with different timescales. Example curves are for a piston flow model (blue line) and an exponential model (red line), and for two multilevel screens of the Tóth model (at x = 2000, exfiltration conditions and at $x = 14\ 000$, infiltration conditions, black dots) together with binary mixtures between screens (small dots).

values per sample. Since each tracer has an age range over which it is sensitive (Fig. 1.3), each tracer can only resolve mixing components within the valid dating range of the tracer. For further numerical modelling approaches as discussed in Chapter 10, the samples from the triangle area in Fig. 9.14 should be avoided, or, if this is impossible, at least be treated with the necessary caution during modelling.

Two examples for the plots using tracers of different timescales are given in Fig. 9.15. The curves in Fig. 9.15 represent the piston flow model, which corresponds to the idealized age since it assumes no mixing (blue curves). Figure 9.15 also shows tracer concentrations for the exponential model, corresponding to the Vogel aquifer with a full screened well as discussed in Section 9.1.1 for different mean ages (red curves). As a mixing example, two multilevel screens from the Tóth model in Section 9.1 are displayed as black dots connected by a line. The left pane focuses on the shorter timescales and displays results computed for screens from the infiltration area at $x = 14\,000$ m, and plots CFC-11 versus radiocarbon. The right pane for the longer timescale displays results computed for screens from the combined infiltration-upward flow area at x = 2000 m, and plots radiocarbon versus ⁸¹Kr. Since screens in the discussed Tóth case are short enough, the large black dots are very close to the piston flow and exponential model curves (blue and red lines, respectively). In both plots, small black dots show binary mixtures between all possible screen combinations in steps of 10% for the mixing ratios.

The plots show that the curves for the exponential model (= full screened Vogel aquifer) are similar to the curves assuming idealized ages for tracers of very different timescales. However, the numerical values for the average age and the idealized age are very different for single pairs of blue and red symbols situated close to each other. The initial condition for ¹⁴C ('no decay' 100 pmc) could be easily deduced from these plots, and from both model assumptions. Values for ¹⁴C in both plots are higher than 100 pmc for small idealized ages and mean ages due to the presence of anthropogenic bomb ¹⁴C in the atmospheric input function. The comparably clear picture of the blue and red line, however, is considerably complicated if binary mixtures between screens of different depth are taken into account. In this case, tracer combinations are possible which could not occur assuming idealized ages or the simple mixture and dispersion patterns used in lumped parameter modelling.

Whereas CFC-11 is measurable only in the topmost screen in the Tóth aquifer, radiocarbon is also present at a greater depth. Consequently, the clear patterns of the piston flow or exponential model can be disturbed with a higher probability in the plot of ¹⁴C versus ⁸¹Kr, because more screens contain ¹⁴C.

This seems initially to be an unsatisfactory result; however, on the contrary, if the absence of CFCs, tritium and even ¹⁴C can be demonstrated, this leads to the conclusion that even small admixtures of young water can be excluded, 'young' meaning, in this case, waters up to several thousand years of age.

Plotting tracers of different timescales versus each other is, therefore, a useful tool for the detection of unwanted mixtures, possibly created during sampling. It also allows the necessary determination of initial values for ¹⁴C and ³⁶Cl close to the infiltration area. A direct comparison of ages, or a detection of processes that influence the long time tracer only, needs a comparison of tracers with similar timescales.

9.3.2. Combination of tracers with similar decay timescales

The combination of different age-dating tracers with similar timescales is always desirable since the assumptions of one tracer application can be checked against another tracer, providing greater confidence in the interpretation of both sets of tracers. Many details of this approach were discussed in the CFC guidebook (IAEA (2006) [85]) for young groundwaters. For old groundwaters, however, there are only two radioactive tracers available that operate on the same timescale, namely ³⁶Cl and ⁸¹Kr. The basic effects that can influence the comparison of these two tracers were described in Chapters 5 and 6, and are summarized in Fig. 9.16.

No study has yet (as of 2012) been published with enough ⁸¹Kr data for a detailed comparison, but the number of available ⁸¹Kr data will probably increase soon, and in view of the comparably low effort needed, measurements of ³⁶Cl will probably always be included for the same samples. Since ³⁶Cl and ⁸¹Kr have very similar half-lives, their evolution with increasing idealized groundwater age should follow a straight line with a slope close to one as indicated by the thin black line (Fig. 9.16). As was shown for radiocarbon and ³⁶Cl, the comparison of ⁸¹Kr and ³⁶Cl should enable the determination of 'initial' ³⁶Cl/Cl ratios. Furthermore, small deviations of measured values from the straight line may be attributed to secular variations in the initial ³⁶Cl/Cl ratio. Possible reasons were discussed in Chapter 6 and may include variations in proximity of recharge areas to marine coastal areas resulting from changes in sea level, or variations in cosmic ³⁶Cl production. Addition of chlorine from sediments will influence only the ³⁶Cl/Cl ratio but not ⁸¹Kr, and should be visible as a horizontal shift towards lower ³⁶Cl/Cl ratios as indicated by the green arrow (Fig. 9.16). More problematic for the ages but nearly invisible in the plot are mixtures of waters with different age. These are evident for tracers with very different



FIG. 9.16. Comparison of ³⁶Cl/Cl and ⁸¹Kr, and possible changes in one or both tracers relevant for age dating.

timescales because the evolution according to idealized age creates a very convex curve. Since both ³⁶Cl and ⁸¹Kr radioactively decay with similar half-lives, the plot of ³⁶Cl versus ⁸¹Kr creates a straight line. Mixtures will also follow this line and with the present accuracy in measurement and interpretation will not be detectable. In addition, invisible in the plot of ⁸¹Kr versus ³⁶Cl is a possible loss of ⁸¹Kr and ³⁶Cl by diffusion into aquitards. This process was described in Chapter 5 and will influence both isotopes in a similar manner, since their diffusion constants are not very different.

9.3.3. Linear accumulating tracer versus exponential decay tracer

Chapter 8 discussed and demonstrated many of the uncertainties connected with the use of helium as a tracer for age dating. However, despite these uncertainties, helium has some significant advantages. First, due to its linear increase with time, its concentration changes during mixing the same way as average age changes during mixing. Second, a stable isotope which is produced linearly with time has no limit concerning the dating range. This allows helium results to be compared both with ¹⁴C and with ⁸¹Kr and ³⁶Cl. Finally, helium can be measured with much less cost than ³⁶Cl and ⁸¹Kr, even if the ³He/⁴He isotope ratio and Ne concentration are to be determined as well. This allows helium to be applied to a larger number of samples than might be possible for measurement of ¹⁴C, ³⁶Cl or, particularly, ⁸¹Kr.

The comparison of the linearly increasing tracer helium with the tracers observing radioactive decay, such as ¹⁴C, ³⁶Cl and ⁸¹Kr, in some aspects is similar to the case of comparing ⁸¹Kr with ³⁶Cl, but there are some very important and sometimes useful differences, which are illustrated in Fig. 9.17.

In the simplest case, helium concentrations increase only by in situ production or by a constant flux at a constant rate and the radioactive tracer decreases only by radioactive decay due to idealized age. In this case, the plot of excess helium (see Chapter 8 for the definition of excess helium) versus the log of a radioactive tracer should display a straight line, starting at a point where the radioactive tracer has its initial condition and at an excess helium value of zero. The slope of this line is a function of the in situ production rate and the radioactive decay constant only. The in situ production rate, as described by Eq. (9.3), can vary within a single aquifer due to changes in U and Th content, and probably differs between different aquifers. This implies that different aquifers may have different slopes, as indicated with the blue and black line of in situ production in Fig. 9.17.



FIG. 9.17. Plot of helium versus a radioactive tracer concentration, with development lines due to the different processes in in situ production, external flux, mixing and helium loss.



FIG. 9.18. Helium in comparison with the radioactive tracers ¹⁴C and ⁸¹Kr. Blue lines represent the piston flow model. Black dots represent tracer values as computed with the Tóth model and presented in Section 9.1.2. In the left panel, black dots display profile A2 in infiltration area at $x = 14\,000$ m; in the right panel, a depth profile with same screen depths, but located at x = 2000 m. Small black diamonds represent binary mixtures between pairs of screens of these depth profiles. Low ¹⁴C values in the left panel are fixed to be not smaller than a practical detection limit of 0.1 ± 0.1 pmc.

As waters grow older along a flowline, helium from external sources, such as the 'crustal flux' discussed in Chapter 8, will become prominent and these external sources will generally show a much higher slope in Fig. 9.17. Of course, the slope of the in situ production might also vary due to different uranium and thorium contents of the aquifer rocks. However, a different in situ production is generally a smaller variation (around a factor of two to five typically) as compared to external fluxes, which was described to be as much as a factor of 70 higher than in situ production in Chapter 8. If helium is lost to overlying formations as well, then a balance of influx and diffusive loss may be reached, resulting in constant helium concentrations with further increases in age. This, in most cases, will require very large timescales.

On the timescale of radiocarbon, another process is important, which applies to samples approaching the dating limit for radiocarbon. The analytical detection limit for radiocarbon may be as low as 0.1 pmc. However, in practice, this corresponds to an admixture of less than 0.1% young water, and such 'clean' samples may be difficult to obtain. Regardless of whether the practical detection limit is 1 or 0.1 pmc, eventually the ¹⁴C detection limit will be reached along the flowline. In this case, the samples will follow the vertical green arrow indicated in Fig. 9.17, because the radiocarbon value will not decrease further and the helium concentration will continue to increase with time.

Mixtures of waters with a different age along a single in situ production line will be difficult to detect: they will manifest themselves by following an evolution that is linear for both tracers in Fig. 9.17 instead of an exponential evolution for radioactive decay. On a semi-logarithmic plot, this linear relation is a curved line which does not differ very much from the straight line. Admixtures of waters which are beyond the dating range for the radioactive tracer, however, will plot above the in situ production line. Mixtures will also be discernible if waters with considerable contributions from external sources mix with those still on the in situ production line. These cases are indicated by red double-arrows in Fig. 9.17.

The case of mixtures can also be easily demonstrated using the infiltration depth profile A2 at $x = 14\ 000\ \text{m}$ in the Tóth aquifer and is shown in Fig. 9.18: the waters in the underlying regional flow system are beyond the dating range for radiocarbon. To illustrate their possible radiocarbon values, taking into account that their measurement uncertainty is different from zero, a random number of $(0.1 \pm 0.1)\ \text{pmc}$ was added to the model results computed and displayed in Fig. 9.8.

It is evident from the left plot in Fig. 9.18 that binary mixtures between pairs of different screens do not follow the in situ production line in the plot versus radiocarbon. Mixtures can, thus, be easily identified. In the plot of binary mixtures of different screens for the tracer pair ⁴He versus ⁸¹Kr, however, these fall close to the in situ production line (right panel in Fig. 9.18). Here, a depth profile at x = 2000 m was chosen to display larger ages. Ages of waters are not beyond the dating range of ⁸¹Kr in this case. Therefore, mixtures of waters with different age plot very close to the lines of the piston flow model and to the Tóth screens. Mixtures will not be detectable with the right plot in Fig. 9.18.

9.3.4. Noble gas patterns

Water in solubility equilibrium with the atmosphere has helium concentrations between 3×10^{-8} and 5×10^{-8} cm³ STP/g, the former value being for 25°C and 2500 m above mean sea level and the latter at sea level for a temperature of 0°C. This value and the presence of a possible excess-air component (see Chapter 8 for details) can be determined with an accuracy of better than 10%, which means that excess values of ⁴He as small as 6×10^{-9} cm³ STP/g can be detected. With the in situ production of 6×10^{-11} cm³ STP · g⁻¹ · a⁻¹ used in this chapter, this implies that the excess helium concentration of a water with an idealized age of 100 a or larger may be detectable. While this is not an age within the scope of the present book and although the estimate may vary from aquifer to aquifer, such small helium excess values may be of interest for other tracers; if attempts are made to determine the initial ¹⁴C value from a plot of CFCs or tritium versus ¹⁴C as shown in Fig. 9.15, it is surely of interest if the CFC or tritium value represents an unmixed sample or one with a contribution of water older than 100 a. To obtain this kind of information, a plot of neon versus helium is useful, which is indicated in Fig. 9.19.

Helium and neon in solubility equilibrium plot along a curve on which the noble gas content is given for a range of (infiltration) temperatures, indicated with blue crosses. The black straight line



FIG. 9.19. Neon versus helium concentration with lines for solubility equilibrium, excess air and excess helium.



FIG. 9.20. Helium isotope mixing plot. Data are identical to those in Fig. 8.10.

indicates excess air added to the solubility concentration at 8°C. Most samples — here from a case study with young waters — plot along this excess air line. Some samples, however, show higher values as indicated by a horizontal shift to the right, towards higher helium concentrations. This can help to further constrain details, when plotting tracers of different timescales versus each other, as in Figs 9.14 and 9.15. In case these samples shifted to the right in Fig. 9.19 contain tritium, they should be regarded as mixed and, for example, not be used to determine initial ¹⁴C values in Fig. 9.15. Of course, a similar plot is possible with any other noble gas instead of neon, for example Ar or Kr.

Very old water contains so much helium, that the equilibrium and the excess air lines are not discernible from the y axis in this plot. In the case of old water, another plot is useful (similar to the Weise plot in Fig. 8.10) and is demonstrated in Fig. 9.20.

In Fig. 9.20, the measured ³He/⁴He isotopic ratio is plotted versus the Ne/He ratio. Together with the data, several lines are plotted: the green vertical line displays additional ³He as produced by radioactive decay from tritium. The blue and red lines display the concentration and isotope ratio of solubility equilibrium (Weiss (1971) [524]), and excess air, respectively. The blue line is horizontal and nearly coincides with the excess air line because any isotope fractionation during solution as well as its temperature dependence is nearly invisible on the scale of this plot (Benson and Krause (1980) [592]). The place where all lines meet corresponds to the ³He/⁴He isotopic ratio of air and to the (slightly temperature dependent) Ne/He ratio in equilibrium with the atmosphere. The red and purple lines are mixing lines of this equilibrium helium with excess helium of different isotopic composition, namely with a ${}^{3}\text{He}/{}^{4}\text{He}$ ratio of 1×10^{-6} and 1×10^{-7} . This plot, as compared to Fig. 8.10 (Weise and Moser (1987)) [562]), has the advantage of displaying only measured values, without needing any model for excess air correction. It is, therefore, a better choice to plot a whole data set at an early stage, if the mechanism of excess air correction is still under discussion or if perhaps different mechanisms of excess air and different infiltration temperatures are possible. Figure 8.10, in contrast, should be used if the excess air model is well constrained, because then the characterization of ³He/⁴He ratios in the external sources is sharper. The important patterns, however, are discernible in both plots, and the isotopic ratio of the excess helium component can be estimated from both plots. If neon measurements are not available, a similar plot can be produced for any other noble gases as nominator (e.g. Ar), or even choosing 1/He as the x coordinate.

Chapter 10

NUMERICAL FLOW MODELS AND THEIR CALIBRATION USING TRACER BASED AGES

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10.1. INTRODUCTION

Any estimate of 'age' of a groundwater sample based on environmental tracers requires some form of geochemical model to interpret the tracer chemistry (Chapter 3) and is, therefore, referred to in this chapter as a tracer model age. The tracer model age of a groundwater sample can be useful for obtaining information on the residence time and replenishment rate of an aquifer system, but that type of data is most useful when it can be incorporated with all other information that is known about the groundwater system under study. Groundwater flow models are constructed of aquifer systems because they are usually the best way of incorporating all of the known information about the system



FIG. 10.1. Flow chart of the groundwater flow modelling process (after Reilly (2001) [72]).

in the context of a mathematical framework that constrains the model to follow the known laws of physics and chemistry as they apply to groundwater flow and transport. It is important that the purpose or objective of the study be identified first before choosing the type and complexity of the model to be constructed, and to make sure such a model is necessary. The purpose of a modelling study is most often to characterize the system within a numerical framework, such that the hydrological responses of the system can be tested under potential stresses that might be imposed given future development scenarios. As this manual discusses dating as it applies to old groundwater, most readers are likely to be interested in studying regional groundwater flow systems and their water resource potential.

Model development occurs in stages (Fig. 10.1) where the model developer must (i) define the problem and the purpose for the model; (ii) develop the conceptual model; (iii) design the model grid; (iv) calibrate the model (adjusting the hydraulic parameters to fit the available data); and (v) apply the model to predict future responses. In some cases, the purpose of the model may be only to improve the understanding of the flow system, in which case stage (v) might never be employed. Given the high uncertainties associated with future predictions based on most models that have relatively limited data and complex hydrogeology, models are often most useful when used to understand and quantify the flow system at the end of stage (iv), or when the results of the predictions are still useful in spite of large accompanying error bars. All models represent systems based on data that are currently available, and so many studies require a return to the data collection phase after an initial model reveals where additional data are needed to improve model predictions. This feedback between data and modelling results is often carried out as an interaction between the hydrologist constructing the model and the geochemist collecting and analysing the data. It is important for the two to have good communication and a working relationship. The feedback can happen both ways - the data control how the model is developed, and the model results can indicate where and what type of additional data need to be collected. This chapter will cover the basics of model design, development and calibration, especially with the use of tracer model ages.

10.2. EQUATIONS AND NUMERICAL METHODS

A groundwater flow model describes the distribution of heads within an aquifer system based on the solution of the fundamental groundwater flow equation, which can be derived solely from the principles of mass balance and Darcy's law. A general form of this equation for three dimensions, transient flow and constant fluid density can be written as:

$$\frac{\partial}{\partial x}\left(K_{x}\frac{\partial h}{\partial x}\right) + \frac{\partial}{\partial y}\left(K_{y}\frac{\partial h}{\partial y}\right) + \frac{\partial}{\partial z}\left(K_{z}\frac{\partial h}{\partial z}\right) = S_{s}\frac{\partial h}{\partial t} - Q(x, y, z, t)$$
(10.1)

where

h	is the hydraulic head within the flow system;				
$K_{\rm x}, K_{\rm y}$ and $K_{\rm z}$	are hydraulic conductivity in the x, y and z directions, respectively;				
$S_{ m s}$	is the specific storage;				
Q	is a general source (+) or sink (-) of water to the aquifer system that can vary in space and time to represent injections or withdrawals at points in space or over regions				
	or boundaries;				
t	is time.				

The derivation of this equation can be found in standard textbooks on hydrogeology (Domenico and Schwartz (1998) [8]; Schwartz and Zhang (2003) [593]).

To solve this partial differential equation, a description of the hydraulic properties (K and S_s) are needed in three dimensions, head and/or flux conditions at the boundaries of the domain, and initial conditions at the simulation starting time. For steady state conditions (often assumed for aquifers

under pre-development conditions), the left term on the right side of Eq. (10.1) becomes zero and the specific storage is not a required parameter, nor is an initial condition required. The solution to this equation gives the distribution of head, h, in three dimensions, and then by using Darcy's law, flow rates within the aquifer can subsequently be calculated. The seepage velocity (that taken by a solute or water molecule) is the specific discharge divided by the porosity and, therefore, by using an estimate of porosity, one can simulate a velocity field within the aquifer by first solving the flow equation. Given two points within the system along a flow path, the seepage velocity between those points divided by the distance yields a time of travel for water or, if the point of origin is the water table, a flow model age.

In some cases, it may be useful initially to consider the flow system as having a simple geometry and boundary conditions, to the extent that an analytical solution might be available. An analytical solution is a continuous solution across the domain where the head or hydraulic (or flow model) age value, for example, can be evaluated at any point. For some simple flow systems, the distribution of the flow model age can be represented by such a function (Cook and Böhlke (1999) [594]). A number of other analytical solutions have been taken from the heat flow literature (Carslaw and Jaeger (1959) [539]), as heat flow is mathematically analogous to fluid flow in porous media. In most cases though, the geometry, boundary conditions and hydraulic parameter distribution are complicated to the extent that no analytical solution exists. For these cases, a numerical solution is the next best alternative. A numerical solution to the flow equation is a distribution of head values at a finite number of discrete, pre-specified points (or nodes) within the aquifer system. The two numerical solution techniques most commonly used to solve the flow equation are finite difference and finite elements. The former requires the user to define a rectangular grid of points or cells at which the solution will be obtained, and the latter requires points that are connected by elements that are usually triangular or rectangular in shape, but not necessarily arranged along a regular grid. The more points in the grid, the more detailed and accurate the solution to the equation, but the more computer time and storage are required. With current computer capabilities, it is possible to have of the order of one million nodes in a grid. Finite elements provide the flexibility of arranging the nodes freely to fit the geometric features of the system, but such an arrangement requires more sophisticated graphical user interfaces to construct the 'mesh', as this could not be reasonably constructed manually if the node number were in the thousands or more.

Many modelling codes have been developed that solve the equations of groundwater flow and solute transport, most of which are adequate for modelling a groundwater system. The only codes chosen to be listed here are those published and supported by the United States Geological Survey (USGS), not because they are necessarily superior, but because they have been the most widely used in the world (and, thus, widely tested), and perhaps more importantly for this manual because the codes and their user guides can all be downloaded free from the Internet (http://water.usgs.gov/software/). The most widely used groundwater flow code has been MODFLOW (McDonald and Harbaugh (1988) [71]), of which the latest release is MODFLOW2005 (Harbaugh (2005) [595]). The code uses integrated finite differences and has a number of different 'modules' that can be used to incorporate different conceptual grid designs and different types of boundary conditions. One recent addition to MODFLOW is the ability to refine the grid in subdomains of local interest within a more regional coarse grid in a process known as local grid refinement (Mehl and Hill (2005) [596]; Mehl and Hill (2007) [597]). Several graphical user interfaces for MODFLOW are available on the open market, but the USGS has also created one recently (Winston (2009) [598]) that is free of charge. Viewing three dimensional results from MODFLOW is possible through the post-processing programme MODELVIEWER (Hsieh and Winston (2002) [599]).

10.3. AQUIFER GEOMETRY AND GRID DESIGN

Once a decision has been made to create a numerical model of an aquifer system, one of the first steps is to begin to conceptualize how the system will be represented by a grid or mesh of nodes. A basic understanding of the aquifer system and its geometry (Chapter 2) should be obtained before this grid

is created. Although three dimensional simulation is now tractable computationally for most systems, sometimes a two dimensional model may be sufficient to meet the desired objective, or it may serve as a good preliminary model that will provide some key understanding for a much smaller investment of time and resources. A two dimensional areal model could be appropriate for an aquifer that is essentially a single hydrogeological layer. On the other hand, in sedimentary basins, a two dimensional cross-section along a flowline can often provide the necessary vertical detail between multiple aquifers and aquitards, and can be simulated such that a great deal is learned about the contrast between the hydraulic conductivity of layers and how flow model ages would be influenced by such contrasts.

If a three dimensional model is to be constructed, some thought must go into how finely the layers are to be discretized in the vertical dimension, and how to balance the vertical resolution requirement with the horizontal grid resolution that is desired to represent landscape features. Aquifers and aquitards can be represented by single layers, but if solute transport and dispersion are to be represented (Chapter 10.8), more than one model layer per hydrogeological layer is usually desirable. There are many issues to consider in grid design (Anderson and Woessner (1992) [600]). All of the boundaries of the flow system of interest must be identified; sometimes, these boundaries are at a substantial distance from the sections of the system that are of most interest. Some hydrologists prefer the analytical element method (Haitjema (1995) [601]) in this case, which can more efficiently handle distant boundary conditions. Finite elements can be arranged to fit boundaries exactly. As finite difference grids are rectangular by nature and flow systems are not, certain sections of the grid will ultimately be outside of the flow system and must be characterized as inactive cells. Refinement of the grid in certain subdomains can be accomplished either by using a finite element method or local grid refinement with finite differences. Grid refinement can also be accomplished with finite differences by using variable grid spacing, which is usually a standard option, but this is somewhat less efficient (although less complicated) than using local grid refinement.

Hydrogeological units in sedimentary basins can be represented either by having them coincide exactly with model layers (Fig. 10.2), or by treating them independently and then calculating the effective hydraulic parameters for each model cell depending on how the model layers intersect the hydrostratigraphy. The latter approach can be more efficient when dealing with highly complex stratigraphy, and has been made easier with the development of software specifically designed for this purpose (Anderman and Hill (2000) [602]; Anderman and Hill (2003) [603]). Finite element models are better designed to handle hydraulic conductivity fields whose directions of maximum and minimum values do not coincide with the rectangular grids of finite-difference methods (e.g. Yager et al. (2008) [604]).

10.4. BOUNDARY CONDITIONS

In order to solve the flow equation for the domain of interest, boundary conditions must be specified at the domain boundaries. Mathematically, these boundary conditions take the form of constant head, specified flux or mixed type. In order to create a model that simulates the conditions that occur in the real system, the real hydraulic boundaries must be expressed in terms of one of the three mathematical types.

Constant head is for boundaries where the head will remain constant no matter what stress is placed within the system; the internal changes in head will not affect the head at this boundary. An ideal example of this would be a large body of water, such as the ocean, that has such a large reservoir of water whose level will not be affected by changing flow conditions within the domain. Specified flux can represent a number of different field conditions. On the external boundaries, a flux of zero represents an impermeable surface. This is often the condition placed on the bottom boundaries or lateral edges of the domain. A groundwater divide would also represent a specified flux of zero. Recharge at the top boundary is a very common flux that is specified at the top boundary of the domain. Recharge can be distributed across the top of the model in a fashion that is consistent with field conditions. In humid



FIG. 10.2. A discretized hypothetical aquifer system (modified from McDonald and Harbaugh (1988) [71]).

climates, this is often represented by a rather even distribution of recharge across the domain, whereas in arid climates recharge is more often distributed at focal areas such as along mountain fronts or in ephemeral streams. Internal specified fluxes can be used to specify withdrawal or injection rates of water at individual wells.

Mixed type boundary conditions represent situations where the head at the boundary of the system may change, but only in a manner that can be described directly by an equation containing a head value outside of the boundary and a hydraulic conductance term across the boundary. Although a large river could be specified as a head, it could also be specified as a mixed type where the flux through the river bed sediments is a function of the vertical hydraulic conductivity of the river bed and the head in the river. A drain or seepage face is another type of mixed boundary where outflow is allowed to occur as a function of the soil conductance when the head in the aquifer exceeds that of the drain or land surface, but inflow is prohibited if the head in the aquifer is below that of the drain or land surface. Evapotranspiration directly from the groundwater can be specified as a mixed type boundary condition where the evapotranspiration upward flux varies depending on three different head conditions. When the head is below the root zone, the flux is zero. When the head is above land surface, the flux is at a maximum value that is plant and climate dependent. When the head is somewhere in between the bottom of the root zone and the land surface, the evapotranspiration flux varies between zero and the maximum value. A leaky confining layer can be represented as a mixed type boundary, where the head in the aquifer across the layer is specified and the boundary conductance is represented by the hydraulic conductivity of the layer divided by its thickness. See McDonald and Harbaugh (1988) [71] for more details of the application of these various types of boundary conditions.

10.5. TRANSIENT SIMULATIONS

Transient simulations are for situations where the effects of hydraulic stresses need to be followed over time. This corresponds to the situation where Q and h in Eq. (10.1) are time dependent Q(t) and h(t). The simulation is then discretized into time steps that follow a given timeline and stresses are defined as to how they change over time. An initial condition of head everywhere in the model domain is required. Extractions from wells are often added to aquifers over time as pumping rates change. Under these conditions, the specific storage (Eq. (10.1)) of the rocks or sediments is also a required hydraulic parameter for the simulations. For water table aquifers, the specific yield is also required. The specific yield is the volume of water that drains from an unconfined aquifer per unit surface area of aquifer per unit decline in the water table. The value will, in general, be somewhat less than the porosity of the aquifer near the water table. In addition, heads at boundary conditions may change over time. Recharge may change over short time periods, such as seasons, or over very long time

periods, as the result of climate change. For regional systems where old groundwater has been dated, the travel times of the groundwater are usually of the order of thousands of years or more. In these cases, simulating steady state conditions as they existed before aquifer development began is frequently the approach taken. It is often more realistic for long time periods if a transient simulation is chosen and recharge is varied to simulate changing climate, during the recent ice age, for example.

10.6. MODEL CALIBRATION

The objective of most groundwater modelling studies is to create the best numerical model of the aquifer system possible given the available data on the hydraulic characteristics of the system. Adjusting the hydraulic parameters of the model until a best or satisfying fit to the observed data is achieved is known as the 'model calibration' (Hill (1998) [605]; Hill and Tiedeman (2007) [606]). This should not be confused with the terms 'model verification', which refers to the testing of the mathematics in the code to solve the equations accurately, and 'validation', which refers to the general process of producing a model that is 'valid' or represents the system well - although, in a strict sense, groundwater models cannot be validated (Konikow and Bredehoeft (1992) [607]). The hydraulic parameters that need to be adjusted during calibration include the hydraulic conductivity of the hydrogeological units and potentially its distribution within the units, recharge and its distribution, and specific storage for transient problems. Observed data almost always include head measurements and some type of measurements or estimates of flux. Some knowledge of the hydraulic properties of the rocks or sediment is often known a priori, as is some estimate of recharge. This is frequently referred to as prior information. As prior information is usually obtained from small scale or local tests or studies, and a model is most often developed to represent a large scale or regional system, the prior information is not usually assigned directly to the parameters, but rather serves as a guide for reasonable values within which the parameters should be adjusted during the calibration process.

As the model is based on Darcy's law, using only heads and head gradients as observations will result in a very, if not completely, non-unique calibration. The head gradient is based on the ratio of the flux to the hydraulic conductivity, so using head values alone will only constrain the ratio of flux to hydraulic conductivity, not individual values of either. Thus, some type of flux observation needs to be included in addition to heads. The most common flux observation used is the baseflow to a stream. The baseflow is directly related to the long term recharge in the stream's watershed. Although recharge is also a flux, it usually cannot be measured directly as an observation, especially in an integrated manner over space and time, and so it is often adjusted as a parameter of the model. Tracer model ages give information on the travel time (flux) within the system, and so can also be used in addition to hydraulic head data, or in addition to both hydraulic-head and base flow data to calibrate a model.

The simplest approach to calibrating a model is by trial and error. It is recommended to start with a simpler model and add complexity over time as the data permit. If there are only a few parameters in a model to adjust, they can be adjusted by hand to create the model that best fits the observed data. For any given set of parameter values, the model is run and the simulated values at the observation locations are compared with the data collected from those observation locations. The goal is to minimize the error difference between the simulated and observed data, most often done by calculating the sum of the squared errors (or some similar quantity). As computers have become faster, they have allowed models to become more complex to the point that they can include dozens or more parameters (usually these are different values of hydraulic conductivity in different units and regions of the model). Automated parameter estimation codes have been developed to greatly accelerate the calibration process (Doherty (2004) [608]; Poeter et al. (2005) [609]). These codes are shell programmes that are able to call any model and keep adjusting the parameters and rerunning the model in a direction that leads to the minimization of the total sum of squared errors. This is done through a continuous cycle of (i) changing the parameter values in the input files, (ii) running the model and (iii) examining the simulated observations. The result is a set of parameters that gives a model with the best fit to the data. However,

the best fit does not always indicate the best model and the calibration process must be guided carefully to avoid erroneous parameter values (Hill (1998) [605]; Reilly and Harbaugh (2004) [610]).

10.7. CALCULATION OF FLOW MODEL AGES

In order to use tracer model ages to calibrate a model, the model must be able to simulate a flow model age. Alternatively, a tracer concentration at any given point (usually a well or spring) can be simulated and compared directly with the measured concentrations, an approach discussed in Section 10.8. One simple and straightforward way to obtain an age from a flow model is to calculate it as a hydraulic time of travel. This is done by dividing the distance between two points along a flowline by the interstitial velocity calculated using Darcy's law. In a discretized groundwater model, this is done over regional distances by calculating the advective path line that an imaginary particle of water will travel along through the aquifer from one model cell to the next, and the time required to move along the path line given the hydraulic conditions defined in the model. Solute dispersion within the groundwater system for this type of calculation is neglected, and although this is not reality, and it is known to introduce some error during a calibration process, that error is often small relative to the uncertainties in the hydraulic properties of the system. Finite difference groundwater models are aptly suited for the calculations of such path lines and flow model ages. Velocities at cell boundaries can be calculated from the head values at the cell nodes using Darcy's law and a specified porosity. A particle of water can be followed from cell to cell, either forwards or backwards, from any specified starting point based on the calculated velocity field for the model grid. A post-processing programme (MODPATH; Pollock (1994) [611]), available for use with MODFLOW, calculates such path lines and travel times. To calculate a unique path that a particle of water would follow across a finitedifference cell, the assumption is first made that the velocity along each coordinate direction varies only in that coordinate direction and not along the other directions (Fig. 10.3). This assumption allows the simplification of the calculation of the distance travelled to the far side of a cell as a smooth curved path. The time required to traverse that distance in the *x* direction becomes:

$$\Delta t = \left(\frac{\Delta x}{V_{x2} - V_{x1}}\right) \ln\left(\frac{V_{x2}}{V_{xp}}\right)$$
(10.2)

where

 Δt is the travel time to the far side of the cell; Δx is the distance to the far side the cell;

 V_{x2} is the velocity at the far cell wall;

 V_{x1} is the velocity at the near side of the cell;

 V_{xp} is the velocity at the *x* location of the particle.

The integration of the changing velocity across the cell yields the natural log term in Eq. (10.2). A similar equation is written for the y direction. Whichever Δt is less (x or y) is the time of travel to the cell wall at the point the particle exits the cell. The exit point can then be calculated and the exit point becomes the entrance point of the neighbouring cell. The particle is, thus, tracked through the cells until a discharge cell is reached (or a recharge cell if backward tracking is being used). Full details on these particle calculations can be found in Pollock (1994) [611]. For finite element models, the velocity is usually regarded as a constant across any given element, and so similar travel times could be calculated for particles to traverse elements. No such software has, however, currently been developed for the widely used finite-element code SUTRA.

Hydraulic path line simulations can be made either in the forwards or backwards direction. Thus, in MODPATH, the time of travel of a particle can be calculated from the water table forwards to its



FIG. 10.3. Schematic showing the computation of exit point and travel time for the case of two dimensional flow in the x-y plane (after Pollock (1994) [611]).



FIG. 10.4. Simulated flow paths and flow model ages in the Middle Rio Grande Basin in comparison with ¹⁴C model ages (after Bartolino and Cole (2002) [612]).

discharge location (e.g. a stream) or the time of travel can be calculated from a well screen backwards to its recharge location (e.g. the water table). The latter can be used to calculate a flow model age at any point within an aquifer system given the set of parameters currently being assigned to the model. For a transient flow model (e.g. with transient recharge), the procedure has the added requirement of storing the flow field at each time step. Flow model ages can be calculated for multiple sites at a time and, therefore, a set of tracer model ages can be compared with the flow model ages (Fig. 10.4) intermittently as parameters are adjusted during the calibration, and the errors can be added to the total sum of squared errors being calculated for the model calibration. For long screen wells, multiple particles can be simulated along the well screen, with the result being a range of different flow model ages assigned to and 'mixing' in the well bore. It should be noted, however, that for environmental tracers it is the concentration of the solute species that is actually mixing and not idealized groundwater ages. For tracers where the solute or isotopic concentrations are not linear functions of time, the average of the flow model ages will not give the equivalent result to the more appropriate average of simulated concentrations that are each back calculated from the flow model ages. A useful visualization technique is to start particles at the centre of every cell in the model and track backwards to the origin location. All of the travel times for these paths are then plotted at their starting cell locations. The result is the flow model age distribution throughout the entire system that can be visualized in two dimensions as maps of flow model age across an entire model layer or cross-sections (e.g. Fig. 13 of Sanford et al. (2004) [47]).

10.8. SIMULATION OF DISPERSION AND APPARENT GROUNDWATER AGE

Advective path lines and flow model ages are straightforward to calculate following groundwater flow simulations, but environmental tracers are subject to hydrodynamic dispersion as well as advection. Dispersion of a solute occurs because heterogeneity in the hydrogeological framework creates variations in velocities from the pore scale to the field scale. These heterogeneities are inherently present but too small to discretize all into the model domain. A potentially more accurate model calibration can be undertaken if the effect of the dispersion on the tracer is also known and simulated. Such a simulation could produce dispersion model ages, as opposed to the previously discussed flow model ages, which are strictly advection model ages. The advection–dispersion transport equation can be written with concentration as the dependent variable and groundwater velocity as a parameter in cartesian–tensor notation as:

$$\frac{\partial}{\partial x_i} \left(D_{ij} \frac{\partial C}{\partial x_j} \right) - \frac{\partial}{\partial x_i} \left(CV_i \right) = \frac{\partial C}{\partial t} + C'Q + R$$
(10.3)

where

C is concentration;

- V_i is the seepage velocity;
- C' is the concentration of a fluid entering the domain at rate Q;

R is the chemical reaction rate of the solute or isotopic species;

 D_{ij} the hydrodyanamic dispersion tensor, which is a function of the velocity components in each direction, the dispersivity and molecular diffusion (Konikow and Grove (1977) [613]).

The velocity field is predetermined from the flow simulation and can vary in space and time. The source term Q and reaction term R can also vary in space and time. The dispersivity is a parameter that describes the inherent make-up of the porous or fractured media that causes spreading, and is usually assumed to simplify into two components, a longitudinal dispersivity that is parallel to the direction of flow and a transverse dispersivity that is perpendicular to the direction of flow. In three dimensional flow systems, two different transverse dispersivities can be used that are perpendicular to each other.

Several codes have been developed that solve Eq. (10.3) (Koch and Prickett (1993) [614]; Konikow et al. (1996) [615]; Voss and Provost (2002) [616]; Zheng and Wang (1999) [617]). The numerical methods used are either Eulerian (fixed reference frame) or Lagrangian (moving reference frame), or a combination of the two. Eulerian techniques include finite differences or finite elements, whereas Lagrangian techniques include random walk or the method of characteristics. The nature of Eq. (10.3) is such that in systems with a high ratio of velocities to dispersivities (known as the Peclet number) Eulerian mathematical solutions (e.g. standard finite differences or finite elements) become unstable. Thus, when simulating transport with dispersion, special care must be taken to make the grid fine enough to avoid numerical oscillations or numerical dispersion. The random walk method tracks a large number of particles, most often from a point source, and randomly adds variability to the particle path in directions both longitudinal and transverse to the flow direction (Prickett et al. (1981) [618]). As this method requires large numbers of particles to get repeatable results, it is not often feasible to use in regional transport problems where tracer model ages are measured. The method of characteristics was developed as a particle tracking technique with the advantage of particle tracking, but with a Eulerian dispersion component, but it has its own set of inherent limitations (Konikow and Bredehoeft (1978) [619]). For all of these methods, the fine resolution requirement of the grid often precludes full three dimensional advection-dispersion simulations of an aquifer on a regional scale.

The final term of Eq. (10.3), *R*, represents the chemical reactions that the tracer of interest may be involved in that either remove it from or add it to the solution. Radioactive decay is the most common of these that would be included for environmental tracers when the objective is to simulate the concentration field of the tracer directly. Carbon-14 has a number of potential reactions and exchanges that can take place with the mineral phase in the aquifer material (e.g. Kalin (1999) [111]; see Chapter 4), and such reactions could also be included if the ¹⁴C concentration field were to be simulated directly. Geochemical codes are available that solve multiple species reactions with transport in one (PHREEQC; Parkhurst and Appelo (1999) [149]) or more (PHAST; Parkhurst et al. (2004) [200]) dimensions. Each of the tracers that might be used to date old groundwater that are described in this book have their own set of issues to be considered when using their tracer model ages in conjunction with a flow and/or transport model. A list of these tracers and the issues are listed in Table 10.1. A more general table of old age tracers are listed in Table 1.1.

Reviews of field studies by Gelhar (1986) [620] and Schulze-Makuch (2005) [621] have suggested that dispersivity is scale dependent and that the longitudinal dispersivity is roughly about 10% of the distance of travel; however, the most detailed field studies (LeBlanc et al. (1991) [622]) suggest that this may greatly overestimate dispersivity, which can often be closer to 1% of the distance of travel. Transverse dispersivity is typically 1–10% of the longitudinal dispersivity. Dispersivity almost certainly also varies spatially within most formations and is difficult to measure directly without special tracer tests, so although dispersion can be simulated, the uncertainty with respect to the accuracy of simulated concentration fields is usually high. One regional effect is that under steady state conditions

TABLE 10.1. TRACER METHODS AND ISSUES TO CONSIDER FOR JOINT USE WITH NUMERICAL FLOW MODELS

Tracer method	Issues to consider
¹⁴ C	Long term variable input, definition of initial ¹⁴ C, often reactive, dispersion, matrix diffusion
Не	Generated in situ, uncertain production rate, quantifying basin flux
³⁶ Cl	Long term variable input, mixing with other Cl sources, matrix diffusion
⁸¹ Kr	Input variations only in the very long term, sampling still difficult at the time of the publication of this book
U	Generated in situ, uncertain production rate



FIG. 10.5. The effect of dispersion on the patterns and magnitudes of flow model ages. Dashed lines are equipotentials. Arrowed lines are flow directions. Solid lines without arrows are contours of equal advection or dispersion model age (in years). Grey regions have lower hydraulic conductivity. (Modified from Goode (1996) [69]).

(not always applicable) the flow model age of groundwater is not a function of the interchange (transverse dispersion) of solutes between aquifers and interbeds, but simply a function of the ratio of the total porosity of the system to the porosity of the aquifer (Bethke and Johnson (2002) [623]; Sanford (1997) [207]). For tracers with long half-lives (e.g. ¹⁴C and ³⁶Cl), the relatively constant (or slowly changing) input function through time creates a condition where the longitudinal dispersion of the solute is relatively small (5–10%) relative to its decay rate (Johnson and DePaolo (1996) [624]), indicating that advective path line and flow model age calculations may not be a bad assumption for many old groundwater simulations.

In spite of the uncertainty associated with the simulation of dispersion in groundwater, hypothetical simulations can illustrate well the expected behaviour on environmental tracers. When possible, it is most straightforward to simulate the tracer of interest, as each tracer may have a different input function or reactive behaviour in the subsurface. These individual tracer characteristics can be included directly in the simulation parameters. A more generalized approach is also possible where a dispersion model age can be simulated directly (Goode (1996) [69]) by setting R in Eq. (10.3) to a value of one, and Q to zero. This approach is often known in the modelling community as 'direct age simulation'. The reaction term R is used to represent the passing of time and the concentration field becomes the dispersion age field. Much discussion has surrounded the simulation of dispersion model ages in this manner (Bethke and Johnson (2008) [84]; Perrochet and Etcheverry (2000) [625]; Varni and Carrera (1998) [83]). The technique for simulating the dispersion model age can also be used to calculate the frequency distribution of groundwater ages expected to be encountered at a sampling site such as a long screened well (Varni and Carrera (1998) [83]). A dispersion model age simulation is useful for visualizing the potential impact of dispersion on advection model age simulations (Fig. 10.5). This approach is also useful for finite element models that do not have advection model age calculation software available. From Fig. 10.5, it can be seen that dispersion spreads out the transport model age

and typically reduces the size and magnitude of pockets of old water that may result from stagnant regions of circulation.

10.9. MODEL CALIBRATION USING TRACER BASED AGES

A number of regional modelling studies have used tracer model ages effectively as constraints (e.g. Castro et al. (1998) [96]; Park et al. (2002) [90]; Sanford and Buapeng (1996) [626] and Sanford et al. (2004) [47]). Some of these studies have been described in detail in other chapters of this manual. Tracer model ages can be valuable data with which to help calibrate a model (Sanford (2011) [627]). They provide information directly related to the fluxes in the system, which are often more difficult to obtain than heads. Baseflows to streams, a common measurement of flux in the system, cannot always be easily measured, especially in arid environments, and so tracer model ages can provide another much needed source of flux data. Tracer model age data, however, require one additional type of information, porosity, to be used as model constraints. Flow model ages are based on travel paths that are based on seepage velocities that include porosity in their calculations. Simulated baseflows do not require porosity measurements. This porosity requirement does not necessarily hamper the use of tracer model ages to calibrate a model. In unconsolidated sediments, porosity can often be easily estimated or measured and so can be added to the model as prior information. When both baseflow and tracer model age data are available in hard rock terrains, the tracer model ages can help constrain the porosity, which might otherwise be poorly known.

A number of different hydraulic characteristics of a groundwater flow system can affect the distribution of the flow model age within that system (Fig. 10.6), including the distribution of recharge, the vertical anisotropy and the regional scale heterogeneity. Homogeneous systems with



FIG. 10.6. Spatial patterns of groundwater age as a result of various distributions of recharge and hydraulic conductivity (K). Contour values are flow model age (in years). Arrows show general direction of flow. The vertical anisotropy ratio in the middle set of simulations is 10 000 horizontal to 1 vertical. The confining layer contrast in K in the lower set of simulations is 1000 to 1. (After Sanford (2011) [627].)

evenly distributed recharge can be expected to have flow model ages that increase with depth and have lines of equal flow model age that are nearly horizontal. If the recharge is distributed predominantly towards the upper reaches of the flow system, however, as is often the case in arid environments or low lying areas where the water table closely mimics the topography, the lines of equal flow model age can become closer to vertical. Increasing vertical anisotropy in a system nearly always increases the vertical gradient in the flow model age.

Regional heterogeneities such as confining layers can create pockets of older water where substantial vertical hydraulic gradients are not present. In general, the distribution, connectivity and vertical hydraulic conductivity of the confining layers are one of the largest controlling factors on both the flow model ages and the tracer model ages within a groundwater flow system. The conceptual model adopted for the presence of confining layers is important. For example, a system conceptualized as having a large regional vertical anisotropy, but not a discrete heterogeneity, cannot under any conditions yield a depth profile of flow model ages that are overturned (younger beneath older), whereas overturned tracer model ages in regional systems are not uncommon in discharge areas. The fact that hydraulic properties can greatly impact the flow model age distribution is equally an indicator that spatially distributed tracer model age data can provide good information on the nature of the flow system. This equally demonstrates that tracer model age data can be quite valuable in constraining conceptual and numerical models of flow systems. This is additionally supported by the fact that regional scale confining unit properties are often the most difficult to measure directly.

A number of field studies using tracer model ages to calibrate groundwater flow models have demonstrated that matching of individual flow model ages to tracer model ages is more difficult than matching simulated water levels to observed water levels. Water levels represent a potential field of energy within a groundwater system, and as such values vary relatively smoothly within the system as a function of the spatial distribution of the hydraulic property distribution and the boundary conditions. In addition, boundary conditions using specified water levels already partially constrain the simulated water level values. On the other hand, flow model ages are calculated based on the velocity field, which is based on the gradient or first derivative of the water level (potential) field. As the flow field is usually complicated by heterogeneity in the hydraulic properties and recharge distribution, the velocity field is usually relatively complex both in magnitude and direction. It, therefore, becomes very common for the variations that exist within the velocity fields (creating, for example, local flow cells within regional flow cells) to be misrepresented at the very local scale at which the tracer samples were collected and the flow model ages were simulated. A well screen, for example, may be located near the boundary between a local and regional flow subsystem, and the slightest misrepresentation of those systems in the model might cause the equivalent flow model age to be calculated at a very different value because it is located within the wrong flow subsystem. In addition, the first derivates (velocities) are not continuous across the boundaries of flow subsystems, and this can further complicate automated calibration tools that rely on the parameter sensitivities (first derivatives). The resulting end effect very often appears like a poor match between tracer model ages and flow model ages. Two recent examples of this using ¹⁴C model ages demonstrate this issue (Fig. 10.7). Although this demonstrates the difficulty in using tracer model ages to calibrate flow models at fine scales, it still does not negate the usefulness of tracer model ages in the calibration of flow models at coarser scales.

In spite of the usefulness of tracer model ages in model calibration, a number of caveats should be noted. Steady state model assumptions are often used for regional models with relatively old flow model ages, but these assumptions are not always valid. Climatic changes leading to changing recharge rates over time may need to be considered. Substantial groundwater withdrawals from wells may also need to be included in the model as these can affect the distribution of flow model and tracer model age in the system (Zinn and Konikow (2007) [628]). Use of advection model ages alone will create some degree of error from the lack of considering dispersion. Simulating dispersion with advection can reduce this error, but the uncertainty in the appropriate field dispersivities to assign to the model may offset this benefit. Simulation of dispersion in three dimensions is also computationally very

challenging on a regional scale without introducing numerical dispersion (Sanford and Pope (2010) [629]). Thus, although, in theory, it is possible to simulate dispersion model ages, this is usually not tractable for three dimensional groundwater models. In spite of the assumptions behind advection model age simulation, it is still an efficient and potentially very useful tool for model calibration. This is especially true considering that there is often a lack of other basic flux information in addition to that provided by tracer model ages, and groundwater models lacking in adequate flux information can remain relatively unconstrained.



FIG. 10.7. Plots of observed versus simulated water levels in (a) central Hungary and (b) New Mexico, USA; and ¹⁴C model and flow model ages in (c) central Hungary and (d) New Mexico, USA (after Sanford et al. (2004) [47] and Sanford et al. (2001) [630]). It should be noted that the age plots are in log–log scale, yet still have more visual scatter around the perfect match (solid) lines than the water level plots.

Chapter 11

MILK RIVER AQUIFER, ALBERTA, CANADA — A CASE STUDY

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11.1. INTRODUCTION

The Milk River aquifer is a complex system in terms of origin and evolution of the chemical and isotopic composition of the groundwater. Fortunately, a wealth of physical and chemical data of the groundwater and the bonding shales was collected by numerous authors over a period of about 15 a that allowed applying various complementary approaches in dating the groundwater. Although these Milk River aquifer studies were carried out more than two decades ago, they can still be considered an outstanding example for dating of old groundwater.

The Milk River aquifer fits the definition of an idealized confined aquifer system, and dips gently from its outcrop area (~5 m/km). A short distance from the recharge area, the 'idealized groundwater age'¹ extends beyond the ¹⁴C dating limit and further downstream reaches values up to more than one million years. Owing to this feature, the Milk River aquifer was selected for an IAEA sponsored international project that was aimed at evaluating all isotope techniques available for dating of old groundwater; it finally resulted in the most comprehensive application of isotope and geochemical techniques to an individual aquifer system at that time. Analyses were carried out for halides and other major and minor ions, stable isotopes (²H, ³He, ⁴He, ¹³C, ¹⁸O) and radioactive isotopes (²²²Rn, ⁸⁵Kr, ³⁷Ar, ³⁹Ar, ¹⁴C, ⁸¹Kr, ³⁶Cl, ¹²⁹I, ²³⁴U, ²³⁸U). The results of the various isotopic and geochemical studies were published in a special edition of Applied Geochemistry (Ivanovich et al. (1991) [631]). The following is a summary and comparative discussion of the results, with particular emphasis on the determination of the groundwater age in the Milk River aquifer system.

11.2. GEOLOGICAL AND HYDROLOGICAL BACKGROUND

The Milk River aquifer underlies 15 000 km² of southern Alberta. Most of the area is covered by Pleistocene glacial drift (Hendry et al. (1991) [632]). The aquifer crops out in southern Alberta, Canada, predominantly on the flanks of Sweetgrass Hills, northern Montana, USA, at the southern end of the study area (Fig. 11.1). The Milk River Formation is composed of sandstone (30–75 m in thickness) sandwiched between shales. It is confined above by marine shale of the Pakowki Formation (typically 120 m thick) and below by the Colorado Group that ranges in thickness from 500 to 650 m (Fig. 11.2). The transmissivity of the aquifer decreases from south to north, and from west and east.

This decrease is caused by a general thinning of the sandstone in these directions and a decrease in hydraulic conductivity towards the north due to an increase in the shale content. The groundwater flow is generally towards the north, west and east, following the dip of the aquifer. Two main flow paths were identified by valleys of low Cl⁻ concentrations (Fig. 11.3). Since the sandstone pinches out in all directions, the aquifer must discharge by upward and downward leakage. All water that leaves the aquifer must, therefore, pass through the shale/sand interface. Hendry and Schwartz (1988) [633] suggested that about 500 ka ago the outcrop area was uncovered by erosion and meteoric water replaced connate water at that time. In fact, groundwater model ages of this order were found by ³⁶Cl dating (Phillips et al. (1986) [319]).

¹ The 'idealized groundwater age' is defined in Chapter 3 of this book. For the sake of simplicity, in the following the expression 'groundwater age' is used.



FIG. 11.1. Study area (from Hendry and Schwartz (1988) [633]).



FIG. 11.2. Geology of the Milk River aquifer along the S–N cross-section (from Hendry et al. (1991) [632]).

11.3. THE ROLE OF GEOCHEMISTRY IN CONSTRAINING WATER AND SOLUTE TRANSPORT MODELS — THE MILK RIVER AQUIFER EXPERIENCE

The geochemistry of the Milk River aquifer was studied by numerous authors (Hendry and Schwartz (1988) [633]; Hitcheon and Friedman (1969) [634]; Meyboom (1960) [635]; Phillips et al. (1986) [319]; Schwartz and Muehlenbachs (1979) [636]; Schwartz et al. (1981) [637]; Swanick (1982) [638]). It is characterized by significant changes in major ion concentrations along the groundwater flow. Ion exchange of Ca^{2+} (and Mg^{2+}) for Na⁺ creates calcite undersaturation that forces calcite dissolution down the flow path and raises the HCO₃ concentration. Concentrations of SO²⁺ are high in groundwater of the recharge area but due to bacterial reduction virtually disappear in the central part of the aquifer. The concentrations of Cl⁻ and l⁻ strongly increase in the flow direction; near the recharge area, they are less than 0.5 and 0.001 mmol/L, respectively, and increase to more than 100 and 0.15 mmol/L,



FIG. 11.3. Contour plot of the Cl concentrations with the two main flow paths (I = eastern flow path, II = western flow path) along the valleys of the Cl concentrations. The numbers give the concentration in mmol/L (from Nolte et al. (1991) [291]).

respectively, at the northern edge of the aquifer. Similarly, the ¹⁸O (δ^2 H) values increase from less than -21% (-167‰) near the recharge area to -8% (-70‰) in the north. While the δ^{18} O and δ^2 H values of the recharge waters plot on the global meteoric water line, further downstream, the data deviate from the meteoric water line and fit a line with a slope of 6.3 instead of 8 (Hendry and Schwartz (1988) [633]). Several alternative mechanisms were proposed to explain the observed distribution of non-reactive species in the Milk River aquifer (Fig. 11.4): (i) introduction of connate formation water through the Colorado shale and subsequent mixing with infiltrating meteoric water (Schwartz and Muehlenbachs (1979) [636]; Schwartz et al. (1981) [637]); (ii) meteoric recharge mixing with more saline water in the aquifer (Domenico and Robbins (1985) [639]); (iii) chemical and isotopic enrichment due to ion filtration (Phillips et al. (1986) [319]); and (iv) aquitard diffusion (Hendry and Schwartz (1988) [633]).

Hendry and Schwartz (1988) [633] reviewed the previously proposed mechanisms (i)–(iii), especially ion filtration, and concluded that these mechanisms are not supported by hydraulic conductivity and hydraulic head data, Cl⁻ concentrations of drill cuttings and isotope values from Colorado shale groundwater. They proposed an alternative mechanism based on diffusion between saline, isotopically enriched water of the Colorado shale and fresher, isotopically depleted water in the aquifer. Using an analytical mass transport model, the authors found that the pattern in Cl⁻, I⁻, δ^{18} O and δ^{2} H in the aquifer can be explained by aquitard diffusion. The best model fit to both Cl⁻ and δ^{18} O data yielded an effective aquitard diffusion coefficient (the most critical parameter in the model) of 6×10^{-12} m²/s for these species. On the basis of this aquitard diffusion mechanism, Hendry and Schwartz (1988) [633] evaluated ³⁶Cl data published by Phillips et al. (1986) [319]. The derived ³⁶Cl model ages of the groundwater were found to be consistent with earlier age estimates based on hydraulic modelling (Swanick (1982) [638]). Consequently, Hendry and Schwartz (1988) [633] concluded that aquitard



FIG. 11.4. Conceptual models to explain the origin of chemical patterns in the Milk River aquifer: (a) megascopic dispersion; (b) partial area of recharge; (c) membrane filtration; and (d) aquitard diffusion (from Hendry and Schwartz (1988) [633]).

diffusion must be considered when using ³⁶Cl to date groundwater in aquifer–aquitard systems such as the Milk River aquifer.

In contrast, Phillips et al. (1990) [640] concluded from an in-depth review of Hendry and Schwartz's arguments, that there was no evidence for aquitard diffusion. On the basis of a Peclet number analysis with parameter values selected from Hendry and Schwartz's paper, they found that "transport in the aquitard is strongly advection dominated". However, it should be noted that the Peclet numbers referred to by Phillips et al. (1990) [640] are proportional to the square of the seepage velocity and that this parameter was estimated from the measured hydraulic conductivity. Given that the hydraulic conductivity values of the aquitard ranged from less than 10⁻¹¹ up to about 10⁻⁸ m/s (Hendry and Schwartz (1988) [633]), it can be concluded that the uncertainty of the Peclet numbers estimated by Phillips et al. (1990) [640] is very high. Thus, the observed ambiguity in the conceptual models on the solute transport appears to be associated with high uncertainty of the field data used in both approaches. Phillips et al. (1990) [640] came to the conclusion that "the reality is that we very seldom posses even a fraction of the field data necessary to constrain such models". It should, however, be

Well	$^{129}I/I \times 10^{-15}$	(atoms/mL)		
3	_	_		
4	90 ± 30	5200 ± 1700		
5	1130 ± 70	850 ± 53		
9	135 ± 40	960 ± 280		
10	390 ± 65	5700 ± 950		
11	165 ± 50	250 ± 76		
14	790 ± 10	1240 ± 20		
16	190 ± 80	1900 ± 785		
18	145 ± 50	3200 ± 1100		

TABLE 11.1. IODINE-129 IN GROUNDWATER OF THE MILK RIVER AQUIFER (from Fabryka-Martin et al. (1991) [385])

noted, that additional data became available which provided new insights into the processes operating in the Milk River aquifer.

Fabryka-Martin et al. (1991) [385] measured the ¹²⁹I/I ratio in groundwater samples of the aquifer which turned out to be useful for answering the question of whether ion filtration or diffusion controls the observed increase of halide concentrations. The highest value of the ¹²⁹I/I ratio (1.1×10^{-12}) was found in the youngest groundwater of the recharge area (Table 11.1, well 5). This value corresponds to a meteoric input that is undiluted by iodine released from the aquifer matrix or from the confining units. Further down flow, the ¹²⁹I/I ratio decreased remarkably; in the oldest groundwater (well 18), it was about one order of magnitude lower. These lower values cannot be explained with radioactive decay of the meteoric component of ¹²⁹I since the half-life of ¹²⁹I (16 Ma) is so long that even for groundwater model ages of 2 Ma the radioactive decay of the meteoric component of ¹²⁹I would be insignificant. Thus, Fabryka-Martin et al. (1991) [385] concluded that a subsurface source of iodine must be present and that the high iodine concentrations in the water are not a simple result of ion filtration. On the basis of their study of halides, the authors advanced an additional hypothesis. They found that the Cl/I and Cl/Br ratios of groundwater close to the recharge zone are well below those of sea water. This suggests diagenesis of organic matter in the sediments as the source of the halides.

However, moving down flow, the halide ratios reach nearly constant values, suggesting the dominance of a common subsurface source for these ions. Fabryka-Martin et al. (1991) [385] concluded that the observed halide ratios rule out unaltered sea water or leakage and/or diffusion from the underlying Bow Island sandstone as a major source of the halides in the groundwater. They suggested that the primary source of the halides is altered connate sea water diffusing from low permeability units within the Milk River Formation. This is also at variance with the hypothesis offered by Hendry and Schwartz (1988) [633] in which the halides and other dissolved constituents diffuse primarily from the underlying Colorado shales. Fabryka-Martin et al. (1991) [385] emphasized that this (fifth) conceptual model does not require the assumption of mixing with an external water body or complex mechanisms such as ion filtration. Furthermore, they argued that "other saline sources proposed by other authors cannot be ruled out altogether and are probably contributing to the groundwater geochemistry to some extent, but the model, in which the solute source resides mainly within the Milk River Formation, is the simplest one and is able to account for most of the observed data". Phillips (2000) [306] largely agreed with this explanation admitting that a significant portion of the increase of Cl⁻ concentration observed in the Milk River aquifer is due to diffusion from low permeability units within the aquifer and "the remainder is most likely due either to ion filtration or variable evaporation during recharge".

Finally, it has to be noted that in the case of the Milk River aquifer a possible glacial 'squeezee' effect should be taken into account. It is known that the aquifer experienced massive glacial loading moving from north to south and, thus, potentially squeezing water out of the shale into the aquifer at the initiation of glaciation and reversing the flow at glacial retreat (F. Phillips, personal communication²). Recent research on glacial chronology of the area in south-western Alberta, Canada, suggests that there was perhaps only one glacial advance over the study area, the Wisconsinan (Jackson and Little (2004) [641]).

Overall, the situation that a number of alternative mechanisms were suggested for the explanation of observed geochemical data points to an ambiguity that seems to be inherent in complex systems such as the Milk River aquifer. In such systems, shale aquitards and interbeds can play a critical role as sources of the chemistry of the groundwater in the aquifer. Tackling this ambiguity is a formidable challenge in connection with dating of old groundwater.

11.4. ISOTOPIC STUDIES OF THE MILK RIVER AQUIFER

11.4.1. Radiocarbon and stable isotopes

Measurements of ²H, ³H and ¹⁸O in groundwater, ²H and ¹³C in methane, ¹⁸O and ³⁴S in SO₄⁻, ¹³C and ¹⁴C in DIC and DOC have been discussed by Drimmie et al. (1991) [168]. Here, focus is put on interpretation of the ¹⁸O and ²H data and the ¹⁴C results. Plotting δ^{18} O against δ^{2} H, the authors were able to identify three distinct clusters (Fig. 11.5): cluster A with δ^{18} O values of approximately –19‰, cluster B with δ^{18} O of –16‰, and cluster C with δ^{18} O of –8‰. Cluster A represents groundwater near the recharge area in the southern part of the aquifer (some samples contained measurable levels of bomb tritium). The isotopic signatures are not followed by even more negative δ^{18} O and δ^{2} H values down flow as might be expected if Pleistocene recharge were present. This absence of a glacial signature suggests that this groundwater was recharged before 15 ka, and that the Pleistocene period of that region is characterized by insignificant recharge over long periods. The uniform δ^{18} O and δ^{2} H values found in groundwater to about 20 km distance from the recharge zone indicate a minimum flow rate of about 1 to 1.5 m/a in this part of the aquifer. The data in cluster B fall close to the modern meteoric water line for the region. However, this groundwater contains no measurable ¹⁴C and could, thus, have been recharged before the last glaciation.

Assuming constant flow rates beyond the Milk River on the order of 0.1 m/a, Drimmie et al. (1991) [168] suggested groundwater model ages >50 ka BP and possibly as much as 600 ka BP along path I. Cluster C data represent groundwater in the most distant section of the Milk River aquifer. They follow a line that deviates from the meteoric water line. Hendry and Schwartz (1988) [633] suggest that this line represents diffusive mixing between isotopically enriched water in the confining shales and meteoric water recharged during warm climate phases. Alternatively, Phillips et al. (1990) [640] mentioned that the slope of this line is consistent with ion filtration (see Chapter 3).

Radiocarbon was measurable only in groundwater sampled from wells located within 20 km of the recharge zone. Although the DIC ¹⁴C pmc values are much lower than those for DOC in both wells, the age differences between the two wells are quite similar, averaging about 14 ka (Fig. 11.6). The lower DIC values led to the conclusion that the DIC ¹⁴C content when the water entered the aquifer was as low as 30 pmc. From these data, a flow rate of ~1 m/a has been estimated for the distance of 12 km between the two wells (Fig. 11.6). This flow rate agrees surprisingly well with the stable isotope data but is an order of magnitude higher than the flow rates estimated for the northern part of the aquifer by hydraulic modelling (Hendry and Schwartz (1988) [633]; Swanick (1982) [638]), ³⁶Cl data (Nolte et al. (1991) [291]; Phillips et al. (1986) [319]) and uranium isotope measurements (Ivanovich et al. (1991) [422]). Thus, the ¹⁴C derived flow rates for the southern part cannot be adopted for the entire flow

² PHILLIPS, F., Department of Earth and Environmental Science, New Mexico Tech, personal communication.



FIG. 11.5. Oxygen-18 versus deuterium plot including the global meteoric water line (GMWL) (from Drimmie et al. (1991) [168]).



FIG. 11.6. Cross-section from the recharge zone in the Sweetgrass Hills, USA, to well No. 52 (approximately the Milk River). The boxes above give the ${}^{14}C$ results for the three main pools of C and their difference in years (from Drimmie et al. (1991) [168]).

system in which ¹⁴C is, for the most part, absent. It is, therefore, concluded that the fast groundwater movement in the southern part of the aquifer (about 1 m/a) occurs only up to the Milk River. This river, thus, represents a discharge rather than a recharge strip. Consequently, the flow rate north of the river slows down to values of about 0.1 m/a in the northern sections of the aquifer.

11.4.2. Dissolved gases

Andrews et al. (1991) [397] discussed the results obtained from analyses of CH_4 and its isotopic composition, N_2 , noble gases (He, Ne, Ar, Kr and Xe), and isotopic composition of Ar and ²²²Rn.



FIG. 11.7. Theoretical stored He contents as a function of depth for the radioelement contents of Milk River sandstone and for the underlying Colorado shale. Milk River sandstone profiles are shown for the diffusion coefficient of water ($D_1 = 3.2 \times 10^{-2} m^2/a$, open circles), rock with 10% interstitial water ($D_2 = 3.2 \times 10^{-3} m^2/a$) and to match the observed He/depth profile for groundwater ($D_3 = 3.2 \times 10^{-4} m^2/a$, triangles). The calculated profile for the Colorado shale is shown for the diffusion coefficient D3 (inverted triangles). Helium data for the Milk River groundwater are shown as filled circles (from Andrews et al. (1991) [397]).

The recharge temperatures derived from the noble gases indicated that the youngest groundwater was recharged under cooler climatic conditions than the ones prevailing during earlier recharge episodes. The inferred recharge temperature difference of about 4 to 5°C has been found to be consistent with estimates based on the stable isotope data.

The concentration of ⁴He varies with depth of the aquifer. This result is consistent with radiogenic ⁴He accumulation in the aquifer and adjacent shales. From the ⁴He depth profile of the Milk River sandstone and the Colorado shale, the diffusion constant for ⁴He loss from the formation was estimated to be $\sim 3.2 \times 10^{-4}$ m²/a (Fig. 11.7). With this value and the ⁴He generation rate derived from U and Th content and porosity of the Milk River sandstone and Colorado shale, a ⁴He flux from the surface of the Colorado shale of about 1.2–1.8 × 10⁸ atoms \cdot cm⁻² \cdot s⁻¹ was obtained. This value corresponds to less than 2% of other continental ⁴He flux estimates and is consistent with the assumption that ⁴He release from continental crust is a discontinuous process controlled by random tectonic events or by aqueous transport (Torgersen (1989) [546]). The ⁴He content tends to increase with the Cl content of the groundwater. Since increasing Cl content is regarded as an index of groundwater ageing, the increase of the ⁴He content appears to be associated with an increase of the groundwater age. However, no reliable age values could be inferred from the available ⁴He data because some of these data are distorted by degassing during groundwater sampling.

The mean ²²²Rn activity concentration of the Milk River groundwater was found to be 1.7×10^4 Bq/m³ (Andrews et al. (1991) [397]). The ²²²Rn content of the groundwater is controlled by the uranium content of the aquifer and by the fractional release, *E*, of ²²²Rn from the rock matrix into the interstitial fluid: $E = \varphi N_w/[(1 - \varphi)N_m] = \varphi N_w N_b$, where N_w , N_m and N_b is the concentration of ²²²Rn atoms in the groundwater, the equilibrium concentration in the rock matrix and in the bulk rock, respectively; φ is the rock porosity. With this equation, Andrews et al. (1991) [397] estimated a value of the fractional release in the Milk River sandstone of 2.7%. They used the measured value of the mean ²²²Rn content of 1.7×10^4 Bq/m³, a porosity of 10% and a uranium content of 2.4 ppm for the confined sandstone. The observed fluctuation of the ²²²Rn concentration was attributed to the variability of

the aquifer parameters controlling the ²²²Rn release (uranium content, porosity and release efficiency). A value of less than 25% was estimated for most of the area (Andrews et al. (1991) [397]).

Andrews et al. (1991) [642] measured ³⁷Ar and ³⁹Ar in samples taken from three wells located about 20–40 km from the recharge area. At these locations, the groundwater model age was found to be far beyond the radioactive lifetimes of ³⁷Ar (50 d) and ³⁹Ar (390 a); therefore, no residual cosmogenic ³⁷Ar and ³⁹Ar should remain. The measured ³⁹Ar/³⁷Ar ratio was rather close to the ratio calculated for in situ production within sandstone of the aquifer, but very different from the ratio for production within the underlying Colorado shale. Thus, the source of ³⁹Ar and ³⁷Ar of the groundwater samples appeared to be sandstone of the aquifer rather than the Colorado shale.

Lehmann et al. (1991) [282] measured ⁸¹Kr and ⁸⁵Kr in well 9 located at a distance of about 20 km from the recharge area. The activity of ⁸⁵Kr was only 0.3% of the modern atmospheric value and, thus, any admixture with younger groundwater could be neglected. From the ⁸¹Kr value, a maximum model age of 140 ka was estimated, which appeared to be in good agreement with hydraulic modelling and groundwater dating by ³⁶Cl and uranium isotopes.

11.4.3. Chlorine-36 and chloride

First measurements of ³⁶Cl in groundwater of the Milk River aquifer were carried out by Phillips et al. (1986) [319]. For the evaluation of the ³⁶Cl (and Cl) data in terms of groundwater model age, two processes were considered. Phillips et al. (1986) [319] assumed ion filtration and estimated an age of about 2 Ma for groundwater at the end of the aquifer. Hendry and Schwartz (1988) [633] used a diffusion model from which ages of 0.25 and 0.51 Ma were deduced for groundwater at the end of the eastern and western flow paths, respectively.

Additional ³⁶Cl/Cl measurements were carried out within the frame of the IAEA sponsored Milk River project (Nolte et al. (1991) [291]). The observed changes of ³⁶Cl and Cl along the two flow paths were evaluated under two different assumptions: (i) simple exponential decrease of ³⁶Cl and linear increase of Cl with distance from the recharge area where in one case in situ production of ³⁶Cl was included and in the other one excluded; (ii) radioactive decay of ³⁶Cl and diffusion of ³⁶Cl and Cl from the underlying Colorado shale to the aquifer without and with in situ production of ³⁶Cl. For in situ production, a saturation value of ³⁶Cl/Cl = 4×10^{-15} was used. The results of the first approach are shown in Fig. 11.8.



FIG. 11.8. Concentration of ³⁶Cl versus distance from the recharge area. The drawn lines represent least square fits without (a) and with (b) in situ production of ³⁶Cl (from Nolte et al. (1991) [291]).



FIG. 11.9. Concentration of Cl and ³⁶Cl along the eastern flow path calculated by the diffusion model, with in situ ³⁶Cl production (from Nolte et al. (1991) [291]).

		Eastern f	How noth	Western flow noth		
		Eastern now path		western now path		
		Without in situ production	With in situ production	Without in situ production	With in situ production	
Flow velocity (m/a)	without diffusion	0.11	0.09	0.08	0.06	
	with diffusion	0.14	0.5	0.1	0.07	

TABLE 11.2. COMPARISON OF FLOW VELOCITIES DETERMINED (after Nolte et al. (1991) [291])

The groundwater flow velocities were obtained by least square fits of the theoretical curves to the experimental data. Figure 11.9 shows the results of the diffusion model with in situ production for the eastern flow path.

Table 11.2 compiles all values of the groundwater flow velocity obtained with different assumptions. In the first approach (without diffusion), consideration of in situ production yields a value of the flow velocity that is only 75% of the value without in situ production. The flow velocities inferred from the diffusion model (second approach) are about 30% greater than the values deduced without consideration of diffusive losses of ³⁶Cl. Thus, Nolte et al. (1991) [291] conclude that radioactive decay of ³⁶Cl rather than diffusive loss controls the ³⁶Cl concentration in groundwater during advective transport in the aquifer. The flow velocities are in the range 0.09–0.14 m/a (eastern flow path) and 0.06–0.10 m/a (western flow path). The corresponding groundwater model ages at a distance of 80 km from the recharge area are in the range of 0.6–0.9 Ma (east) and 0.8–1.6 Ma (west). For comparison: using ion filtration to describe the evolution of Cl in the Milk River groundwater, Phillips et al. (1986) [319] obtained ages of up to about 2 Ma at the end of the aquifer. On the other hand, the values of the groundwater velocity determined by Hendry and Schwartz (1988) [633] are remarkably larger than the ones deduced by Nolte et al. (1991) [291]. For the eastern flow path, they obtained 0.32 m/a and for the western flow path 0.16 m/a. Comparing the various ³⁶Cl dating approaches of the Milk River aquifer, Phillips (2000) [306] suggested that the age estimates derived from the ³⁶Cl/Cl ratio under assumption of ion filtration ('ion filtration age', Phillips et al. (1990) [640]) may be more accurate for regions close to the recharge zone while further away dating based on the ³⁶Cl concentration (Nolte et al. (1991) [291]) may be more adequate.

Although in situ production of ³⁶Cl in aquifer matrices is generally known to be significant, its contribution to the ³⁶Cl content of Milk River aquifer groundwater appeared to be relatively low in

comparison to the cosmogenic input. Groundwater ages calculated with in situ production of ³⁶Cl were only between 30% (western flow path) and 25% (eastern flow path) higher than the ages calculated for zero in situ production. However, when the groundwater Cl content reaches very high values (~500 ppm), in situ production may be significant (Figs 11.8 and 11.9).

11.4.4. Uranium isotopes

For uranium isotope analysis, 21 water samples and two rock samples (core samples) were collected from the Milk River aquifer, and one surface water sample from the Milk River (Fig. 11.10). The uranium concentrations were found to decrease along the groundwater flow direction.



FIG. 11.10. Location of sampling wells and core samples in the Milk River aquifer. Two identified flow paths are indicated by arrows (from Ivanovich et al. (1991) [422]).



FIG. 11.11. ²³⁴U/²³⁸U ratio against Cl concentration in the groundwater of the Milk River aquifer and delineation of the oxic and anoxic regions (from Ivanovich et al. (1991) [422]).



FIG. 11.12. Decrease of the relative ${}^{234}U$ excess $({}^{234}U/{}^{238}U$ activity ratio -1) along flow path 1 (from Ivanovich et al. (1991) [422]).



FIG. 11.13(a). Plot of the ²³⁸U activity concentration against the distance along the flow path from the outcrop of the Milk River aquifer. The solid line represents the best-fit line of approach to using the complete data set (after Ivanovich et al. (1991) [422]).



FIG. 11.13(b). Plot of the ${}^{234}U$ activity concentration against the distance along the flow path from the outcrop of the Milk River aquifer. The solid line represents the best-fit line of approach to using the complete data set (after Ivanovich et al. (1991) [422]).

In the oxidizing zone near the recharge area, the uranium concentrations ranged from about 12 to 0.7 μ g/L and under anoxic conditions from 0.07 to 0.007 μ g/L.

Parallel geochemical investigations of dissolved ions in groundwater (Ivanovich et al. (1991) [422]) have shown that all groundwater samples are undersaturated with respect to common uranium minerals, which suggests that uranium minerals do not precipitate. Furthermore, the Cl concentrations were found to increase with the groundwater age. The ²³⁴U/²³⁸U ratios tend to increase with distance down flow of the outcrop in the oxic zone and reach a maximum at well 11 where the redox front is positioned. In the downstream anoxic zone, the ²³⁴U/²³⁸U ratios decrease with increasing Cl concentrations, i.e. increasing groundwater age (Fig. 11.11). The decrease in ²³⁴U/²³⁸U is accompanied

by a constant but low ²³⁸U concentration, and the change in ²³⁴U/²³⁸U ratio could, thus, be attributed to the radioactive decay of ²³⁴U and exchange between the liquid and adsorbed phase (retardation). It should be noted that a similar pattern of the evolution of the uranium isotopes (low and basically constant uranium concentration at decreasing ²³⁴U/²³⁸U ratios downdip the anoxic zone) was also observed in other regional aquifers such as the Hosston aquifer (Kronfeld and Adams (1974) [424]), Carrizo aquifer (Cowart and Osmond (1974) [419]), Lincolnshire limestone (Edmunds (1973) [643]) and Lincolnshire chalk (Cuttell et al. (1986) [644]).

The Milk River uranium isotope data were evaluated by two different approaches. In a first approach, only the data of the anoxic part of the aquifer were evaluated, assuming constant ²³⁸U concentration and exponential decrease of ²³⁴U excess down flow. The model corresponds to Eq. (7.17) assuming that the stationary value of the ²³⁴U excess is zero (no ²³⁴U production by recoil ejection). Figure 11.12 shows the best fit line of the model to the experimental data in a semi-logarithmic plot. According to Eq. (7.17), the slope of this line represents the ratio λ_{234}/v^* , from which the velocity, v^* , can be calculated. The obtained value is 0.12 m/a (Ivanovich et al. (1991) [422]). Using a hydraulic model, Hendry and Schwartz (1988) [633] determined a groundwater flow velocity v of 0.3 m/a for the same flow path. Obviously, the velocity v^* characterizes the uranium migration velocity which is related to the groundwater flow velocity by the expression $v^* = v/R$, where R is the retardation factor. Thus, for the considered anoxic part of the Milk River aquifer, the uranium retardation factor appears to be R = 0.3/0.12 = 2.5.

In a second approach, all measured ²³⁸U and ²³⁴U concentrations were plotted against distance along a generalized flow path from the Milk River outcrop area (Figs 11.13(a) and 11.13(b)). For the estimation of the distances, the position of each sampled well was projected onto the generalized N–S flow path. The main feature of the semi-logarithmic plots in Figs 11.13(a) and 11.13(b) is an approximately linear decrease of the uranium isotope concentrations with increasing distance along the flow path. However, there are considerable deviations of individual data from the linear trend lines which point to significant local fluctuations of the geochemical and/or hydrological conditions along groundwater flow.

Nevertheless, the absence of any independent evidence for these inhomogeneities in the aquifer was deemed to justify this statistical approach that does not explicitly take into consideration the influence of a redox front. Assuming, as in the first approach, that the stationary values of the uranium isotope concentrations are negligible, the slope, s, of the best-fit lines in Figs 11.13(a) and 11.13(b) can be derived from Eqs (7.7, 7.8), respectively (see Chapter 7). The following expression is obtained:

$$s_i = K_i / v \tag{11.1}$$

where

 K_i is defined by Eq. (7.11); i stands for ²³⁴U and ²³⁸U, respectively.

The following values have been determined by this approach: $s_8 = 5.8 \times 10^{-5}$ /m and $s_4 = 4.7 \times 10^{-5}$ /m. Thus, within the accuracy of this estimate, the two lines have the same slope of about 5×10^{-5} /m. Adopting the value of the parameter *K* determined by Fröhlich and Gellermann (1987) [426] for the Hosston aquifer ($K_8 \approx K_4 \approx (1-3) \times 10^{-5}$ /a), Ivanovich et al. (1991) [422] estimated a groundwater flow rate for the Milk River aquifer of between 0.2 and 0.6 m/a. Within the range of the given uncertainties, this result seems to be in good agreement with estimates by other methods (Table 11.3), which indicates "that uranium isotope data are a viable tool for dating very old groundwater provided the local uranium geochemistry is understood adequately" (Ivanovich et al. (1991) [422]).

	Hydraulic method ^a		36C1 b		U isotopes ^c	
	Path 1	Path 2	Path 1	Path 2	Method 1 Anoxic part	Method 2 Total aquifer
v (m/a)	0.32	0.16	0.09-0.14	0.05-0.10	0.12	0.2–0.6
age (Ma) ^d	0.25	0.51	0.6-0.9	0.8-1.6	0.7	0.13-0.4

TABLE 11.3. COMPARISON OF METHODS APPLIED TO DATE GROUNDWATER OF THE MILK RIVER AQUIFER

^a Hendry and Schwarz (1988) [633].

^bNolte et al. (1991) [291].

^c Ivanovich et al. (1991) [422].

^dAt a distance of 80 km from the outcrop.

11.5. CONCLUSIONS

Examining the hydrochemistry, in particular the distribution of chloride, it was possible to identify major groundwater flow paths through the extended confined aquifer system. The stable isotopes ²H and ¹⁸O provided information on the groundwater regime under past climate conditions. Radiocarbon has been of use near the recharge zone; after a distance of 20 km down flow, its concentration was below the detection limit. From the ¹⁴C data, a value of about 1 m/a was derived for the flow velocity of the groundwater between the outcrop area and the Milk River. The river acts as a discharge strip which is manifested by a drastic decrease in the groundwater flow velocity further down flow.

The analyses of noble gases provided information on the groundwater recharge temperatures. The ⁴He content was found to increase along the flow path but could not be used to date the groundwater because some of the ⁴He data appeared to be distorted by degassing during groundwater sampling. Only one ⁸¹Kr measurement could be afforded at this early stage in the development of the ⁸¹Kr method. An upper limit of 140 ka has been calculated for the ⁸¹K based model age of groundwater collected about 20 km from the recharge area. This model age value is consistent with results obtained by other dating tools. Argon isotope measurements could not be interpreted in terms of groundwater age. The observed ³⁹Ar concentrations were found to be in good agreement with values corresponding to in situ production. Furthermore, the ³⁹Ar and ³⁷Ar data indicate that these isotopes are released to groundwater from the sandstone of the aquifer rather than the Colorado shale.

The ³⁶Cl data indicate that, in comparison to in situ production, the cosmogenic ³⁶Cl input to this system is high. Thus, radioactive decay of ³⁶Cl appeared to be the dominant process controlling the decrease of the ³⁶Cl content with distance down flow. On the contrary, most of the measured ¹²⁹I concentrations clearly point to in situ production of ¹²⁹I in the aquifer sandstone, with subsequent release to the surrounding groundwater. The groundwater flow velocities estimated from the uranium isotope data were found to be in reasonable agreement with the results obtained by hydraulic modelling and ³⁶Cl dating. In this context, it should be noted that hydraulic modelling based on present day hydraulic heads may underestimate the groundwater age because of the impact of climatic changes on the groundwater flow regime in the past.

In conclusion, the Milk River aquifer is a complex system in terms of origin and evolution of the chemical and isotopic composition of the groundwater. Fortunately, a wealth of physical and chemical data of the groundwater and the bonding shales was collected by numerous authors over a period of about 15 a that allowed applying various complementary approaches in dating the groundwater. Although the Milk River aquifer studies were carried out more than two decades ago, they can still be considered an outstanding example for dating of old groundwater.

Chapter 12

CASE STUDY MIDDLE RIO GRANDE BASIN, NEW MEXICO, USA

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12.1. INTRODUCTION

Chemical and isotopic patterns in groundwater can record characteristics of water sources, flow directions and groundwater age information. This hydrochemical information can be useful in refining conceptualization of groundwater flow, in calibration of numerical models of groundwater flow and in estimation of palaeo- and modern recharge rates. This case study shows how chemical and isotopic data were used to characterize sources and flow of groundwater in the Middle Rio Grande Basin, New Mexico, USA. The ¹⁴C model ages of the groundwater samples are on the tens of thousands of years timescale. These data changed some of the prevailing ideas about flow in the Middle Rio Grande Basin, and were used to improve a numerical model of the aquifer system.

12.2. BACKGROUND: HYDROGEOLOGICAL SETTING

The Middle Rio Grande Basin covers about 7800 km² along the Rio Grande Rift in central New Mexico, USA (Fig. 12.1). The Rio Grande Rift is a zone of faults and sediment filled basins that extends from northern Mexico to southern Colorado, USA. The basin consists of generally unconsolidated Cenozoic basin-fill sediment with a maximum thickness of about 4300 m (Fig. 12.2). The average elevation is about 1500 m, with surrounding mountains approaching 3300 m. The primary aquifer system of the Middle Rio Grande Basin consists of generally unconsolidated to moderately consolidated basin-fill sediment of the Santa Fe Group.

The Santa Fe Group aquifer system is defined by Thorn et al. (1993) [21] as including both the Santa Fe Group deposits, which are of Oligocene to middle Pleistocene age, and the more recent (post-Santa Fe Group) flood plain, channel and basin-fill deposits of Pleistocene to Holocene age that are in hydraulic connection with the Santa Fe Group. The Santa Fe Group deposits range in thickness from about 900 to 4300 m. The lower Santa Fe Group ranges in thickness from about 300 to 1000 m and consists largely of piedmont-slope, eolian sand and silt, and fine to medium grained basin-floor deposits (Fig. 12.2). The middle Santa Fe Group deposits range in thickness from about 75 to 2740 m and consist of piedmont-slope sediments and fluvial deposits (identified mostly as medium sand in Fig. 12.2). The upper Santa Fe Group sediments are generally less than 300 m thick and consist predominantly of piedmont-slope and fluvial basin-floor deposits, and are the most productive part of the aquifer system (denoted axial gravel, blanket sand/gravel, and medium-coarse sand in Fig. 12.2). A red-brown clay separates the upper and middle Santa Fe Group deposits at Albuquerque. Geophysical measurements have recognized three sub-basins within the Middle Rio Grande Basin that are separated by structural highs (Grauch et al. (1999) [645]; Grauch et al. (2001) [646]; see Bartolino and Cole (2002) [612] for further details). Most production wells are completed in the upper and/or middle Santa Fe Group, although wells on the west side of the Rio Grande reach parts of the lower Santa Fe Group.

In the 1980s, there was the perception that Albuquerque was situated over a large and almost unlimited supply of fresh groundwater, and optimism prevailed for seemingly unlimited growth potential. However, as new and detailed geological and hydrological data were gathered (Bartolino


FIG. 12.1. Location of the Middle Rio Grande Basin in west-central New Mexico, USA, and other physiographic features of the region.

and Cole (2002) [612]; Cole (2001) [647]; Connell et al. (1998) [648]; Hawley and Haase (1992) [649]; Thorn et al. 1993) [21]), the conceptualization of the aquifer system greatly changed. The most productive part of the aquifer system was found to be limited to a relatively small area of ancestral Rio Grande sediments under parts of Albuquerque.

Water level declines of as much as 40 m (130 ft) were observed between 1960 and 2002 at Albuquerque (Fig. 12.3). Until recently, groundwater was the sole source of drinking water for Albuquerque. During the 1990s, basin-wide pumping was about 200 Mm³ annually and about 75% of this water was withdrawn for public supply at Albuquerque. It is now thought that the basin-wide pumping rate amounted to about three times the modern recharge rate for the entire basin.

Recharge occurs along and near the basin margin. This includes mountain front processes, infiltration from arroyos and subsurface groundwater inflow. The other major source of recharge is surface water, particularly from the Rio Grande in central parts of the basin, its tributaries and, more recently, irrigation canals. Today, areal recharge is thought to be negligible across the semi-arid basin.



FIG. 12.2. Map and cross-section of the Middle Rio Grande Basin in west-central New Mexico, USA, showing (left) major physiographic features of the region, major faults in the basin, the basin boundary, the lowland inner valley of the Rio Grande and other drainage in the basin. The cross-section, A-A' (right), shows stratigraphic, lithologic and structural features of the basin to depths of more than 3500 m along an east–west cross-section at Albuquerque (from Bartolino and Cole (2002) [612]).



FIG. 12.3. Groundwater levels that represent 2002 conditions in the Santa Fe Group aquifer system in the Albuquerque area showing water level declines of more than 40 m since 1960 (from Bexfield and Anderholm (2002) [650]). Water level contours for the year 2002 (in feet; 1 ft = 0.3048 m) are shown as black lines, dashed where inferred.

12.3. THE UNITED STATES GEOLOGICAL SURVEY MIDDLE RIO GRANDE BASIN STUDY

A series of numerical groundwater models have been constructed for the basin by the United States Geological Survey (USGS). The model completed by Kernodle et al. (1995) [651], just before the present hydrochemical study began, included the geological and hydrogeological framework of Hawley and Haase (1992) [649], and the hydrogeological work of the USGS as summarized in Thorn et al. (1993) [21]. However, this model was not based on any hydrochemical data. Due to computational limitations at the time and the large model size, it could not be rigorously calibrated and some model parameters were assumed, such as recharge rate along the eastern mountain front. This model indicated no net recharge from the Rio Grande to the aquifer system - only infiltration to the inner valley of the Rio Grande, which was taken up by evapotranspiration. The basin-scale recharge rate was 5.45 m³/s and 62% of this was attributed to mountain block recharge and infiltration from arroyos adjacent to mountains. The relatively high recharge rate along mountain fronts resulted in the model calculating flow of mountain block recharge westward from the Sandia Mountains (on the eastern margin of the basin at Albuquerque) all the way to the Rio Grande at Albuquerque. Thus, the model indicated that water pumped at Albuquerque was recharged along the eastern mountain front. Although some stable isotope data on water from public supply wells at Albuquerque (Yapp (1985) [652]) suggested a Rio Grande source of the water beneath most of Albuquerque, these data were not accounted for in development of the Kernodle et al. (1995) [651] model.

Further studies by the USGS (1995–2001) and other federal and state agencies were conducted to improve the understanding of the hydrology, geology and land surface characteristics of the Middle Rio Grande Basin and to provide the scientific information needed for water resource management. The investigations included:

- (a) Detailed geological mapping and high resolution airborne geophysics to better characterize faults and hydrological properties;
- (b) Use of chemical and environmental tracers to quantify mountain front recharge, characterize river–aquifer interaction and improve knowledge of the flow system;
- (c) Groundwater flow modelling.

A series of 20 deep monitoring well clusters were drilled during the investigation, typically with 3–6 completions at each location. Most of these were in the vicinity of Albuquerque with a maximum depth of 550 m below the land surface and open intervals, typically of 1.5 m at each discrete depth. About 280 groundwater samples from wells and springs were collected throughout the basin and analysed for a wide range of chemical and isotopic constituents, including 30 major and minor elements, stable isotopes of water (²H and ¹⁸O), carbon isotopic composition (¹³C and ¹⁴C) of disolved inorganic carbon (DIC), dissolved nitrogen (N₂), argon (Ar), helium (He), ${}^{3}He/{}^{4}He$ isotope ratio, neon (Ne), sulphur hexafluoride (SF₆), CFCs and tritium (${}^{3}H$). These and additional chemical and hydrogeological data are tabulated and discussed in Plummer et al. (2004) [49]. Selected observations based on the stable isotope, ${}^{14}C$, helium and water chemical composition data are discussed below.

12.4. STABLE ISOTOPES, ⁴He, RADIOCARBON AGES AND HYDROCHEMICAL ZONES

12.4.1. Stable isotopes

Groundwater of the Middle Rio Grande Basin varied widely in stable isotopic composition, due mostly to the source of recharge and age (palaeoclimatic variation). The δ^2 H composition of the groundwater varied more than 50‰ throughout the basin (Fig. 12.4). Most of the stable isotope



FIG. 12.4. Variations in the stable isotopic composition of groundwater samples (blue + signs) in the Middle Rio Grande Basin. The solid line shows the least squares fit to the values and is compared to the global meteoric water line (dashed line). The red circles show the median isotopic composition of the hydrochemical zones (12 zones of recharge and one of discharge; see Fig. 12.12). The data suggest that discharge from the basin is dominated by water recharged from the Rio Grande (central zone and water from the west-central zone). There is typically more than 50‰ variation in δ^2 H of Middle Rio Grande Basin groundwater (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]).



FIG. 12.5. The $\delta^2 H$ isotopic composition, in per mille, of groundwater was mapped throughout the basin and is indicative of the source of recharge. Contours for deuterium align generally north to south in the central part of the basin, parallel to the regional north to south direction of groundwater flow (from Plummer et al. (2004) [51]).



FIG. 12.6. $\delta^2 H$ composition of groundwater from narrow-screened monitoring wells, mostly in the Albuquerque vicinity, as a function of depth below the water table (Plummer et al. (2004) [49]).

values plotted below the global meteoric water line (Fig. 12.4) and fitted a least squares line of $\delta^2 H = 7.62 \delta^{18}O + 2.48$.

Spatial patterns in the chemical and isotopic composition of groundwater were recognized and mapped basin-wide for approximately the upper 60 m of the aquifer (Plummer et al. (2004) [49]). The contours for deuterium (Fig. 12.5) aligned generally north to south in the central part of the basin, parallel to the regional north to south direction of groundwater flow, and reflected the isotopic composition of the source.

The most depleted water was found throughout the west-central part of the basin. Enriched water was found in the western and south-western parts of the basin, -90s% values in δ^2 H were found along the Rio Grande, and the -70s and -80s% range occurred along the eastern and northern margins of the basin (Fig. 12.5). The δ^2 H composition of groundwater from the narrow-screened monitoring wells, mostly in the Albuquerque vicinity, show that δ^2 H was nearly constant to depths of more than 400 m below the water table at Albuquerque, and was similar in isotopic composition to that of the Rio Grande measured during the late winter to spring runoff period (Fig. 12.6). The red line in well nest (F) (Fig. 12.6) is in the depleted zone that extends down through the west-central part of the basin. The green line (J) is adjacent to the eastern mountain front. Line A (magenta) appears to be water recharged at low altitude along the northern margin of the basin. Other well nests (K, S, I) appear to contain fractions of either depleted or enriched water at intermediate depths.

12.4.2. Carbon-14 model age

The measured ¹⁴C content of DIC in groundwater from 211 sites ranged from 0.62 to 123.1 pmc. Most of the contours in ¹⁴C align in a north–south direction that roughly parallels the pattern in δ^2 H (Fig. 12.7). The unadjusted ¹⁴C model age of DIC in the upper 60 m of the aquifer (Fig. 12.8) is based on the measured non-normalized ¹⁴C pmc value of DIC in groundwater and was calculated using an initial ¹⁴C value of 100 pmc in recharge water (see Fig. 4.1, Chapter 4). Patterns in ¹⁴C model age were similar to the patterns in ¹⁴C content of the DIC. Carbon-14 values were highest along the eastern mountain front, along the northern margin of the basin, and along the inner valley of the Rio Grande



FIG. 12.7. Carbon-14 content in pmc of dissolved inorganic carbon in the upper approximately 60 m of the aquifer throughout the Middle Rio Grande Basin (after Plummer et al. (2004) [51]).

(Fig. 12.7, dark brown pattern, >80 pmc). Relatively high ¹⁴C values also occurred near areas where surface water inflow (from Abo Arroyo, the Rio Puerco and the Jemez River) enters the basin.

Waters with low ¹⁴C values of the DIC were present along the western and south-western basin margins (<20 pmc). Another zone of low ¹⁴C content extended through nearly the entire length of the west-central part of the basin.

Along the eastern mountain front, values of ¹³C of DIC tended to be more negative (typically -12%) than those of DIC further down gradient into the aquifer (typically -7 to -8%). The change in δ^{13} C of DIC could indicate dissolution of carbonate rock fragments of marine origin, which may occur in low abundance within the alluvial and fluvial sediments of the basin. If so, it would then be necessary to adjust the ¹⁴C model ages for carbonate rock dissolution. However, geochemical mass balance calculations indicated that water–rock reactions were probably minimal in the primarily siliciclastic basin-fill sediment and that the shift in δ^{13} C must be attributed to other processes. The geochemical modelling supported the unadjusted ¹⁴C model ages that were then well defined in the range from modern to more than 30 ka BP (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]; Plummer et al. (2004) [51]) (Fig. 12.8). The shift in δ^{13} C isotopic composition with distance of flow (and age) into the basin was concluded to be the result of climate change. In the past few thousand years, or less, there appears to have been an increase in C₃ plant abundance relative to C₄ plants in the recharge areas of the Middle Rio Grande Basin (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]; Plummer et al. (2004) [51]), resulting in a decrease in δ^{13} C of DIC along the eastern mountain front. The cause is



FIG. 12.8. Unadjusted ¹⁴C model age in thousands of years BP in the upper approximately 60 m of the aquifer throughout the Middle Rio Grande Basin (after Plummer et al. (2004) [51]).

not known but possible factors include increased precipitation in recharge areas and, more recently, an increase in the atmospheric mixing ratio of CO_2 (Plummer et al. (2004) [49]; Plummer et al. (2004) [51]). Geochemical modelling of water–rock reactions and quantification of mixing of waters from adjacent hydrochemical zones were critical in demonstrating that geochemical corrections were negligible in the siliciclastic sediments of the Middle Rio Grande Basin, even though a shift to enriched $\delta^{13}C$ of DIC was evident between the recharge area and older waters further down gradient.

12.4.3. Helium-4

Helium-4 concentrations in Middle Rio Grande Basin groundwater increased with depth below the water table and with ¹⁴C model age (Fig. 12.9). The ⁴He concentrations ranged from values near air–water equilibrium ($\sim 5 \times 10^{-8}$ cm³ STP/g) to about 1.2×10^{-4} cm³ STP/g.

The isotopic composition of dissolved helium, along with amounts of dissolved He and Ne, were determined by mass spectrometry in a relatively small subset of the Middle Rio Grande Basin samples — basically a subset that was thought to contain a fraction of young water that might possibly be dated by the ³H–³He method. Unfortunately, relatively few of the samples could be dated by this method due to large excesses of (predominantly) mantle-derived helium.

A log–log plot of the ³He/⁴He isotope ratio as a function of the Ne/He ratio for these samples indicates two sources of He in the Middle Rio Grande Basin waters: (i) a crustal source with a ³He/⁴He



FIG. 12.9. Three dimensional plot showing ⁴He concentration as a function of depth below the water table and ¹⁴C model age for waters from the eastern mountain front, central zone (palaeo-Rio Grande water) and the west-central hydrochemical zones (hydrochemical zones are defined in Section 12.4.4).



FIG. 12.10. Plot showing variations in the 3 He/ 4 He ratio of dissolved He as a function of Ne/He for various hydrochemical zones of the Middle Rio Grande Basin (the hydrochemical zones are defined in Section 12.4.4). The red circles denote samples containing tritium of more than 1 TU. Most of the groundwater samples of the Middle Rio Grande Basin contain a mantle signature of 3 He/ 4 He ratio near 1 × 10⁻⁶. Samples with a 3 He/ 4 He ratio greater than 1 × 10⁻⁶ have Ne/He ratios near those of water in equilibrium with air and probably are bomb era waters infiltrated from the Rio Grande; some of these samples contain more than 50 TU of tritiogenic 3 He.

ratio of approximately 1×10^{-8} , and (ii) a mantle source, which predominates most of the samples, with a ³He/⁴He ratio near 1×10^{-6} (Fig. 12.10).

The red circles in Fig. 12.10 denote those samples that contain more than 1 TU of tritium. Many of the tritiated samples plot along the Ne/He line for water in equilibrium with air (at 1500 m, 14°C) and were identified as samples of Rio Grande water that has infiltrated the Middle Rio Grande Basin. The ³He/⁴He ratio of these samples indicates some of them originally contained more than 50 TU of tritiogenic ³He, and are likely representative of Rio Grande water from the bomb era. The largest amount of tritium in any of the samples was 28 TU when sampled in 1996–1998. A few samples probably contain a crustal He signature near 1×10^{-8} , and are derived from water sourced outside the eastern basin margin.

The samples containing more than 1 TU (red-circled samples in Fig. 12.10) and having a Ne/He ratio less than that of water in equilibrium with air are mixtures of young and old water pumped from wells open to both the shallow aquifer and considerable depth (several hundred metres). Excluding the samples with a crustal ${}^{3}\text{He}/{}^{4}\text{He}$ signature, there are 23 samples with Ne/He < 1.0. The average ${}^{3}\text{He}/{}^{4}\text{He}$ ratio of these samples was $1.02 \pm 0.15 \times 10^{-6}$. No trend was recognized in He isotope ratio with regard to source or location in the basin for those samples with a mantle signature (Fig. 12.10).

It appears that the samples with the crustal signature represent relatively shallow water, with a recharge source outside the eastern margin of the basin. The one sample originally identified as being from the eastern mountain front zone with the lowest ³H/⁴He ratio (Fig. 12.10) was obtained down gradient from where the other 'exotic' samples were obtained and the water could have originated along with that of the other 'exotic' samples just outside the eastern margin of the basin. All of the samples with the mantle signature were obtained within the Middle Rio Grande Rift zone (Fig. 12.11).



FIG. 12.11. Helium-4 accumulation in the Middle Rio Grande Basin plots in two groups with average accumulation rates of about 1.3×10^{-10} cm³ STP · g⁻¹ · a⁻¹ and 0.05×10^{-10} cm³ STP · g⁻¹ · a⁻¹. Many of the samples with the lowest ⁴He accumulation rates are from the west-central zone, beneath deep unsaturated zones.



FIG. 12.12. Location of 12 sources of water to the Middle Rio Grande Basin identified based on chemical and isotopic characteristics (after Plummer et al. (2004) [49]). The arrows show the inferred directions of groundwater flow based on the chemical and isotopic data.

The rate of He accumulation varied more than two orders of magnitude in the Middle Rio Grande Basin samples (Fig. 12.11). Using the unadjusted ¹⁴C model ages that were more than 1 ka, and calculating the He accumulation rates for samples from monitoring wells (and other narrow-screened wells), the He accumulation rates varied from 0.044 to 7.7×10^{-10} cm³ STP \cdot g⁻¹ \cdot a⁻¹. This rate can be compared to an average value of 1.3×10^{-10} reported by Solomon et al. (1996) [295] for a variety of sedimentary environments. Some of the samples, particularly from the west-central and central zones have very low ⁴He accumulation rates (Fig. 12.11) and may be in sediment that is particularly low in U and Th content (see Chapter 8). Given the observed wide variations in He accumulation rate, additional data on U and Th abundance in sediment of the Middle Rio Grande Basin, and data on He flux in the basin would be needed for application of He accumulation as a reliable age indicator in this complex hydrogeological environment.

12.4.4. Hydrochemical zones

Using much of the available chemical and isotopic data, including the deuterium, ¹⁴C and major and minor element composition, 12 separate zones of recharge to the basin and a zone of groundwater discharge (zone 13) were recognized (Plummer et al. (2004) [49]). The hydrochemical zones (Fig. 12.12) provided insight into likely recharge sources, flow paths and aquifer properties. Zone 12 (Fig. 12.12) was determined to be water sourced from the Rio Grande. Mountain front recharge waters were identified along the northern, eastern and southern margins of the basin (zones 1, 8 and 6; Fig. 12.12). Palaeowater that entered the basin along the northern margin either as underflow (subsurface inflow) or recharge from the Jemez Mountains north of the basin margin, extends down the west-central part of the basin. It flows beneath zone 2 in the north, and beneath parts of zones 1 and 12 in the northern and central parts of the basin, as denoted by the dashed line on Fig. 12.12. The arrows (Fig. 12.12) show the inferred directions of flow based on identified source and location of hydrochemical zones. Most of the flow in the basin appears to be from north to south.



FIG. 12.13. Map showing pre-development water levels in the Middle Rio Grande Basin, inferred directions of flow based on the pre-development potentiometric surface and location of major faults (Bexfield and Anderholm (2000) [653]; Plummer et al. (2004) [49]; Plummer et al. (2004) [50]).

12.4.5. Pre-development water levels

The pre-development water levels (Fig. 12.13) were constructed from water level measurements from the mid-1930s in the vicinity of Albuquerque, NM that predate groundwater production, and other sources of data throughout the basin that are representative of pre-development conditions (Bexfield and Anderholm (2000) [653]). An interesting feature of the water table surface is a groundwater trough that extends through much of the west-central part of the basin. The trough was originally observed in the early 1960s (Titus (1963) [654]). The arrows show the implied directions of groundwater flow based on the pre-development water levels.

The pre-development hydraulic-head map (Bexfield and Anderholm (2000) [653]; Bjorklund and Maxwell (1961) [655]; Titus (1961) [656]) is broadly consistent with the primary direction of groundwater flow indicated by geochemical data, but there are some apparent inconsistencies. In particular, the pre-development hydraulic heads indicate greater east–west components of flow through the centre of the basin into the groundwater trough than are suggested by the orientation of the hydrochemical zones. The differences in flow direction indicated by hydraulic heads compared with geochemical tracers are likely associated with different time horizons — the chemistry being on the 10 ka timescale and the pre- development water levels on a more recent timescale.



FIG. 12.14. Cross-section of the Upper Santa Fe aquifer system at Albuquerque showing ranges of ¹⁴C model age as a function of depth and water sources. The slanted grey patterns denote approximate locations of hydrochemical zone boundaries. The direction of groundwater flow is generally north to south, that is, out of the plane of the cross-section (see Fig. 12.2 for approximate location of cross-section; after Plummer et al. (2004) [49]).



FIG. 12.15. Comparison of $\delta^2 H$ in groundwater recharged along the eastern mountain front of the Middle Rio Grande Basin and infiltration from the Rio Grande (central zone) as a function of ¹⁴C model age (Plummer et al. (2004) [49]; Plummer et al. (2004) [51]).

12.4.6. Variations in ¹⁴C model age with depth

A cross-section of the Middle Rio Grande Basin aquifer system through central Albuquerque, NM (Fig. 12.14; at approximately the same location as cross-section A–A' in Fig. 12.2), shows ranges of ¹⁴C model ages (less than 5 ka, 5–20 ka and >20 ka) in relation to water sources (hydrochemical zones).

There is a large central core of palaeo-Rio Grande water beneath Albuquerque, the base of which was not located. The boundary between water recharged along the eastern mountain front and infiltration from the Rio Grande is nearly vertical. Palaeowater of the west-central zone flows beneath palaeo-Rio Grande water under the river. Palaeowater of more than 20 ka was at the water table beneath deep unsaturated zones west of Albuquerque.

12.4.7. Stable isotopes, deuterium excess and radiocarbon age

During the past 5 ka, δ^2 H of water from the central zone (Rio Grande origin) increased by nearly 6‰ from a minimum near –98‰; and δ^2 H of moisture recharged along the eastern mountain front became more depleted in ²H, by about 7‰ (Fig. 12.15).

Most groundwater samples from the eastern mountain front zone, with radiocarbon ages greater than 5 ka BP, ranged in ²H isotopic composition from about –90 to –70‰ with little evidence of temporal variability (Fig. 12.15). Water recharged from the Rio Grande to the central zone apparently had a minimum δ^2 H isotopic composition at approximately 5 ka BP, reached a maximum at about 15 ka BP, but was relatively depleted in ²H at about 22 ka BP (Fig. 12.15). The changes in δ^2 H of water from the central and eastern mountain front zones during the past 20 ka were interpreted in terms of changes in palaeoclimatic conditions (Plummer et al. (2004) [49]; Plummer et al. (2004) [51]), i.e. (i) changes in temperature; (ii) changes in the balance between the amount of precipitation falling within



FIG. 12.16. Comparison of the deuterium excess in groundwater recharged from the palaeo-Rio Grande, water recharged along the eastern mountain front, and palaeowater from the west-central part of the Middle Rio Grande Basin as a function of ¹⁴C model age. Water recharged to the west-central zone during the last glacial maximum had the lowest deuterium excess and that recharged 3–5 ka BP during the mid-Holocene warm period has relatively high deuterium excess.

the basin and that falling within the mountain watershed source areas to the Rio Grande; and (iii) shifts in season of predominant runoff (snowmelt) affecting discharge within the Rio Grande. Although affected by many climatic variables, the most depleted waters in the Middle Rio Grande Basin had ¹⁴C model ages of about 20 ka. Similarly, the waters with the lowest recharge temperatures, based on dissolved N₂ and Ar measurements, also had ¹⁴C model ages of about 20 ka (Plummer et al. (2004) [51]), consistent with cooling during the LGM. Therefore, the stable isotope and dissolved gas data helped to corroborate the ¹⁴C model ages. During the past 5 ka, the δ^2 H isotopic composition of recharge along the eastern mountain front decreased about 7‰ (Fig. 12.15), suggesting an average cooling of about 1.5°C following the mid-Holocene warm period (Plummer et al. (2004) [49]; Plummer et al. (2004) [51]). Over the same time span, the δ^2 H isotopic composition of Rio Grande water increased 5–10‰, consistent with a shift in season of peak snowmelt into the beginning of the summer monsoon season, which is again, likely a result of cooling during the past 5 ka.

In Fig. 12.16, the deuterium excess as a function of ¹⁴C model age for waters from three hydrochemical zones is examined: (i) the central zone, which represents palaeo-infiltration from the Rio Grande; (ii) the eastern mountain front zone, which represents mountain recharge along the eastern margin of the basin; and (iii) the palaeowaters that fill the west-central part of the basin, which may represent recharge from the Jemez Mountains north of the basin or subsurface inflow from north of the Middle Rio Grande Basin.

The deuterium excess, d_{excess} in per mille, is defined as $d_{\text{excess}} = \delta^2 \text{H} - 8 \times \delta^{18}\text{O}$, and can be related to relative humidity (and, thus, sea surface temperature) for the oceanic source water (Jouzel et al. (1982) [657]; Merlivat and Jouzel (1979) [658]; Straaten and Mook (1983) [59]). The highest values of d_{excess} were found in waters of the eastern mountain front zone (12.6‰), and the lowest values were in waters from the west-central zone (0.6‰). The median values of d_{excess} for water from the west-central, eastern mountain front and central zones were 5.0, 9.3 and 7.2, respectively during the past 40 000 radiocarbon years. Values of d_{excess} are expected to be low during the last glacial minimum (LGM) due to lower sea surface temperature, resulting in elevated relative humidity over the oceanic source relative to today (Jouzel et al. (1982) [657]; Merlivat and Jouzel (1979) [658]; Straaten and Mook (1983) [59]), and elevated during warm periods due to lower relative humidity at the source in response to the elevated sea surface temperature. The data of Fig. 12.16 at least partially support this expectation, showing a peak in d_{excess} approximately 3–5 ka during the time of the mid-Holocene warm period, and low values of d_{excess} at approximately 20–25 ka during the LGM. This, at least qualitatively, provides further evidence in support of the ¹⁴C model ages.

A strong El Nino was observed in the Pacific Ocean during the period 1997–1998 (Oceanic ENSO Index of 2.5, http://ggweather.com/enso/oni.htm). Monthly samples of Rio Grande water collected just north of Albuquerque from December 1996 through May 1999 were analysed for stable isotope composition (Plummer et al. (2004) [49]). Values of d_{excess} increased from about 5‰ in late 1996 to 8‰ in January 1998, then fell again to about 4–5‰ in late 1998 to early 1999. Although a number of factors, including moisture source, can affect the values of d_{excess} , this correlation suggests there may be, at least in part, a connection today between d_{excess} of precipitation reaching the Middle Rio Grande Basin and sea surface temperatures in the Pacific Ocean.

12.4.8. Carbon-14 model age profiles and recharge rates

In addition to providing information on spatial variations in ¹⁴C model age throughout the basin, the radiocarbon data help to constrain recharge-rate estimates. Along the eastern mountain front, there appear to be two different age–depth relations (Fig. 12.17). Water from the eastern mountain front zone found north of Albuquerque, or south of Tijeras Arroyo, just south of Albuquerque (red symbols), had a relatively high age gradient (approximately 6.6 a/cm) in relation to waters from the eastern mountain front zone at Albuquerque (approximately 0.4 a/cm) (blue symbols; Fig. 12.17). Apparently, over at least the past 10 ka, there was appreciably more recharge along the eastern mountain front at



FIG. 12.17. Carbon-14 model ages of dissolved inorganic carbon in groundwater of the Middle Rio Grande Basin at Albuquerque and in areas just north and south of Albuquerque (south of Tijeras Arroyo) as a function of depth below the water table. Two depth–age gradients imply recharge rates, assuming 30% porosity, of 7.5 mm/a at Albuquerque compared to 0.5 mm/a north and south of Albuquerque. The fit to the exponential model suggests a slightly higher recharge rate, 8 mm/a, at Albuquerque. The depth–age relations can be related to lithologic and structural features along the eastern margin of the basin (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]).

Albuquerque than either to the north or south of Albuquerque. Assuming a porosity of 30%, a recharge rate of 7.5 mm/a is found at Albuquerque from the linear depth–age relation (blue line) compared to 0.5 mm/a for recharge north and south of Albuquerque from the linear depth–age relation (red line). If an exponential model is fitted to the data at Albuquerque, assuming an aquifer thickness of 500 m, the recharge rate is 8 mm/a (green line). Factors that may contribute to this difference are: (i) a greater thickness of ancestral Rio Grande sands and gravels at Albuquerque than elsewhere along the eastern mountain front (Hawley and Haase (1992) [649]); (ii) the presence of structural features, including the Hubble Bench and Tijeras and Hubble Springs fault zones to the south, which place low permeability rocks at shallow depths; and (iii) higher precipitation rates along the Sandia Mountains at Albuquerque than along lower altitude portions of the eastern mountain front.

12.5. SUMMARY OF CHEMICAL AND ENVIRONMENTAL TRACER CONSTRAINTS ON THE FLOW SYSTEM

This study demonstrates some of the benefits of obtaining a diverse and extensive chemical and isotopic dataset when characterizing hydrological processes and tracer model age in groundwater systems and when there is a need to refine the conceptual model of the groundwater flow system. A wide range of chemical and isotopic constituents were identified in groundwater from the Middle Rio Grande Basin (Plummer et al. (2004) [49]; Plummer et al. (2004) [50]; Plummer et al. (2004) [51]). Selected results from stable isotope, ¹⁴C, helium and major element chemistry are summarized below.

The δ^2 H composition of groundwater in the Middle Rio Grande Basin varied regionally more than 50‰, and in combination with other chemical and isotopic constraints, allowed recognition and mapping of flow from 12 separate recharge sources to the basin, and a zone of discharge.

The boundaries between waters of different recharge sources align parallel to the general north to south direction of groundwater flow, a property of inert tracers in groundwater systems (Glynn and Plummer (2005) [15]), and are generally in agreement with regional north to south flow directions indicated by the pre-development water levels.

The chemical and isotopic patterns trace groundwater flow regionally on the timescale of the aquifer system (tens of thousands of years), but locally are inconsistent with flow directions implied by a trough in the pre-development surface through the central part of the basin. The trough in the pre-development surface is thought to be the response of the water levels to a recent lowering of recharge rate along the basin margin (see modelling section).

The stable isotope data showed that groundwater at Albuquerque is mostly derived from the Rio Grande and not from the eastern mountain front, as early groundwater models had predicted.

Carbon-14 content was highest along the eastern mountain front, along the northern margin of the basin, along the inner valley of the Rio Grande, and along other surface water sources, indicating areas of recent recharge (past several thousands of years).

In this semi-arid region, the initial ¹⁴C content in recharge areas was found to be near 100 pmc in pre-bomb waters (open system conditions). Geochemical mass balance calculations showed that water–rock interactions were negligible in the primarily siliciclastic sediments of the Middle Rio Grande Basin, justifying use of the unadjusted ¹⁴C model age. Shifts in the stable isotope composition of mountain front recharge over the past 5 ka, and of palaeo-Rio Grande water over the past 20 ka were consistent with known climate variation and support the unadjusted ¹⁴C model ages. Other evidence helping to corroborate the ¹⁴C model ages was found in recharge temperatures calculated from dissolved N₂ and Ar data, and in the deuterium excess as a function of ¹⁴C model age.

Gradients in ¹⁴C model age (and inferred recharge rates) varied by more than an order of magnitude in the vicinity of Albuquerque, resulting mostly from geological factors.

The waters sampled as a part of the investigation were representative of only relatively shallow parts of the aquifer system (typically, the upper 60 m of the aquifer, though some samples were from as deep as 500 m below the water table). The lowest ¹⁴C content measured was 0.6 pmc and beyond the usefulness of radiocarbon as an age indicator.

Excess helium in the Middle Rio Grande Basin is dominated by a mantle source and has a remarkably uniform 3 He/ 4 He ratio of $1.02 \pm 0.15 \times 10^{-6}$. Helium accumulation rates in groundwater from the Middle Rio Grande Rift vary more than two orders of magnitude and could be used only as a quasi-age indicator in the Middle Rio Grande Basin.

12.6. GROUNDWATER MODEL DEVELOPMENT

A groundwater flow model developed with MODFLOW (McDonald and Harbaugh (1988) [71]) was used to estimate recharge to the Middle Rio Grande Basin. Travel times to observation wells were calculated using MODPATH (Pollock (1994) [611]). The MODFLOW and MODPATH representations of the basin were calibrated using UCODE (Poeter and Hill (1998) [659]). The model domain was divided into a rectilinear grid comprised of 156 rows and 80 columns of equally spaced 1 km sized cells (Sanford et al. (2004) [47]; Sanford et al. (2004) [48]). The eastern and western model boundaries mostly were coincident with faults that either act as barriers to horizontal groundwater movement or separate areas with different thickness of permeable sediment (Kernodle et al. (1995) [651]). The vertical extent of the aquifer system was represented by nine model layers of variable thickness down to the base of the Santa Fe Group sediments at 2400 m below sea level at the deepest point.

River-cell boundaries were implemented over the width of the inner valley of the Rio Grande, and along the Jemez River and Rio Puerco to represent the groundwater/surface water interaction along those waterways. The recharge was divided into segments along the eastern and southern mountain fronts and arroyos. Several underflow segments were specified, extending the length of the northern and western model boundaries. The hydraulic conductivity zones for the basin were based on the three dimensional geological model of Cole (2001) [647] (see also Bartolino and Cole (2002) [612]). A total of 18 hydraulic conductivity zones were defined within the groundwater flow model (Sanford et al. (2004) [47]; Sanford et al. (2004) [48]). Vertical conductances in the groundwater flow model were divided into 12 zones — the associated parameters were represented as values of vertical anisotropy. Two fault zones, representative of the Cat Mesa fault zone in the south-western part of the basin and the Sandia Fault zone along the eastern mountain front at Albuquerque, were added to the groundwater flow model as discrete (low), hydraulic conductivity zones (Fig. 12.13).

Porosity for the unconsolidated sediment of the basin was estimated from field measurements (Haneberg (1995) [660]; Stone et al. (1998) [661]) and assigned separately for the model layers, beginning with 36% for model layer 1 and decreasing 2% per layer down to 20% for layer 9.

Hydrochemical tracer data were used as a part of the calibration of the groundwater flow model. Groundwater ages obtained from ¹⁴C measurements were one set of these data. Simulated ages were obtained by using MODPATH to track the line of travel of a parcel of water from the observation well backwards to its recharge location. Hydrodynamic dispersion in these calculations was neglected, as the effect of dispersion on the concentrations from a nearly invariant source over a 100 km basin would be negligible for values of longitudinal dispersivity less than 1 km (Johnson and DePaolo (1996) [624]; Phillips et al. (1989) [39]).

Another source of tracer information that was used for model calibration was the delineation of the hydrochemical zones (Fig. 12.12), representing different water sources. MODPATH was used to simulate the locations of the boundaries between hydrochemical zones, which were compared to the observed locations (Fig. 12.12).

The groundwater model was calibrated using a combination of a non-linear least squares regression method as it is implemented in the computer code UCODE (Poeter and Hill (1998) [659]), and manual adjustment of individual parameters. A total of 200 hydraulic heads, 200 ¹⁴C measurements, and the locations of two of the river water hydrochemical zones within nine hydrochemical target regions were used as observations, making a grand total of 409 observations (Sanford et al. (2004) [47]; Sanford et al. (2004) [48]). The groundwater model was first set up to simulate steady state groundwater flow prior to the development of groundwater as a resource within the basin. The head data were compiled by Bexfield and Anderholm (2000) [653] from many sources (Fig. 12.13), and the hydraulic heads from the final simulation matched relatively well with the observed heads (Sanford et al. (2004) [47]; Sanford et al. (2004) [48]).

Values for hydraulic conductivities were calibrated to values mostly between 3×10^{-6} and 3×10^{-5} m/s, and were similar to estimates from previous models (Kernodle et al. (1995) [651]; McAda and Barroll (2002) [662]; Tiedeman et al. (1998) [663]) and prior field measurements concerning the basin-fill material (Thorn et al. (1993) [21]). The anisotropy (K_v/K_h) was calibrated for 12 individual zones within the basin, and the calibrated values all ranged between 1×10^{-4} and 1×10^{-2} . These values are consistent with what might be expected for a layered aquifer system where the individual layers are isotropic and have hydraulic conductivity values that vary by two to four orders of magnitude.

During each of the time steps, all recharge and underflow boundary cells were multiplied by a single coefficient. These coefficients, or multipliers, were all given an initial value of 1.0 to reproduce the conditions in the steady state simulation. The multiplier for each time step was then adjusted until an optimum fit was obtained between the measured and simulated observations. The non-linear regression routine in UCODE was initially used to reduce the total sum of the squared errors, but eventually the individual recharge multipliers were adjusted manually to obtain the 'best-fit' multiplier values.

The observed hydraulic heads are strongly correlated with the simulated heads along the 1:1 line (Fig. 12.18(a)), but the observed ¹⁴C pmc values show a substantially greater amount of scatter about the 1:1 line compared to the simulated values (Fig. 12.18(b)). This poorer fit to the ¹⁴C data than to the head data results from the fact that the heads represent a smoothly varying potential field that can be fitted without much difficulty to the solution of the flow equation, but the groundwater ages are



FIG. 12.18. Comparison of (a) observed and simulated hydraulic heads, and (b) observed and simulated ¹⁴C values in per cent modern carbon (Sanford et al. (2004) [47]; Sanford et al. (2004) [48]).

a function of velocities that are, in turn, a function of the first derivatives of the groundwater potential field and, thus, are more difficult to fit.

This difficulty in matching observed and simulated ¹⁴C values exists because, although the travel time to a point in the aquifer is an integration of the upstream velocity field, errors in calculated velocities can accumulate down a flow path. In addition, multiple source areas in the Middle Rio Grande Basin (Fig. 12.12) create age patterns within the basin that are discontinuous (Fig. 12.19), increasing further the complexity and difficulty in fitting the age related simulations to observations. The multiple sources of water in the Middle Rio Grande Basin create numerous flow divides. These divides often have very sharp gradients in age across them and are difficult to match exactly, increasing the scatter in simulated versus observed ¹⁴C model ages.

The final model configuration reproduced the groundwater trough that extends north to south through the west-central part of the basin, although not as far north as some of the measured water levels indicate (Fig. 12.13). Earlier models (e.g. Kernodle et al. (1995) [651]) did not manage to reproduce this feature. Attempts were also made by Tiedeman et al. (1998) [663] to investigate different conceptual models of what was creating the trough, including a high permeability zone or a north–south trending fault. Sanford et al. (2004) [48], however, demonstrated that by lowering the basin boundary recharge in the model, the aquifer system changed from one dominated by the movement of water from the boundaries towards the Rio Grande to one dominated by water leaking from and back into the Rio Grande. The latter conceptual system results in heads to the west of the Rio Grande that are lower than the river, and is consistent with the presence of the trough and the relatively low recharge values estimated with the model. The final model configuration also reproduces the section of the Rio Grande that loses water into the aquifer, just north of Albuquerque (Fig. 12.13). Additional details of the groundwater flow model and calibration procedure are given in Sanford et al. (2004) [47], Sanford et al. (2004) [48] and Plummer et al. (2004) [51].

From the water level contours (Fig. 12.13), one can see that groundwater moves away from the Rio Grande, both to the west towards the trough, and to the south beneath Albuquerque, as is also shown by the pre-development water table map (Fig. 12.13). This zone of Rio Grande water beneath the city of Albuquerque is also corroborated by the hydrochemical zone delineation (Figs 12.12 and 12.14).



FIG. 12.19. Simulated groundwater flow model ages at relatively shallow depths (50–100 m, model layer 2) and deeper depths (300–500 m, model layer 6). Simulated hydrochemical zones (source areas) are delineated by black lines and labelled (Plummer et al. (2004) [51]; Sanford et al. (2004) [47]; Sanford et al. (2004) [48]).

Simulated groundwater flow model ages are shown in Fig. 12.19 for two of the model layers. Young water (<3000 a), represented by the dark blue areas in layer 2, is present near the mountain fronts where recharge occurs at the land surface, and along the Rio Grande and Rio Puerco near where the rivers are losing water to the aquifer system. Flow model ages in layer 6 at depths of 300–500 m below the water table are shown in the right panel of Fig. 12.19. A cross-section of the simulated ages reveals a general pattern of increasing simulated age with depth, but the heterogeneity of the system in some places creates local inversions where old water is simulated above younger water moving through a more permeable zone. The hydrochemical zones were also simulated with MODPATH, using source area delineation of path lines, as shown in Fig. 12.19.

Recharge was not specified directly for the Rio Puerco and the Jemez River in the model, but was calculated through their riverbed conductance values. The calculated recharge rates were 0.14 m³/s for the Rio Puerco and 0.01 m³/s for the Jemez River (Plummer et al. (2004) [51]; Sanford et al. (2004)

[47]; Sanford et al. (2004) [48]). The recharge for the Rio Puerco was similar to values used in earlier models, but the Jemez River recharge value was much lower. Recharge from the eastern mountain front was estimated to be 0.33 m³/s, with 0.04 m³/s of additional recharge from Abo Arroyo. These numbers are appreciably lower than previous estimates that were based on rainfall–runoff equations (Kernodle et al. (1995) [651]), but are similar to estimates of recharge of 0.35 and 0.05 m³/s along the eastern mountain front and Abo Arroyo and vicinity, respectively, made from a field study of chloride mass balance (Anderholm (2001) [664]). McAda and Barroll (2002) [662] created a groundwater flow model of the basin partially incorporating preliminary results from this study. They used a combination of some higher recharge values used in the earlier studies, and lower values estimated by Anderholm (2001) [664], Sanford et al. (2004) [47] and Sanford et al. (2004) [48].

Total recharge to the basin was estimated by Sanford et al. (2004) [47] and Sanford et al. (2004) [48] to be 2.14 m³/s, with 0.78 m³/s of the total attributed to infiltration from the Rio Grande. The basinmargin recharge estimated from the model, 1.37 m³/s, is one fourth of the 5.45 m³/s estimate used in the Kernodle et al. (1995) [651] model and one half of that used by McAda and Barroll (2002) [662]. Overall, the lower recharge values are consistent with the presence of the groundwater trough and zone of Rio Grande water in the central basin. McAda and Barroll (2002) [662] partially reproduced these features by adding N–S trending fault barriers in the centre of the basin.

12.7. REFINING CONCEPTUALIZATION OF GROUNDWATER FLOW IN THE BASIN

Some of the results of Plummer et al. (2004) [49], Plummer et al. (2004) [50], Plummer et al. (2004) [51], Sanford et al. (2004) [47] and Sanford et al. (2004) [48] helped change conceptualization of groundwater flow in the Middle Rio Grande Basin.

The Kernodle et al. (1995) [651] model obtained a modern basin-scale recharge rate of 5.45 m³/s, which was mostly derived from mountain front and arroyo recharge, with no net recharge from the Rio Grande. In comparison, the Sanford et al. (2004) [47] and Sanford et al. (2004) [48] model found a basin-scale recharge rate of 2.14 m³/s, which is only about 39% of the previous model, with mountain front recharge at Albuquerque only about 20% of the previous model. Further, the Sanford et al. model shows that there is much more recharge from the Rio Grande than previously thought (36% of the basin recharge is from the Rio Grande). From a water management perspective, the results show that there is even less modern recharge to the aquifer in the vicinity of Albuquerque than previously thought (Fig. 12.20). The Sanford model benefited from the revised hydrogeological data for the basin, and was calibrated using water levels, the determined ¹⁴C model ages and locations of hydrochemical zone boundaries. The pie areas in Fig. 12.20 are in proportion to the modelled modern basin-wide recharge rate: (a) 5.45 m³/s; (b) 2.14 m³/s.

The Sanford et al. model and hydrochemical data show that groundwater flow paths are generally parallel to the Rio Grande, rather than perpendicular, near the eastern mountain front, and especially beneath Albuquerque.

Most of the locations of the hydrochemical zones are consistent with the pre-development surface, but the groundwater trough is not, and may represent a recent lowering of recharge along the basin margins.

Steep gradients in ¹⁴C model age with depth indicate most flow occurs in upper parts of the aquifer (large vertical anisotropy); spatial differences in ¹⁴C model age gradients indicate differences in geological and hydrological conditions. A recharge rate of 3 cm/a was found along the mountain front at Albuquerque and beneath the Rio Grande at Albuquerque.

There appear to be relatively large amounts of groundwater inflow into the northern part of the basin, either under or from the Jemez Mountains.



FIG. 12.20. Pie diagrams showing modelled quantities of recharge to the Middle Rio Grande Basin, in per cent of each source to the total modelled basin recharge. (a) Kernodle et al. (1995) [651] show a MODFLOW model using an earlier hydrogeological framework, pre-development water levels and assumed mountain front recharge rates that did not account for evapotranspiration. (b) Sanford et al. (2004) [47] and Sanford et al. (2004) [48] is based on a MODFLOW–MODPATH calibration procedure using inverse modelling with UCODE.

12.8. PALAEORECHARGE RATES

Finally, a transient groundwater flow simulation was performed using twelve 2500 a time steps (Plummer et al. (2004) [51]; Sanford et al. (2004) [47]; Sanford et al. (2004) [48]) to investigate the effect of time-varying recharge rates over the past 30 ka. Results from the transient simulation indicate that recharge was greater before 15 ka ago than today. The optimal values for the recharge multipliers are greater than ten for the period between 20 ka and 25 ka BP. Evidence for a wetter climate during this period is present in the Estancia Basin, just east of the Sandia Mountains, in the form of playa lake deposits (Allen and Anderson (2000) [665]; Bachhuber (1992) [666]). Although precipitation may have increased by a factor of approximately 2.5 during the LGM relative to today (Thompson et al. (1999)) [667]), a small percentage increase in rainfall in arid regions can easily lead to a much larger percentage increase in recharge. The palaeorecharge rates from the transient simulation were accompanied by high degrees of uncertainty. Underflows ten times modern rates would also require hydraulic gradients ten times greater, and this rate is highly unlikely, if not physically impossible in some regions. In addition, vertical transverse dispersivity likely contributes additional ¹⁴C to some older waters of the basin, leading to ages that are younger than advective travel times and, in turn, higher palaeorecharge rates. The highest values of palaeorecharge predicted should, therefore, be seen as maximum rates, and likely greater than the actual rates. The results consistently point to an amount of recharge just before or at the beginning of the Holocene that was lower than modern values.

12.9. CONCLUDING REMARKS

The overall lesson from the Middle Rio Grande Basin study is that geochemical and isotopic data were of considerable value in refining the conceptual model of groundwater flow and improving the calibration of numerical models of groundwater flow in the basin. The model was improved by new hydrogeological data collected as a part of this study. The modelling exercise is viewed as an iterative process of data gathering and model refinement (as discussed in Chapter 2).

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Chapter 13

METHODS FOR DATING VERY OLD GROUNDWATER: EASTERN AND CENTRAL GREAT ARTESIAN BASIN CASE STUDY

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13.1. INTRODUCTION

The Great Artesian Basin extends across 1.7×10^6 km² or one fifth of the Australian continent. Annual rainfall ranges from 100 mm in the arid western parts to a maximum of 600 mm near the main recharge areas along the eastern basin margin. Average annual runoff is less than 10 mm and generally less than 5 mm. Ephemeral rivers dominate the land surface of the basin, except for a few perennial rivers in the most northern, tropical parts of the region. Most interior rivers drain into Lake Eyre (a dry salt pan at 12 m below sea level); however, the river waters often evaporate or infiltrate before reaching Lake Eyre because of the long distances. With little or no surface water present in the dry, hot and harsh climate of Australia's interior, the ability of the early settlers to explore and exploit the resources of this region were limited.

Artesian water was discovered in this vast interior region in the late 1870s and eventually most of the 4700 flowing artesian waterbores were drilled into the artesian aquifers in the Cadna-owie Formation and Hooray Sandstone aquifers, the main exploited confined aquifers in the Lower Cretaceous–Jurassic sedimentary sequence (Habermehl (1980) [668]; Habermehl (2001) [669]). In addition, the overlying Cretaceous aquifers are tapped by 20 000 pumped waterbores. This degree of exploitation led to a significant drawdown of the artesian groundwater levels and by 1970–2000, only 3100 wells remained flowing under artesian pressure and many of the artesian bores which ceased flowing were pumped, usually by windmills (Habermehl (1980) [668]; Radke et al. (2000) [670]). Recent estimates of the artesian groundwater in storage in the Great Artesian Basin (8.70×10^{12} – 1.0×10^{15} m³) make it one of the largest artesian aquifers in the world (Radke et al. (2000) [670]). Investigations including the geology, groundwater hydrology and borehole measurements have been conducted since the early 1900s, but a significantly increased scientific effort has been in effect beginning in the early 1970s to understand the hydrogeology, hydrodynamics, hydrochemistry and isotope hydrology characteristics of this system, as well as its recharge, discharge and groundwater movement.

In the following sections, a case study is developed to demonstrate how the Eastern and Central Great Artesian Basin was studied, quantified and evaluated. This case study deals predominantly with the structure and components of the scientific study of very old groundwater and places this in a logical framework, so that the knowledge, precedents and the lessons of the Great Artesian Basin can be applied to other systems.

The Great Artesian Basin comprises multiple subsystems or three sedimentary basins which are hydraulically connected, the Eromanga, Surat and Carpentaria Basins (Fig. 13.1), with each system subject to differing developmental pressures as well as unique recharge flow and discharge conditions. Jack (1923) [671] recognized the convergence of two separate flow systems near longitude 138°E characterized by high alkalinity waters from the east and high sulphate waters from the west. In this case study, the focus will be on the primary, long timescale flow within the Central Eromanga Basin portion of the Great Artesian Basin. The primary groundwater use in the Central Eromanga Basin is the pastoral industry, with an emphasis on cattle for beef and sheep for wool. Additionally, the artesian



FIG. 13.1. The Great Artesian Basin of Australia (from Radke et al. (2000) [670]). The basin is composed of several sub-basins that are both hydrologically and structurally identifiable. The recharge areas, the reconstructed 1880 potentiometric surface and the inferred flow directions are also shown.

groundwater is also the vital supply for town water and homesteads, and for the petroleum (since the 1960s) and mining (since the 1980s) industries. The driving economics of the Basin are utilization of a sustainable resource, with conservation, rehabilitation and/or removal of some waterbores. As the artesian groundwater in this part of the Great Artesian Basin has some of the longest flowlines and some of the slowest flow rates, it provides an end member for the application, analysis and evaluation of methods for dating very old groundwater.

Habermehl (1980) [668], Habermehl (2001) [669], and Habermehl and Lau (1997) [672] set the stage for detailed scientific investigations of the Great Artesian Basin system and the individual studies discussed below. The discussion in the following sections is largely an overview of the information contained within the individual studies with a historical context to elucidate how dating methods and field sampling were guided by existing information. The reader is referred to these primary literature sources for greater detail. Radke et al. (2000) [670] provide details about the field sampling and detailed interpretations of the combined geological, hydrogeological, hydrodynamics, hydrochemical, radiochemical and isotopic analyses, and is an example of how information can be combined, integrated and utilized for the fullest understanding of very old groundwater basins.

13.2. DEPOSITION, STRUCTURE AND HYDROGEOLOGY OF THE EASTERN GREAT ARTESIAN BASIN

The primary deposition of the sediments comprising the aquifers and the aquitards of the Great Artesian Basin began with an intracratonic downwarp (Shaw (1990) [673]; Veevers (1984) [674]) of the eastern Australian continent. During Jurassic–Cretaceous (200–100 Ma) time, fluvial and fluviolacustrine sediments were deposited in the three constituent sedimentary basins of the Great Artesian Basin (the Eromanga, Surat and Carpentaria Basins; Senior et al. (1978) [675]), as a result of drainage from the east, west and south. Rising sea levels in the early Cretaceous deposited shallow marine sediments over much of the previous fluvio-lacustrine sequences from the north with maximum marine inundation around 120–110 Ma (Struckmeyer and Brown (1990) [676]). Major uplift of the continent commenced around 95 Ma ago and reached 200 m over a time span of 110–60 Ma (Gurnis et al. (1998) [677]). These fluvio-lacustrine and marine sediments were converted to a hydrogeological groundwater system by regional uplift along the eastern margins of the continent between 10–15 Ma (Senior and Habermehl (1980) [678]) and 5 Ma ago (Toupin et al. (1997) [679]). The eastern margin of the present Great Artesian Basin was marked by Jurassic and Cenozoic volcanism (Duncan and McDougall (1989) [680]). The present hydrogeological structure of the Great Artesian Basin is shown in Fig. 13.2.



FIG. 13.2. The regional geological and hydrogeological structure of the Great Artesian Basin of Australia (from Radke et al. (2000) [670]). It should be noted that north is to the left.

This hydrogeological history is important in the subsequent evaluation because the residence times of groundwaters in the Great Artesian Basin (of the order of 1 Ma) may or may not have had time to flush connate waters from the aquifers in the Cadna-owie Formation and Hooray Sandstone, and/or from the overlying marine and continental connate waters in the Cretaceous aquifers. Secondly, because Cenozoic volcanism was common along the eastern margin of the Great Artesian Basin, specific locales have been 'spiked' with components representing contact with the volcanic centres including low ⁸⁷Sr/⁸⁶Sr groundwater (Collerson et al. (1988) [681]) and high ³He/⁴He ratios (Torgersen et al. (1987) [682]).

After the uplift of the eastern margins, it is likely that Australia was latitudinally positioned to benefit from coastal rains in summer along the north-east slopes of the Great Dividing Range that include parts of the eastern recharge zone as well as monsoon rains that provide precipitation for the main recharge areas on the western slopes of the Great Dividing Range and that can penetrate deeper into the arid continental interior. The palaeoclimatic records of Lake Eyre (Magee et al. (2004) [683]) and the fluvial records of the interior (Nanson and Price (1999) [684]; Nanson et al. (1992) [685]) suggest a clear trend towards aridity from 130 ka to the present. The analysis of Torgersen et al. (1985) [686] and Torgersen et al. (1988) [687] suggests that Pleistocene–Holocene climates in the Gulf of Carpentaria region (northern parts of the Great Artesian Basin) were similar to the present.

13.3. SETTING THE STAGE

The synthesis of Habermehl (1980) [668] summarized the geology and hydrogeology of the Great Artesian Basin, its primary aquifers and its fundamental chemical characteristics. Hydraulic conductivities of the aquifers are found to be generally in the range of 0.1-10 m/d with transmissivities



FIG. 13.3. Regional drawdown (m) of the potentiometric surface of the Cadna-owie–Hooray aquifer following development during the period 1880–1970 (from Habermehl (1980) [668]; copyright Commonwealth of Australia).



FIG. 13.4. Recharge, natural spring discharge areas and directions of regional groundwater flow in the primary Cadna-owie–Hooray aquifer of the Great Artesian Basin based on 1980 data sources (from Habermehl (1980) [668]; copyright Commonwealth of Australia). These inferred flowlines were used to guide the sampling locations for the 1982 and 1985 fieldwork (should be compared with Fig. 13.1).

on the order of 1–2000 m²/d. Artesian pressure heads had been mapped and the 1970 potentiometric contours defined the drawdown of potentiometric head and the loss of storage relative to the reconstructed 1880 (pre-development) potentiometric head (Fig. 13.3). This reconstruction and the bore-measured hydraulic conductivities enabled the numerical groundwater flow model of Seidel (1980) [688]; and the interpretation and definition of artesian groundwater flow directions (Fig. 13.4) and estimates of flow velocities for broad sections of the Great Artesian Basin. Regional scale applications of the model were developed (Habermehl and Seidel (1979) [689]), and model application and calibration were reported in Seidel (1980) [688]. Subsequent updates of artesian groundwater flow models have preserved these basic characteristics while defining details. The basic bidirectional artesian groundwater flow pattern that defines the eastern and central Great Artesian Basin from the western Great Artesian Basin was confirmed by the distribution of water chemistry types and confirmed the preliminary analysis of Jack (1923) [671] and in more detail by Habermehl (1986) [690]. The original hydrodynamic model of Seidel (1980) [688] was subsequently replaced by (steady state and transient) MODFLOW models described by Welsh (2000) [691], Welsh and Doherty (2005) [692], and Welsh (2006) [693].

13.4. STABLE ISOTOPE AND ¹⁴C MEASUREMENTS

Airey et al. (1979) [578] reported stable isotope (²H, ¹⁸O) measurements from bores within the eastern part of the Great Artesian Basin and showed that the composition was consistent with



FIG. 13.5. Chemical profiles along multiple flowlines within the Central Eromanga Basin of the eastern Great Artesian Basin. (a) Chloride, (b) sodium, (c) bicarbonate, (d) initial bicarbonate based on a ¹³C balance. The solid lines indicate 8-point moving averages of all wells except those in parentheses. Differing symbols represent various flowlines within the central Eromanga Basin. The insert in part (a) shows the variation of rainfall for the region over the past 120 ka. These data (from Airey et al. (1979) [578]) provided guidance for 1982 fieldwork.

a rainwater source and minimal interaction with the host rock. The minimal variation in the stable isotope ratios along apparent flowlines indicated a minimal climate signal over the timescale represented by the transect and the time interval allowed by the bore spacing. Transects of Na, Cl and HCO₃ indicated some co-variation down flowlines (Fig. 13.5) that may or may not have resulted from rainfall variations (Kershaw (1978) [694]; Kershaw (1994) [695]; Kershaw and Nanson (1993) [696]). Carbon-13 ratios were shown to co-vary with HCO₃ (Calf and Habermehl (1984) [697]). This variation was interpreted as a two-component system where HCO₃ introduced during recharge increasingly reacts with and is diluted by dissolved CaCO₃ of marine origin along the flow path.

13.5. THE 1982 FIELDWORK: STANNUM TO INNAMINCKA AND BONNA VISTA TO THARGOMINDAH

The above studies set the stage for the fieldwork in the Great Artesian Basin in 1982 which focused on sampling bores located along artesian groundwater flowlines (Fig. 13.6) identified by the potentiometric head and previous chemistry and stable isotope profiles. This field effort included sampling for ¹⁴C, ³⁶Cl and ⁴He that had the potential to quantify groundwater ages and flow rates within the eastern and central Great Artesian Basin in addition to chemistry and stable isotopes.

Stable isotope measurements from the 1982 fieldwork (Airey et al. (1983) [363]; Calf and Habermehl (1984) [697]) confirmed flowlines inferred from potentiometric heads (Habermehl (1980) [668]) (Fig. 13.7). Specifically, the deuterium contours show tongues of isotopically heavier water (Airey et al. (1983) [363]) that are consistent with those flow directions. Numerous ¹⁴C samples collected



FIG. 13.6. Sampling locations and bore numbers for both the 1982 and the 1985 fieldwork. Discussion of flowline evolution is typically discussed in terms of first and last waterbore (from Torgersen et al. (1992) [698]).

along the flowlines near the recharge areas confirmed the presence of relatively young groundwaters (for the Great Artesian Basin) that contained measureable modern carbon (>1%; Calf and Habermehl (1984) [697]). The transects of ¹³C generally confirmed flow directions inferred from the reconstructed potentiometric surface when the effects of increasing down gradient dissolution of marine carbonates identified in earlier work (Airey et al. (1979) [578]) were included. Bentley et al. (1986) [301] tested the ³⁶Cl groundwater dating method and developed its potential. Extensive ¹⁴C samples taken in and near the recharge area were used to define the initial condition for ³⁶Cl within the confined portion of the basin. Hydrological ages were used to select bores to define the recharge condition for ³⁶Cl; ¹⁴C was used to confirm the appropriateness of those bores.

The evaluation by Bentley et al. (1986) [301] of the ³⁶Cl samples taken in 1982 identified dissolution of 'dead' Cl (presumably from ancient marine deposits) and/or addition of Cl from other sources to be a significant diluent for ³⁶Cl. Consequently, ³⁶Cl ages are calculated by one of three end member equations. The comparison in Fig. 13.8 generally confirms the validity of the hydraulically calculated groundwater ages through the calculation of the isotope tracer ages. It is noted, however, that the interpreted ³⁶Cl tracer ages do not account for mixing of waters via flow convergences and it is noted that the artesian groundwater flowlines used for the 1982 expedition were specifically selected to minimize flow convergence.

The helium isotope collection of 1982 sought to verify the potential for ⁴He dating of groundwater as proposed by, for example, Davis and De Wiest (1966) [699] and within the background of work that had already been conducted (Andrews (1977) [536]; Andrews and Lee (1979) [577]; Heaton and Vogel (1979) [700]; Marine (1976); Marine (1976) [701]; Torgersen (1980) [535]). Torgersen and Clarke



FIG. 13.7. Contours of deuterium isotopes (top) show a tongue of isotopically heavy water following the trends in flow directions seen in Fig. 13.4. Contours of ${}^{13}C$ isotopes (bottom) reflect the trend in flow directions and the dissolution of marine carbonates (from Airey et al. (1983) [363]).

(1985) [293], working with knowledge that the apparent hydraulic groundwater ages had been confirmed by ³⁶Cl measures, showed that (relatively) 'young' groundwaters of the Great Artesian Basin increased their ⁴He concentration at a rate that was consistent with a ⁴He source derived from local sources within the aquifer sandstones. However, further along flowlines in 'older' groundwaters, the rate at which ⁴He increased was up to 74 times the rate of in situ production (Fig. 13.9). Measurements of ²²²Rn in the 1982 groundwater samples showed no significant increase in the ²²²Rn activity in the older portion (high ⁴He flux region) of the flowline and, thus, no evidence that a stronger, local, in situ source of ⁴He was acting to increase the rate of ⁴He introduction. These helium results indicated the predominance of an external source of ⁴He that was consistent with a basal flux derived from U–Th series decay in the Earth's crust beneath the Great Artesian Basin. Most importantly, the inference of a large basal flux of ⁴He was supported by the simple hydraulic flow model of Torgersen and Ivey (1985) [93] that accounted for the delay time (see Fig. 13.9) before the enhanced rate of ⁴He accumulation (the basal



FIG. 13.8. ³⁶Cl/Cl versus ³⁶Cl concentration for the Great Artesian Basin (top) and the comparison (bottom) of apparent ³⁶Cl tracer ages to apparent groundwater ages calculated from hydraulic properties (from Bentley et al. (1986) [310]; reproduced with permission of the American Geophysical Union).



FIG. 13.9. Helium concentrations versus groundwater hydraulic age (as supported by ³⁶Cl dates (Bentley et al. (1986) [310])) for the Great Artesian Basin, Australia as deduced from the 1982 fieldwork. For groundwaters younger than 40 ka, the accumulation rate is 4.6×10^{-12} cm³ STP ⁴He \cdot cm⁻³_{H2O} \cdot a⁻¹ which agrees with the calculated rate ($A_{He} = 1$) of 3.95×10^{-12} cm³ STP ⁴He \cdot cm⁻³_{H2O} \cdot a⁻¹. For groundwaters greater than 100 ka, the rate of accumulation is 2.91×10^{-10} cm³ STP ⁴He \cdot cm⁻³_{H2O} \cdot a⁻¹ or 74 times in situ production. An external bottom boundary flux provides the best explanation for the source and the timescale over which it can be seen (Torgersen and Clarke (1985) [293]).

flux) was observed. Owing to the predominance of this external ⁴He source, the ⁴He tracer ages were never calculated from the Great Artesian Basin ⁴He measurements.

Helium isotope measurements from the 1982 and 1985 expeditions (Torgersen et al. (1987) [682]) showed that the isotope ratio of helium accumulating along most flow paths was consistent with the calculated in situ production ratio and was, additionally, indistinguishable from an expected deep crustal production ratio (both order 10⁻⁸; Fig. 13.10). However, some paths showed ³He/⁴He ratios that were significantly elevated (Fig. 13.10) and suggested a mantle source of helium (³He/⁴He ratios of the order of 10⁻⁵). These data suggest a point source input of a ³He-rich component that is diluted along the groundwater flow path by mixing and addition of helium from the basal fluxes to the in situ production. This stable helium tracer, thus, defines a unique source region within the recharge area that can be tracked downstream to define a flow path. This ³He-rich tracer, thus, further defines and supports the flow paths inferred by Habermehl (1980) [668] from the potentiometric surface. In addition, Collerson et al. (1988) [681] showed that recharge area groundwaters were 'spiked' with low ⁸⁷Sr/⁸⁶Sr ratios (and a higher Ca/Sr ratio) as a result of Cenozoic volcanic intrusions, and Jurassic and



FIG. 13.10. Mantle ³He is identified in portions of the two flowlines of the Great Artesian Basin (Fairlight Trust to Wilfred Downs and Juanbong to Bonna Vista; lower right numbers in parentheses indicate bore number for cross-referencing with the top two figures) based on the occurrence of the high ratio in ³He/⁴He as seen by the slope of the line. The occurrence of Cenozoic volcanism (left) in the area of recharge and the groundwater flowlines (top right) show how this signal is carried into the interior of the Great Artesian Basin (from Torgersen et al. (1987) [682]; reproduced with permission of the American Geophysical Union).

younger volcanic activity that was active in and along the eastern margin of the sedimentary basin of what would become the Great Artesian Basin (Fig. 13.11). The downstream dilution of this recharge area ⁸⁷Sr/⁸⁶Sr 'spike' again serves to strongly support the validity of the flowlines identified from potentiometric surfaces.

Torgersen et al. (1989) [573] show that ⁴⁰Ar results appear to follow the same dynamics as ⁴He in the Great Artesian Basin and are also consistent with in situ production followed by input from an external basal flux. The ⁴He and ⁴⁰Ar data are generally explained by similar processes but the ⁴He/⁴⁰Ar ratio remains quite variable. This suggests that these deep crustal noble gas fluxes are decoupled. Decoupling of ⁴He and ⁴⁰Ar from their U–Th series and K sources is likely accomplished by processes at the grain scale including recoil, diffusive release and dissolution as well as large scale fracturing that



FIG. 13.11. The evolution of dissolved ⁸⁷Sr/⁸⁶Sr within two flowlines of the Great Artesian Basin (north is Stannum to Innamincka and south is Bonna Vista to Thargomindah). The low ⁸⁷Sr/⁸⁶Sr ratio is acquired in the recharge zone, likely via contact with Cenozoic volcanics (see Fig. 13.9 and note also the acquired ³He signature). As the flowing groundwaters dissolve the host rock (⁸⁷Sr/⁸⁶Sr ~ 0.7111) and marine carbonates (⁸⁷Sr/⁸⁶Sr ~ 0.709234) in situ, that end member is steadily acquired in the dissolved phase (after the measurements of Collerson et al. (1988) [681]).

will additionally separate ⁴He and ⁴⁰Ar (Torgersen and O'Donnell (1991) [543]). Given the relative signal strengths, the ⁴⁰Ar results suggest that ⁴He is more useful for basins with very old groundwater.

13.6. THE 1985 FIELDWORK: FAIRLIGHT TRUST TO CLAYTON, ATHOL TO MUTTI MUTTI AND MT. CRISPE TO CURDIMURKA

In continuing to build a knowledge base of the flow paths and flow rates of the eastern Great Artesian Basin, fieldwork in 1985 addressed additional flowlines in the eastern and central Great Artesian Basin as well as a flowline in the western Great Artesian Basin that is not included in this discussion. The flowlines sampled explore the northern area of the basin and the role of converging flowlines as a complication in the application and use of tracer age calculations.

Torgersen et al. (1991) [300] identified an increase in Cl and SO₄ down the flowline for the Athol to Mutti Mutti group which also showed ³⁶Cl ages on the high side of hydraulic ages (see Fig. 13.12). A discontinuous ³⁶Cl evolution is distinct near Meerabooka where the east–west transect possibly intersects the north–south transect. Distinct addition of Cl is also evident near the end of the north–south transect at Clayton bore, as flowing groundwater rises from depth and is subject to convergent mixing. The impact of such mixing on the calculated tracer age was estimated based on linear mixing along an exponential decay curve. For this flowline, convergent mixing was suspected to cause minimal offset of the apparent tracer age.

Torgersen et al. (1992) [698] combine the helium isotope data of 1982 and 1985 fieldwork, and show the area of highest He concentration to be coincident with the oldest water and the lowest



FIG. 13.12. Chlorine-36 measures along the Fairlight Trust to Clayton flowline show a distinct discontinuity at Meerabooka, possibly indicating flowline mixing as deduced by both the ³⁶Cl/Cl versus the ³⁶Cl plot (bottom) and the tracer ³⁶Cl age versus the hydraulic groundwater age (top) (from Torgersen et al. (1991) [300]; reproduced with permission of the American Geophysical Union).

(and near radioequilibrium) ³⁶Cl concentration (compare Figs 13.13 and 13.14). The helium data also show the impact of the western recharge area and the limited recharge along the north-western recharge margin.

13.7. MODELLING ³⁶Cl AND ⁴He

The results of the 1982 and 1985 fieldwork for both ³⁶Cl and ⁴He presented new data and new methods for the evaluation of very old groundwater. Discussion in the literature regarding the approach, assumptions and necessary conditions for the application of new methods (Bentley et al. (1986) [310]) is common. Andrews and Fontes (1991) [702], Andrews and Fontes (1993) [703], Fontes and Andrews (1993) [704], and Mazor (1992) [705] presented an evaluation of Great Artesian Basin ³⁶Cl data that explained spatial variations in ³⁶Cl as the result of mixing between groundwaters along flowlines and


FIG. 13.13. Contours of ⁴He in the Great Artesian Basin compiled from the 1982 and 1985 fieldwork. High ⁴He concentrations clearly delineate the regions of oldest water within the southern Central Eromanga Basin (Torgersen et al. (1992) [698]) and concur with the ³⁶Cl contours (Fig. 13.14).

deep, ³⁶Cl-'dead' waters but presented no mechanisms by which (near instantaneous) mixing could occur over such a broad region. Torgersen and Phillips (1993) [706], and Phillips (1993) [707] countered their argument showing that the conditions necessary to generate the mixing lines proposed by Andrews and Fontes (1993) [703] necessitated unreasonable end members and permitted virtually no radiodecay of recharge water ³⁶Cl and, thus, allowed no time for it to be transported. The exchange highlighted the need to evaluate the role of mixing in the interpretation of apparent ³⁶Cl ages. Bethke et al. (2000) [94], Park et al. (2002) [90] and Radke et al. (2000) [670] included such effects in their models.

Mazor (1995) [580], Mazor and Nativ (1992) [708], and Mazor and Nativ (1994) [709] suggested that helium in the 'older' portions of the Great Artesian Basin could be explained as the result of water trapped in stagnant compartments of the aquifer. However, among a number of points raised by Torgersen (1994) [710], such stagnation is inconsistent with the continuing evolution of ⁸⁷Sr/⁸⁶Sr (Collerson et al. (1988) [681]) and would require not only that flow stopped in stagnant zones but also that geochemical processes of mineral dissolution were halted in a unique increasing sequence. The discussion highlights the need to examine all of the ancillary physical, chemical and isotopic data available, including the progression in geochemical reactions, stable isotopes and tracers, to establish a means to validate the basic assumptions used for calculating groundwater flow velocity and age. This synthetic approach to analysis (all together) was adopted by Radke et al. (2000) [670] for their benchmark analysis of the Great Artesian Basin.

Zhao et al. (1998) [98] evaluated the effect of hydrodynamic flow in a typical confined aquifer on the distribution and accumulation of ⁴He in the flowing groundwaters. Their modelling suggests that flow divergence and convergence and especially upflow in a discharge zone can induce significant mixing (see also Goode (1996) [69]). The Zhao et al. (1998) [98] study, thus, begins the process of questioning the application of piston flow mechanics to either hydraulic ages or groundwater dating methods. Bethke et al. (2000) [94] and Bethke et al. (1999) [95] undertook full-scale modelling of



FIG. 13.14. Contours of ³⁶Cl from Radke et al. (2000) [670]. The primary recharge areas (high ³⁶Cl) are clearly delineated as is the locale for very old groundwater (low ³⁶Cl). The agreement between the areas of low ³⁶Cl and high ⁴He (older) and between high ³⁶Cl and low ⁴He (younger) (Fig. 13.13) is clear.

the Great Artesian Basin groundwater flow system, including the ⁴He accumulation and concluded that the distribution of ⁴He is controlled not only by lateral flow but also by upflow and downflow regions that develop in response to basin topography and structure. This modelling effort showed that the spatial distribution of ⁴He can be quantitatively reconciled with groundwater flow patterns using a 3-D modelling framework. Similar modelling of the ³⁶Cl dynamics (Park et al. (2002) [90]) again confirmed the need to consider 3-D flow in aquifer systems and the role of upflow, downflow and

convergent flow in the reconciliation of hydraulic ages with tracer based ages. The summary manuscript (Bethke and Johnson (2008) [84]) reiterates these principles.

13.8. GEOCHEMICAL MODELLING OF GROUNDWATER REACTION PATHS

Herczeg et al. (1991) [711] conducted a detailed analysis of the groundwater geochemistry from the 1985 fieldwork using PHREEQE (Parkhurst et al. (1980) [160]). That study explained the increase in total dissolved solids (TDS) along flowlines and distinct chemical differences between the eastern Great Artesian Basin (Na–HCO₃ type) and the western Great Artesian Basin (Na–SO₄–Cl type) waters. Figures 13.15 and 13.16 show clearly the strong increase in alkalinity, DIC and δ^{13} C along eastern Great Artesian Basin groundwater flowlines as well as the slowly increasing Na, Cl and TDS, and the decreasing Ca and Mg. Herczeg et al. (1991) [711] discussed the increase in TDS as a result of: (i) mixing of flowline groundwaters with saline waters within the deeper portions of the basin; (2) ion filtration through mudstone membranes; and (3) dissolution of evaporates, carbonate minerals or other minerals in situ. They inferred that saline waters most likely originated from the overlying Cretaceous marine sediments and were introduced by downward diffusion into the aquifers of the Cadna-owie Formation and Hooray Sandstone. However, given the upward leakage of artesian groundwater from



FIG. 13.15. Evolution of Na and K chemistry and TDS along the 1985 sampling lines as reported by Herczeg et al. (1991) [711]. It should be noted that the western Great Artesian Basin (Mt. Crispe-o-Curdimurka) is distinct from the eastern Great Artesian Basin and that mixing with the eastern Great Artesian Basin flow is apparent at the end of the western flowline.

the deeper, stratigraphically lower aquifers to the stratigraphically higher Cretaceous aquifers, mixing is likely to be slight. Herczeg et al. (1991) [711] further inferred that ion filtration is likely to be minimal based on the ³⁶Cl studies of Bentley et al. (1986) [301], and concluded that variable evapotranspiration in the recharge areas in combination with mineral dissolution along flowlines represented the most plausible mechanism for the chemical evolution observed in Figs 13.15 and 13.16.

The eastern Great Artesian Basin flowline trends of increasing Na alkalinity and DIC together with the decreasing Ca and Mg were evaluated (Herczeg et al. (1991) [711]) in terms of a model proposed by Blake (1989) [712] which includes: (i) dissolution of carbonate minerals resulting in increased Ca, Mg and HCO₃; (ii) cation exchange of Ca and Mg for Na in clay minerals, followed by; (iii) a reaction of Na with kaolinite to produce Na–smectite. Reasoning that the down gradient flow increase in alkalinity can only be accomplished by carbonate dissolution in the presence of high pCO₂, they concluded that CO₂ respiration by plants in the recharge zone can drive the δ^{13} C of DIC resulting from these reactions from an initial –15‰ to approximately –12‰. However, to enable the reactions to continue requires the addition of CO₂ as a result of anaerobic fermentation and reduction of CO₂ to methane.



FIG. 13.16. Evolution of alkalinity, ¹³C, Ca^{+2} and Mg^{+2} chemistry along the 1985 sampling lines as reported by Herczeg et al. (1991) [711]. It should be noted that the western Great Artesian Basin (Mt. Crispe-to-Curdimurka) is distinct from the eastern Great Artesian Basin and that mixing with the eastern Great Artesian Basin flow is apparent at the end of the western flowline.

13.9. THE 2000 BENCHMARK AND SYNTHESIS

Following the seminal paper of Habermehl (1980) [668], the publication by Radke et al. (2000) [670] is a compilation and synthesis of the hydrogeology, hydrochemistry and isotope hydrology of the Great Artesian Basin. It is based largely on samples and laboratory results of the fieldwork by Habermehl and others during the 1970s, 1980s and 1990s, with some additions of analyses and results from Queensland and South Australia. This benchmark paper synthesized groundwater flow models, geochemical reaction and transport models, and the dating of the artesian groundwater in the aquifers of the Cadna-owie Formation and Hooray Sandstone to infer the timescale of recharge and the in situ flow rates. It further utilized distinctive hydrogeochemical anomalies to infer details of groundwater flow in these aquifers. In the few paragraphs that follow, these findings are summarized, especially as they relate to this case study and the additional detail deduced through the use of modern hydrodynamic and hydrogeochemical codes.

The mapped (Radke et al. (2000) [670]) spatial distributions of modern ¹⁴C (Fig. 13.17) and ³⁶Cl (Fig. 13.14) are consistent with previous work. The location of very old groundwater (near equilibrium values of ³⁶Cl) is consistent with the mapped regions of very high ⁴He (Fig. 13.13). Recharge, flow direction and discharge zones (Figs 13.18 and 13.19) reported by Radke et al. (2000) [670] were similar to the original diagrams of Habermehl (1980) [668]. Recharge is estimated to be on the order of 10¹² L/a with an unknown proportion distributed between rainfall and river infiltration. This current recharge rate may be enhanced as a result of the previous century of drawdown. Natural discharge is of the order of 0.5×10^{12} L/a with most discharge via upward leakage and minimal discharge via outlet springs (see Table 13.1). The range of estimates for Great Artesian Basin storage of water is significant (Table 13.1), leading to vastly different simple estimates of groundwater residence times (storage volume divided by input rate (or output rate)). The climate reconstructions of, for example, Magee et al. (2004) [683] suggest a decline in rainfall over Pleistocene time and discharge springs have experienced a significantly reduced head over the past century. Thus, it is not anticipated that discharge rates contribute significantly to this residence time discrepancy. Using the Habermehl and Seidel (1979) [689] estimated storage (10¹⁸ L) would yield recharge-based and discharge-based residence times of 1 and 2 Ma which are in general agreement with estimates from ³⁶Cl and hydraulic estimates. The precision and the precise meanings of these differences in storage are not clear but it may be the difference between in situ storage and recoverable storage.

The eastern Great Artesian Basin is characterized by increasing TDS and alkalinity along flowlines. Chemical anomalies are noted along the Birdsville-Diamantina Track with additional high Cl anomalies along the Eulo-Nebine Ridge area. Groundwater temperatures increase with depth of the aquifers and anomalous geothermal gradients throughout the basin (Habermehl and Pestov (2002) [713]; Habermehl et al. (2002) [714]) and the Central Eromanga Basin shows a distinct increase in Na especially when expressed as sodium excess (e.g. [Na] – [Cl]). High fluoride concentrations occur over basement highs where the aquifer is possibly in contact with igneous and metamorphic basement rocks. The stable isotopic signature of the groundwater suggests that heavy monsoon rainfall in the eastern recharge zone is responsible for the majority of recharge although evapotranspiration before recharge may be significant. Stable isotopes throughout the basin (Radke et al. (2000) [670]) show little variation. This apparent lack of any palaeoclimatic signature may be the result of minimal climatic variation and/or attenuation by dispersive mixing. Hydrodynamic models of groundwater flow calibrated against ¹⁴C in and near the recharge areas suggest flow rates range from 1.4 to 2.9 m/a (Radke et al. (2000) [670]). Flow rates calculated by hydrodynamic models and estimates of the ³⁶Cl controls indicate several areas with artesian groundwater flow rates as low as 0.03–0.3 m/a (see Fig. 13.18). Very slow flow regions are areas of predominant water loss via upward leakage although the hydrochemical signatures in low flow areas also indicate the possibility of downward diffusion of some ions from overlying Lower Cretaceous aquitards into the Lower Cretaceous-Jurassic aquifers (Fig. 13.19). It would appear that discharge from artesian springs (11%) is small compared to discharge via upward leakage (89%) for



FIG. 13.17. Contours of ¹⁴C (in per cent modern) from Radke et al. (2000) [670]. The primary recharge areas are clearly delineated and the loss of ¹⁴C in the older regions of the Great Artesian Basin is clear.

a total natural discharge of 0.5×10^9 L/a. However, spring discharges might have been much larger in past geological times (Prescott and Habermehl (2008) [715]). Anthropogenic discharge (0.57×10^9 L/a) is estimated to currently be slightly in excess of natural discharge.

Overall, the benchmark paper of Radke et al. (2000) [670] is in general agreement with earlier studies including the flow rate and age of groundwater inferred from ¹⁴C, ³⁶Cl and ⁴He studies. However, their detailed analysis appears to identify high flow regimes with lower salinities in the shallow depth of burial regions. NETPATH (Plummer et al. (1994) [120]) modelling of Great Artesian Basin geochemistry produced results in agreement with the overall net reactions postulated by Herczeg et al. (1991) [711] but suggested that carbonate dissolution reactions are the primary driving mechanism rather than smectite–kaolinite transformations. Thermal convection (Pestov (2000) [716]) has not been substantiated.



FIG. 13.18. Benchmark synthesis of flow rates and chemical evolution of the Great Artesian Basin (Radke et al. (2000) [670]).

13.10. CONTINUING WORK IN THE GREAT ARTESIAN BASIN

As a result of the large data base available for the Great Artesian Basin, several anomalies have been identified within the recharge areas (Collerson et al. (1988) [681]; Torgersen et al. (1987) [682]). The TACEM anomalies are found near wellbores named Tambo, Augathella, Charleville, Eddystone and Mitchell (Radke et al. (2000) [670]). Other anomalies are found along artesian groundwater flow paths. The groundwaters in the central and western Queensland and northern South Australia portions of the Great Artesian Basin (and, in particular, along the Birdsville Track) are characterized by higher temperatures than anticipated (Habermehl and Pestov (2002) [713]). TDS are low along the Birdsville Track compared to central and western Queensland and South Australia. This trend is inferred to be the result of mixing induced by the rapid rise in elevation of the crystalline bedrock



FIG. 13.19. Benchmark synthesis of the Great Artesian Basin showing flow rates, upward leakage and chemical evolution (increasing salinity; blue to orange) displayed over the basal structure of the Cadna-owie–Hooray aquifer (from Radke et al. (2000) [670]).

			Storage	Residence time: storage /rate
Natural recharge	Rainfall plus rivers	1012 L/a	(1)	8.7 ka
			(2)	1 Ma
			(3)	65 ka
Natural discharge	Upward leakage	$0.45 imes 10^{12} ext{ L/a}$		
	Springs	$0.05\times 10^{\rm 12}~L/a$		
Natural discharge	Sum	$0.5\times 10^{12}\ L/a$	(1)	17.4 ka
			(2)	2 Ma
			(3)	130 ka
Anthropogenic discharge	Waterbores	$0.5 imes 10^{12} ext{ L/a}$		
Storage (1)	Radke et al. (2000)			$8.7 imes 10^{15}$ L
Storage (2)	Habermehl and Senior (1979)			$1 \times 10^{18} L$
Storage (3)	QDNRW (2007)			$6.5 imes 10^{16} m L$

TABLE 13.1. WATER BALANCE FOR THE GREAT ARTESIAN BASIN, AUSTRALIA: FLUXES, STORAGE AND RESIDENCE TIMES

based on geothermometry studies of Pirlo (2004) [717]. Evidence for this mixing of waters is provided by the discord among silica geothermometers and cation geothermometers. As silica geothermometers re-equilibrate relatively quickly compared to cation geothermometers, the low Si temperatures and the high cation temperatures indicate mixing from deeper, hotter (faster reactions) regions and shallow regions.

O'Shea and Jankowski (2006) [718] have performed hierarchical cluster analysis on the chemical compositions in the Coonamble Embayment (south-eastern Great Artesian Basin and an area in New South Wales not discussed above) and compared them with traditional Piper diagrams (Piper (1944) [719]), Durov diagrams (Chiligar (1956) [720]) and a modification of Piper analysis (Chada (1999) [721]). This cluster analysis indicates three main geochemical water types that can be associated with processes of ion exchange, precipitation and mixing from different sources. They were also able to identify an anomalous sample that is suspected to be influenced by magmatic sources of CO_2 . This indication of magmatic CO_2 is consistent with the location of other anomalies observed in ⁸⁷Sr/⁸⁶Sr (Collerson et al. (1988) [681]) and ³He/⁴He (Torgersen et al. (1987) [682]) that are geographically associated with the eastern recharge zone that was subject to considerable Cenozoic and pre-Cenozoic volcanism (Duncan and McDougall (1989) [680]).

Recharge, recharge processes and rates, detailed hydrochemistry and isotope studies, including stable (δ^2 H, δ^{18} O and δ^{13} C) and radioactive (14 C, 36 Cl) isotopes have been carried out in the Queensland (Kellett et al. (2003) [722]) and New South Wales (Habermehl et al. (2009) [723]) parts of the Great Artesian Basin and recharge rates range from 0.5 to 10 mm/a, with some higher values. A detailed study of recharge along the western margin and discharge in the south western region of the Great Artesian Basin commenced in 2009.

Shimada et al. (1998) [724], Shimada et al. (1999) [725] and Shimada et al. (1997) [726] sampled several transects in the Coonamble Embayment in 1996 and interpreted the hydrochemistry, and stable (δ^2 H, δ^{18} O and δ^{13} C) and radioactive (14 C, 36 Cl) isotope results for this south-eastern part of the Great Artesian Basin, which has its own recharge area.

Extensive sampling of flowing artesian waterbores tapping the aquifers in the Cadna-owie Formation and Hooray Sandstone was carried out in 2002 and 2003 along transects similar to the 1982 and 1985 transects, with additional transects in the Queensland, South Australia and Northern Territory parts of the Great Artesian Basin. This was followed in 2004 and 2005 by the construction of fully cored drill-holes through the Lower Cretaceous aquitards into the aquifers near the north-eastern recharge area and the south-western discharge area. Laboratory results on hydrochemistry, stable isotopes (8 Cl) and δ^{13} C), radioactive isotopes (14 C, 36 Cl) and noble gases (4 He, 3 He/ 4 He, Ne) were analysed and interpreted and confirm the results of earlier studies. Additional 36 Cl and 4 He measures continue to show they remain useful indicators for groundwater residence times of very old groundwater (Hasegawa et al. (2009) [727]; Mahara et al. (2009) [728]).

Chapter 14

KRYPTON-81 CASE STUDY: THE NUBIAN AQUIFER, EGYPT

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14.1. NUBIAN AQUIFER

The Nubian aquifer of north-east Africa is one of the world's largest fresh groundwater resources (~150 000 km³). An area in the Western Desert of Egypt, for which a number of earlier studies provided sufficient background data on the Nubian aquifer, was selected for the first application of the atom trap trace analysis (ATTA) method (Section 5.4.3) for measurement of ⁸¹Kr in groundwater. This area has relatively simple geology, potential for containing very old groundwater, and favourable characteristics for comparison of the ⁸¹Kr and ³⁶Cl methods (Sturchio et al. (2004) [5]). Before this work, little evidence regarding absolute groundwater residence time in the Nubian aquifer was available. Estimates of groundwater age in the range of 0.54×10^6 – 1.58×10^6 a had been obtained from He/Ar ratios (Himida (1967) [729]). A large number of ¹⁴C data had been obtained for the Nubian aquifer waters in Egypt (Fröhlich et al. (2007) [730]; Sonntag et al. (1979) [731]). Chlorine-36 data indicated possible residence times of up to ~9 × 10⁵ a (unpublished data¹).

14.2. METHODS

Nubian aquifer groundwater was sampled in May 2002 from six irrigation wells in major oasis areas of the Western Desert of Egypt for measurements of ⁸¹Kr, ³⁶Cl, ¹⁴C, ⁴He and other chemical and isotopic constituents. Dissolved gas was extracted from several 10³ kg of water at the field sites using the Bern vacuum-stripping method described above (Section 5.4.1). Krypton was separated from the extracted gas samples at Bern by molecular sieve absorption and gas chromatographic methods; LLC was used to confirm that the abundances of ⁸⁵Kr in these samples were indeed low (⁸⁵Kr/Kr < 3% of modern air) as expected for old groundwaters, verifying minimal air contamination during sampling. For normalization in ATTA analyses, a calibrated amount of ⁸⁵Kr was mixed with each Kr sample. The ⁸¹Kr/⁸⁵Kr ratios in the spiked Kr samples were then measured using ATTA at Argonne National Laboratory (Du et al. (2003) [249]). Chloride concentrations in water samples were measured by ion chromatography and Cl was then precipitated as AgCl for measurements of ³⁶Cl that were performed by AMS at the PRIME Lab of Purdue University. Noble gas samples were collected in copper tubes and measurements were performed on separate sets of samples at both ETH Zurich and Lawrence Berkeley National Laboratory. Aliquots of purified CO_2 were measured for ¹⁴C abundance at the University of Arizona accelerator mass spectrometry facility; these samples were obtained from a portion of the gas used for Kr extraction.

¹ STURCHIO, N., University of Illinois, PURTSCHERT, R., University of Bern, unpublished data.

14.3. KRYPTON-81 DATA

Results of the Nubian aquifer groundwater analyses for ⁸¹Kr are shown in Fig. 14.1 and Table 14.1. Krypton-81 is expressed in terms of the air-normalized ratio, $R/R_{air} = ({}^{81}Kr/Kr)_{sample}/({}^{81}Kr/Kr)_{air}$, where R_{air} is the modern atmospheric ratio (${}^{81}Kr/Kr)_{air} = 1.10 (\pm 0.05) \times 10^{-12}$ as measured by ATTA (Du et al. (2003) [249]). Measured R/R_{air} values in Nubian aquifer groundwater samples range from 4.8% to 52.6% modern. Using the simple expression for radioactive decay, and the ${}^{81}Kr$ decay constant $\lambda_{Kr} = 3.03 (\pm 0.14) \times 10^{-6}/a$, the ${}^{81}Kr$ tracer age t_{Kr} of a groundwater sample is given by:

$$t_{\rm Kr} = -\frac{1}{\lambda} \ln \left(\frac{R}{R_{\rm air}} \right) \tag{14.1}$$

The range of ages thus derived is $0.2-1.0 \times 10^6$ a (Fig. 14.1). These are apparent piston flow ages because the extent of age mixing within the sampled wells is unknown.

Ages increase progressively along flow vectors predicted by numerical hydrodynamic models (Brinkman et al. (1987) [732]), verifying distant lateral flow of deep groundwater towards the northeast from a recharge area south-west of Dakhla. The correspondence of ⁸¹Kr age with predicted hydrodynamic age indicates negligible input of ⁸¹Kr from subsurface sources, in agreement with theoretical calculations and conclusions reached from ⁸¹Kr measurements of groundwater from the Milk River Aquifer in Canada (Lehmann et al. (1991) [282]) and the Great Artesian Basin in Australia (Collon et al. (2000) [281]). The estimated diffusive loss of ⁸¹Kr to aquitards was limited to \leq 20% for the Great Artesian Basin (Lehmann et al. (2003) [256]), and is expected to be even lower within



FIG. 14.1. Map showing sample locations (red circles) in relation to oasis areas (shaded green), Precambrian basement areas (patterned) and other regional features. Groundwater flow in the Nubian aquifer is generally towards the north-east, but diverges towards the north and east as shown by arrows (Brinkman et al. (1987) [732]; Hesse et al. (1987) [733]). Krypton-81 ages are shown in blue numbers (in units of 10⁵ a).

Well name (depth)*	Cl (mg/L)	³⁶ Cl/Cl (10 ⁻¹⁵)	81 Kr/Kr (<i>R</i> / <i>R</i> _{air} %)	⁴ He (10 ⁻⁶ cm ³ STP/g)	¹⁴ C (pmC)	δ ² H (‰)	⁴⁰ Ar (10 ⁻⁵ cm ³ STP/g)
Dakhla Oasis							
Gum Horia (1200 m)	20	76.5 (±3.4)	52.6 (±6.1)	3.0 (±0.3)	n.a.	-81	57 (±6)
El Zayat 12 (720 m)	59	72.7 (±1.7)	30.6 (±3.6)	3.3 (±0.3)	<1.6	-82	33 (±3)
Kharga Oasis							
Sherka 36 (750 m)	95	12.2 (±5.1)	12.8 (±3.0)	43 (±4)	0.28 (±0.11)	-82	67 (±7)
Baris-Aden (600 m)	92	45.6 (±2.1)	22.8 (±3.0)	32 (±3)	3.26 (±0.21)	-81	50 (±5)
Farafra Oasis							
Farafra 6 (800 m)	24	65.0 (±3.0)	36.5 (±4.2)	3.7 (±0.4)	0.96 (±0.11)	-79	50 (±5)
Bahariya Oasis							
Bauti 1 (1200 m)	52	20.2 (±1.6)	4.8 (±3.8)	5.1 (±0.5)	n.a.	-81	40 (±4)

TABLE 14.1. ISOTOPIC DATA FOR NUBIAN AQUIFER WATER SAMPLES

Note: n.a. = not analysed; *sample locations shown in Fig. 14.1; 1σ errors in parentheses.

the Nubian aquifer because of the lower porosity and smaller proportion of aquitard formations within this aquifer system (see Figs 5.3 and 5.4).

Krypton-81 ages increase progressively with distance to the north and east of Dakhla; their areal distribution indicates a flow velocity of $\sim 2 \text{ m/a}$ from Dakhla towards Farafra, and a lower velocity towards Kharga and Baris and from Farafra to Bahariya. These observations are consistent with the distribution of hydraulically conductive sandstone within the aquifer and they provide support to some of the early hydrodynamic models (Brinkman et al. (1987) [732]; Hesse et al. (1987) [733]). South-westward extrapolation of the $\sim 2 \text{ m/a}$ flow rate inferred from the difference in ⁸¹Kr ages for Dakhla and Farafra is consistent with recharge in the area of the Uweinat uplift near the Egypt–Sudan border. In this area, the Nubian sandstone is exposed (or buried beneath sand sheets or dunes) at elevations between 200 and 600 m above sea level over a wide area, forming a broad catchment for recharge of the Nubian aquifer.

14.4. CHLORINE-36 DATA

Patterson et al. (2005) [43] presented ³⁶Cl data for 22 groundwater samples from the Nubian aquifer in the Western Desert of Egypt, including the six samples also measured for ⁸¹Kr. The areal distribution of groundwater ages derived from this data set is shown in comparison with Basin 2 hydrodynamic model ages in Fig. 14.2. The best estimates of groundwater ages from ³⁶Cl data range from about 2×10^5 to 7×10^5 a, and the distribution of these ages indicates flow from south to north, in agreement with ⁸¹Kr ages and hydrodynamic models. The ³⁶Cl ages agree with hydrodynamic model ages within ±30%.



FIG. 14.2. Map of the Western Desert of Egypt showing hydrodynamic ages (black numbers) and ³⁶Cl ages (red numbers) in the Nubian aquifer calculated from ³⁶Cl/Cl ratios and assuming $R_i = 130 \times 10^{-15}$, $R_{se}^{sandstone} = 5 \times 10^{-15}$ and $R_{se}^{shale} = 15 \times 10^{-15}$ (from Patterson et al. (2005) [43]). Age units are 10³ a.

14.5. CORRELATION OF ³⁶Cl AND ⁸¹Kr DATA

There is a good correlation between ³⁶Cl/Cl ratios and ⁸¹Kr ages (Fig. 14.3), in samples for which both measurements were made, providing a firm basis for calibrating apparent ³⁶Cl ages to an apparent value of (³⁶Cl/Cl)_{initial} = R_i for the Nubian aquifer. A best-fit curve through the data using the function:

$$R_{\text{meas}} = R_{\text{Se}} + (R_{\text{i}} - R_{\text{Se}}) \exp(-t_{\text{Kr}} \lambda_{\text{Cl}})$$
(14.2)

where $t_{\rm Kr}$ is the ⁸¹Kr age in years, $\lambda_{\rm Cl} = 2.30(\pm 0.02) \times 10^{-6}/a$ is the ³⁶Cl decay constant and $R_{Se} = 8(\pm 3) 10^{-15}$ is the secular equilibrium in situ production value for the aquifer (assuming constant Cl concentration in water) gives $R_i = 131(\pm 11) \times 10^{-15}$, which coincidentally agrees with the initial value of $125 (\pm 10) \times 10^{-15}$ estimated for the Great Artesian Basin (Love et al. (2000) [292]). Krypton-81 and ³⁶Cl ages for most of these samples agree within error, but two samples exhibit significant age discordance that may be explained by deviations from assumptions used for calculating the best-fit curve (i.e. different values of $R_{\rm Se}$ and/or $R_{\rm i}$ or addition of subsurface Cl). Stable Cl isotope ratios and Cl concentrations for these and other Nubian aquifer groundwater samples measured for ³⁶Cl (Patterson et al. (2005) [43]) indicate subsurface Cl addition for some samples and, in fact, age calculations taking into account added Cl using Eq. (14.2) (Section 5.5 and Chapter 6) yield ³⁶Cl ages in excellent agreement with ⁸¹Kr ages. These results demonstrate that the integrity of the ³⁶Cl chronometer is vulnerable to additions of Cl at any point along a flow path, whereas, in contrast, the potential for open system behaviour of Kr is minimal after water has reached the aquifer. Nonetheless, methods for correcting ³⁶Cl ages for subsurface additions of Cl and ³⁶Cl are well established (Section 5.5 and Chapter 6). The main uncertainty in ⁸¹Kr ages is diffusional exchange of Kr between different water masses (Section 5.1.2.2).



FIG. 14.3. Correlation of ${}^{36}Cl/Cl$ ratio with ${}^{81}Kr$ age. The blue line is an exponential best fit assuming a secular equilibrium ${}^{36}Cl/Cl$ ratio of 8×10^{-15} (with the input ratio R_i as a free fitting parameter).

14.6. HELIUM-4 DATA

Measured ⁴He and ⁴⁰Ar concentrations in the Nubian aguifer samples are provided in Table 14.1. Concentrations of 40 Ar range from 33–67 × 10⁻⁵ cm³ STP/g and indicate excess air incorporation at recharge. Ratios of 40 Ar/ 36 Ar were not measurably different from the atmospheric ratio of 295.5 ± 0.5, so it appears that ⁴⁰Ar production and accumulation within the sandstone aquifer is minimal. However, ⁴He concentrations $(3.0-43 \times 10^{-6} \text{ cm}^3 \text{ STP/g})$ are two to three orders of magnitude greater than the airsaturated water concentration of ⁴He at 20°C, indicating subsurface addition of ⁴He that could reflect groundwater age. ⁴Heter concentrations show apparently linear accumulation along the Dakhla-Bahariya flow path (Table 14.1), suggesting qualitatively that groundwater age increases by nearly a factor of two between Dakhla and Bahariya. Using rock compositions that gave the best fit of the measured ³⁶Cl/Cl data in the Basin 2 model, and by assuming that the aquifer is composed of 80% sandstone and 20% shale, the flux of ⁴He produced in situ, J_{He} , then equals $3.3 \times 10^{-12} \text{ cm}^3 \text{ STP} \cdot \text{g}^{-1} \cdot \text{a}^{-1}$ and the corresponding ⁴He residence times (assuming zero external flux of ⁴He into the aquifer) range from 870 to 1500 ka. These apparent ⁴He ages are two to four times greater than either the hydrodynamic ages or the ³⁶Cl ages, which indicates that the assumed ⁴He production rate or the assumption of zero external He flux is inaccurate. Thus, 50–80% of the ⁴He in these four samples may be from a source external to the aquifer. An external source of ⁴He is apparent in the Sherka-36 and Baris samples, for which ⁴He concentrations are much higher and ⁴He was not used to estimate residence time.

14.7. CARBON-14 DATA

Radiocarbon data for four of the ⁸¹Kr samples is given in Table 14.1. The CO₂ samples for which these measurements were made were purified from aliquots of the dissolved gas extracted for ⁸¹Kr measurements. Unfortunately, aliquots from two other samples were lost during shipping between laboratories because of damage to the package containing them. The fraction of modern carbon in these samples is uniformly low and ranges from about 0.01 to 0.03. These data constrain the upper limits of atmospheric contamination of the Kr samples as well as possible mixing fractions of young

groundwater, and are in good agreement with the constraints from ⁸⁵Kr data. The measured ¹⁴C activities of these samples are at the low end of the range for Nubian aquifer waters (Fröhlich et al. (2007) [730]), indicating minimal contributions from young groundwater.

14.8. HYDROGEOLOGICAL AND PALAEOCLIMATIC IMPLICATIONS OF GROUNDWATER AGE DATA

The concordance of the ³⁶Cl and ⁸¹Kr data supports mean groundwater residence times approaching 10⁶ a in the Western Desert of Egypt. A steady state, two dimensional hydrodynamic model incorporating constraints from ³⁶Cl and available measurements of aquifer hydraulic parameters yields groundwater velocities in the range of 0.5 to 3.5 m/a, consistent with residence times estimated from ⁸¹Kr (Patterson et al. (2005) [43]). A model proposed by Fröhlich et al. (2007) [730] estimates a recharge rate of 0.4 mm/a and a discharge rate of 0.65 mm/a for water in the deep portion of the aquifer. Further progress in understanding the aquifer hydrodynamics will require extensive, depth dependent sampling and measurement of multiple stable and radioactive isotopic tracers.

Stable isotope ratios of hydrogen and oxygen in the Nubian aquifer (and equivalent) groundwaters from across Saharan North Africa indicate a clearly defined continental isotope effect involving precipitation from air masses having an Atlantic moisture source; δ^2 H values decrease gradually from west to east with a geographic pattern resembling that observed in modern European groundwaters (Sonntag et al. (1979) [731]). In the deep Nubian aquifer samples, nearly constant δ^2 H values (from -82 to -79) as a function of ⁸¹Kr age reveal that this Atlantic moisture source was recurrent during all major pre-Holocene pluvial periods throughout the past 1×10^6 a. In contrast, the isotopic composition of modern precipitation in the study area, which mostly delivers moisture from the Mediterranean, is much less depleted in ²H (δ^2 H ranges from -28 to +14‰) (El Bakri et al. (1992) [734]). These observations indicate that Nubian aquifer groundwaters were recharged under a climatic regime in which there had been a persistent southward shift of the intertropical convergence zone relative to modern climate in the region.

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